

Analysis on the Effects of Cut-Outs in Hollow Inconel 718 Gas Turbine Shafts

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Abstract

Gasturbines are provided with cut-outs for minimizing vibrations. Round cut-outs are usually favored but there are various designs which offer more advantages over the circular shape. The objective of this work was to compare stress reduction during the induced vibration in the hollow gas turbine shafts by introducing different cut-outs. Round, square and elliptical cut-outs under different orientations were compared. It is observed that a square cutout at 45° orientation has the least stress concentration. This is due to the effective orientation of plastic strains along the principal axis.

Keywords

Static Analysis, Crack Propagation, Non Linear Analysis, Stress Concentration, Square Cutouts

1. Introduction

A gas turbine, known as a combustion turbine is an inward burning motor. It consists of an upstream rotary compressor coupled to a downstream turbine and an ignition chamber at the center. Gasturbines shafts accumulate oil from the vicinity and result in vibrations; hence they are provided with cutouts for minimizing vibrations by draining the oil. Cutouts are generally circular, square or elliptical in shape. The shape of the cutouts is dependent on their application. For example, sewer vents are either circular or roundabout. Similarly plane windows are rectangular in shape with chamfer at the corners [1]. In plane structures, definite shapes are found as access ports for electrical and mechanical systems or for the reduction of weight [2]. Practically round cutouts are favored due to its simple geometry but there are various designs which offer more advantages over the circular shape. The stress distribution around the cutouts and

along the shaft gives a clear idea of the geometry and orientation of cutouts for reduction of vibration in gas turbines [3].

Ghannadpour *et al.* [4] have demonstrated in their study that buckling strength of rectangular laminated composites reduces with increase in hole diameter. Also for elliptical cut-outs it is observed that buckling strength increases when loaded in the direction along their major axis. Sivakumara *et al.* [5] optimized the operating frequencies of the laminated composites by introducing cut-outs. Optimization was carried using Genetic Algorithm (GA) technique. It was reported that circular cut-out minimizes the weight for 1st and 2nd natural frequencies compared to elliptical cut-outs. Levraea *et al.* [6] investigated the variation in the frequencies of the panels with and without eccentric cut-outs and observed that the variation was less than 10% and increased with the cut-out size.

Rezaeepazh *et al.* [7] have developed analytical and numerical model to determine normal stress in composite plates of different cut-out shapes. Ahmed Noor *et al.* [8] have developed numerical model using first order shear theory to evaluate the thermal buckling of laminated composite with different cut-outs.

From the review of above [1]-[8], it is seen that most of the authors have worked on plates and composites subjected to cut-outs and have carried out the stress analysis. But very scarce amount of work reports on the analysis in a hollow shaft with the introduction of cut-outs. In the present work a comparative study is made for different cut-outs (round, square and elliptical) in hollow Inconel gas turbine shaft and the stress distribution is studied under induced vibrations conditions.

2. Methodology

A hollow shaft was created with the following dimensions. Outer diameter of shaft was taken as 75 mm, inner diameter as 65 mm and length as 300 mm. The diameter of circular cut-out was taken as 6 mm, elliptical cut-out dimension as 12 × 6 mm and square cut-out dimensions as 6 × 6 mm. The model was created using Catia V19 and cut-outs of square, elliptical and circular configuration were introduced perpendicular and inclined (45°) to the shaft axis. This was meshed with HEX (SOLID185) using ANSYS 14 and was subjected to torque. Analysis of the shaft with cut-out was carried out by subjecting it to its plastic limit. The maximum shear stress at cut-outs was tabulated and stress concentration is calculated by using the below formula.

Stress Concentration = Maximum Stress at cut out/Nominal Stress

$$K\alpha = \frac{\sigma_{\max}}{\sigma_{\text{nom}}} \quad (1)$$

The above equation is taken from ref. [9]. Using the torque equation nominal stress is calculated. ANSYS macros were written for different slots for stress calculation. Vonmises Stress, Principal Stress, Equivalent strain and plastic strain for the cut-out regions were calculated and tabulated. The results were compared

between cut-outs of different geometries.

2.1. Material Properties

Nickel based superalloys are used extensively in gas turbines and combustor areas of the motor. They have high creep and fatigue resistance, can withstand high temperatures for long periods of time and reduces processing and element energy costs. Inconel is an austenitic nickel-chromium based superalloy. They are resistant to oxidation and corrosion and are used in extreme environments. Up to temperatures of 650°C, Inconel 718 is usually used. The material properties of Inconel 718 are given in **Table 1** and **Table 2**.

The properties of the metals can be found in ref. [10] [11] and references therein.

2.2. Element Type Description

SOLID185 is for modelling of 3D solid structures. It is characterized by eight nodes that has three degrees of flexibility at every node; interpretations in nodes along x, y and z axes. The element has plasticity, stress stiffening, large deflection, and large strain capabilities. The element is defined by eight nodes and orthotropic material properties.

2.3. Numerical Models

The numerical models developed for various cut-out geometries are as shown in **Figures 1-5**.

Table 1. Composition of Inconel 718.

| Element | Content |
|---------|---------------|
| Ni + Co | 50% - 55% |
| Cr | 17% - 21% |
| Nb + Ta | 4.75% - 5.5% |
| Mo | 2.8% - 3.3% |
| Ti | 0.65% - 1.15% |
| Al | 0.2% - 0.8% |
| Fe | Balance |

Table 2. Mechanical properties of Inconel 718 alloy.

| Property | Metric |
|---------------------------|-----------------------------|
| Density | 8.19 g/cm ³ |
| Melting point | 1336°C |
| Co-efficient of expansion | 13.0 µm/m·°C (20°C - 100°C) |
| Modulus of rigidity | 77.2 kN/mm ² |
| Modulus of elasticity | 204.9 kN/mm ² |

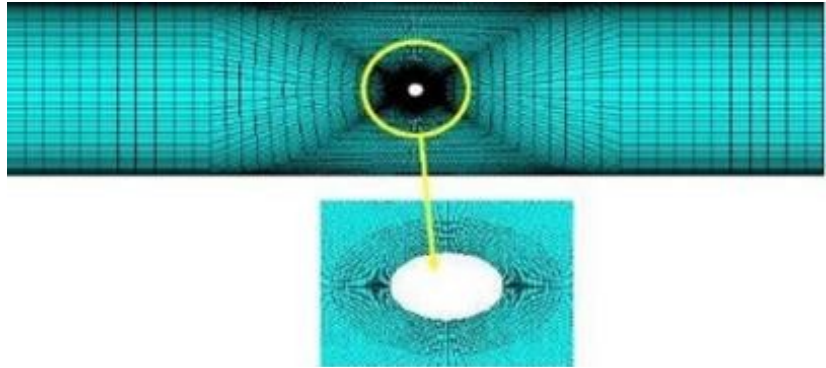


Figure 1. Hollow shaft with circular cut-out showing region of interest with fine mesh being magnified. Element type used: SOLID 185 Mesh type: Hex mesh, Number of nodes: 64174 Number of elements: 58860.

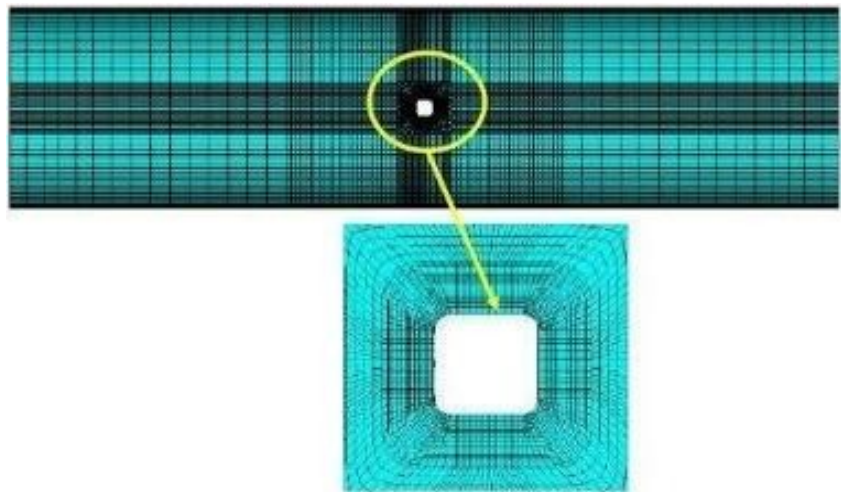


Figure 2. Hollow shaft with square cut-out (0°) showing region of interest with fine mesh being magnified. Element type used: SOLID 185 Mesh type: Hex mesh, Number of nodes: 197474 Number of elements: 174576.

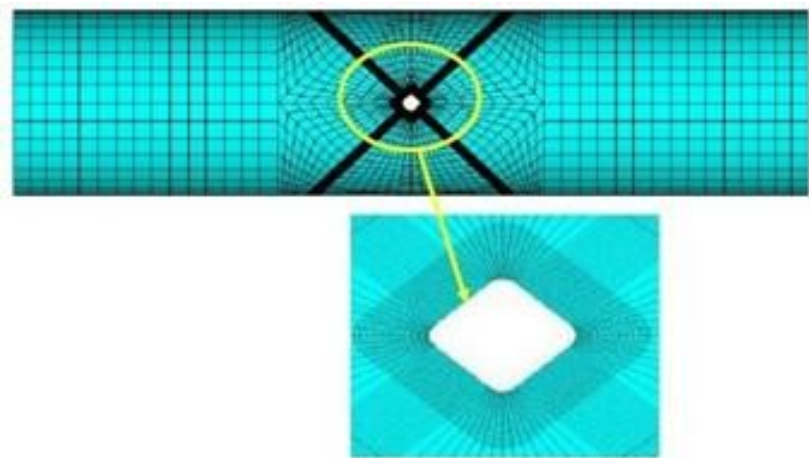


Figure 3. Hollow shaft with square cut-out (45°) showing region of interest with fine mesh being magnified. Element type used: SOLID 185 Mesh type: Hex mesh, Number of nodes: 150144 Number of elements: 135124.

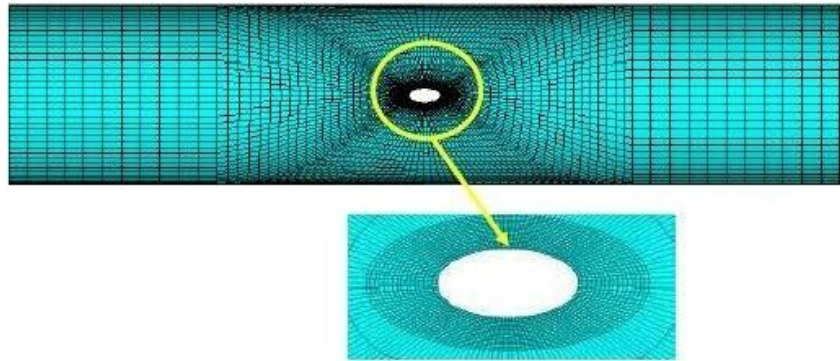


Figure 4. Hollow shaft with elliptical cut-out (0°) showing region of interest with fine mesh being magnified, Element type used: SOLID 185 Mesh type: Hex mesh, Number of nodes: 111880 Number of elements: 102960.

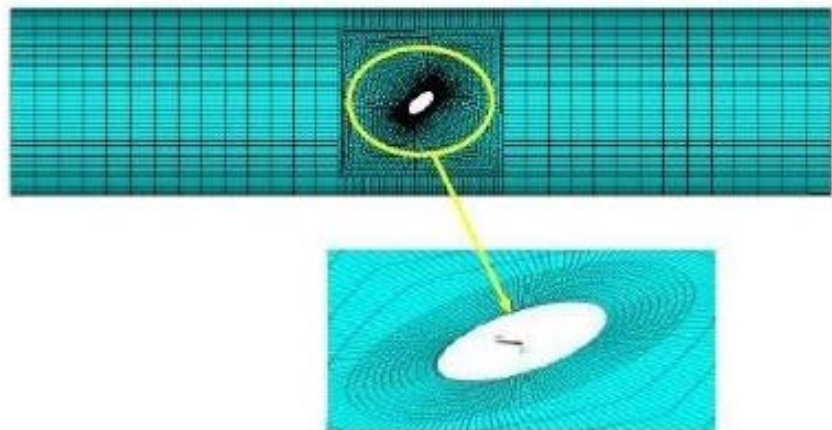


Figure 5. Hollow shaft with elliptical cut-out of (45°) showing region of interest with fine mesh being magnified. Element type used: SOLID 185 Mesh type: Hex mesh, Number of nodes: 113377 Number of elements: 99560.

2.4. Boundary Conditions

The hollow shaft was subjected to the boundary conditions as shown in the **Figure 6**. Rigid connections are provided at both the sides. Torque was applied on one end and the other end was fixed. Power of 12.5 MW and torque of 23.87324×10^6 N-mm is applied. The power and torque has been assumed suitably.

3. Results and Discussions

The behavior of different cutouts and its orientations upon application of torsional moment were studied. Crack initiation starts at geometric discontinuity and crack propagates when component is under plastic deformation. Cracks are initiated and propagated due to tensile stress, whereas any cracks or voids in the material are closed by compressive stress.

Von Mises stress is a combination of tensile and compressive stress. Compressive stress region and tensile stress region cannot be distinguished by it. Hence for better understanding principal stress plots are used.

From the **Figure 7**, when twisting moment is applied on a circular cutout,

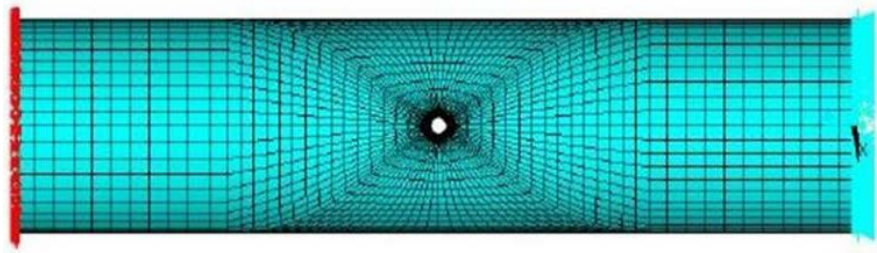


Figure 6. Hollow shaft fixed at one end subject to torsion at the other end.

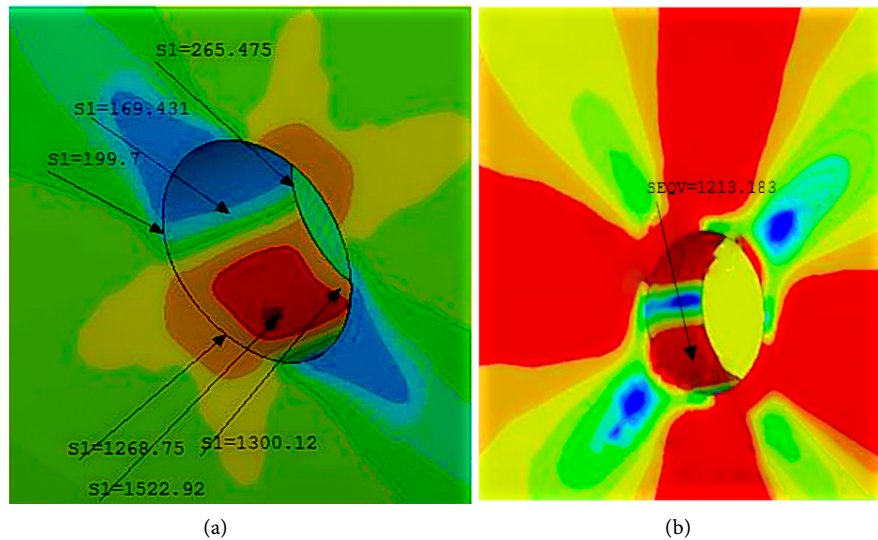


Figure 7. (a) Principal stress and (b) Von Mises stress plots around a circular cutout.

it deforms in an elliptical manner causing contraction and stretching of the circular hole. The red color region in the cutout plots indicate maximum stress, whereas blue colored region indicates compressive stress which can be seen by plotting minimum principal stress and Von Mises stress.

The maximum principal stress and Von Mises stress around the cutout region are observed to be 1523 MPa and 1212 MPa respectively. The principal strain and equivalent strain at the circular cut-out region. The maximum principal strain and equivalent strain around the cutout region are found to be 1.31% and 1.91% respectively.

Figure 8 represents the Principal stress and Von Mises stress plots at the square cut-out (0°) orientation region. The maximum principal stress and Von Mises stress around the cutout region are observed to be 1510 MPa and 1210 MPa respectively. The maximum principal strain and equivalent strain around the cutout region are found to be 1.8% and 2.91% respectively.

Figure 9 shows the principal stress and Von Mises stress plots at the square cut-out (45°) orientation region. The maximum principal stress and Von Mises stress around the cutout region are observed to be 1535 MPa and 1211 MPa respectively. The maximum principal strain and equivalent strain around the cutout region are found to be 0.89% and 0.93% respectively.

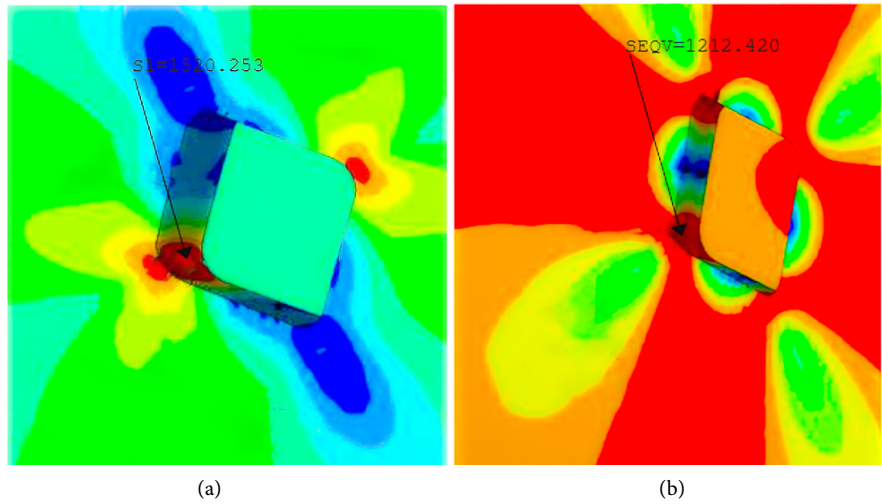


Figure 8. (a) Principal stress and (b) Von Mises stress around square (0°) cut-out.

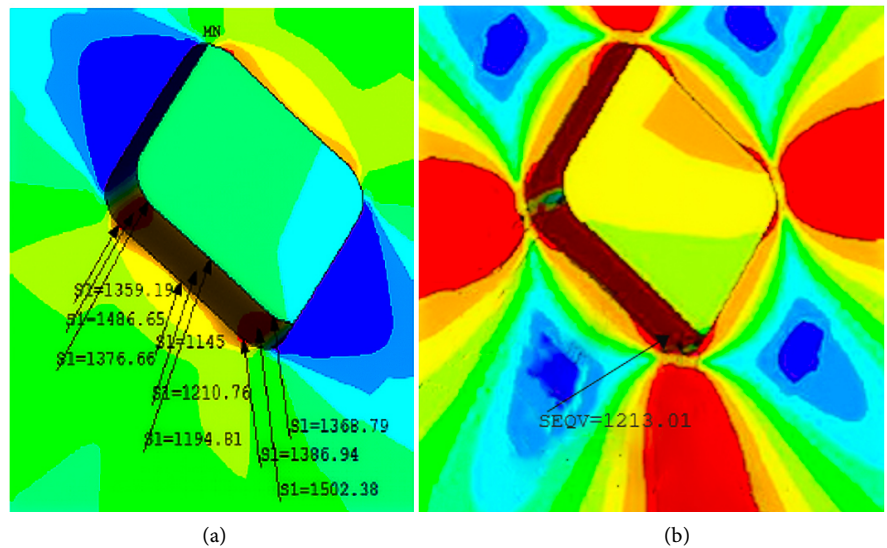


Figure 9. (a) Principal stress and (b) Von Mises stress around square (45°) cut-out.

Figure 10 shows the principal stress and Von Mises stress plots at the elliptical (0°) orientation cut-out region. The maximum principal stress and Von Mises stress around the cutout region are observed to be 1534 MPa and 1213 MPa respectively. The principal strain and equivalent strain at the elliptical cutout region. The maximum principal strain and equivalent strain around the cutout regions are found to be 1.78% and 1.8% respectively.

Figure 11 shows the principal stress and Von Mises stress plots at the elliptical cut-out (45°) region. The maximum principal stress and Von Mises stress around the cutout region are observed to be 1572 MPa and 1213 MPa respectively. The maximum principal strain and equivalent strain around the cutout region are found to be 3.14% and 3.23% respectively.

Table 3 shows the results of the analysis carried out in a hollow shaft with the introduction of cut-outs of different geometry and orientation subjected to

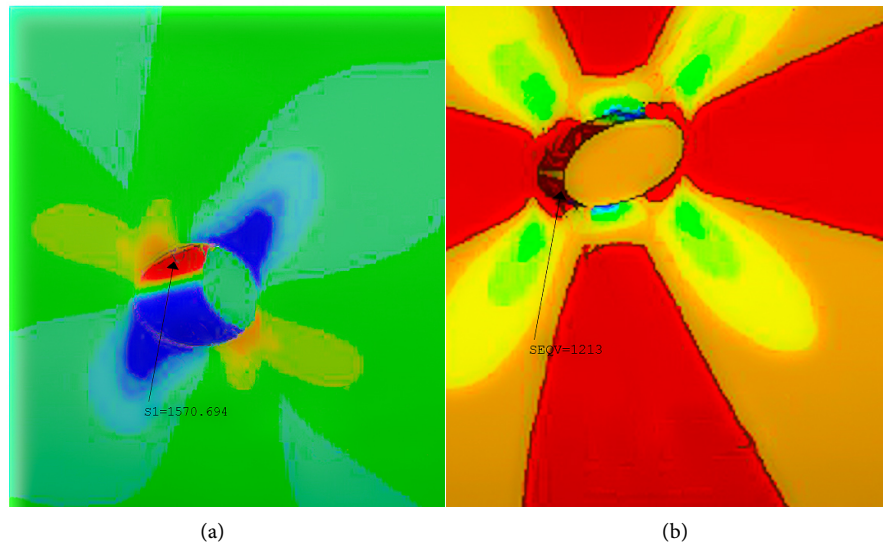


Figure 10. (a) Principal stress and (b) Von Mises stress plots around elliptical (0°) cutout.

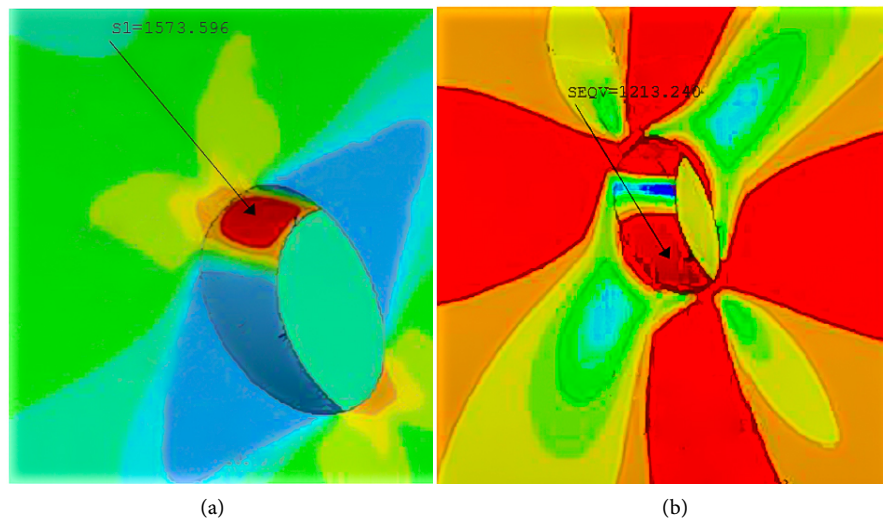


Figure 11. (a) Principal stress and (b) Von Mises stress plots around elliptical (45°) cutout.

specified boundary condition.

The plastic strain in square cut-out (45°) is observed to be the lowest when compared with cut-outs of other geometry and orientation. It is also observed from **Table 1** that values obtained for Von-Mises stress is the same. This is due to the fact that non-linear analysis on the material has been carried out. The stress and strain values varies proportionally up to elastic limit. Once the plastic limit is attained the stress remains constant and only the strain varies which is the characteristic feature of the non-linear analysis.

Also the square cut-out with 45° orientation contains sides parallel and perpendicular to principal stress directions which in turn minimizes the stress concentration and reduces the plastic strain. The principal stress for square cut-out (45°) orientation is around 1502 MPa while it is maximum for elliptical

Table 3. Shows the stress and strain values for different cut-outs.

| Analytical Model | 1 st Principal Stress MPa | Von Mises Stress MPa | 1 st Principal Plastic Strain | Equivalent Strain |
|------------------|--------------------------------------|----------------------|--|-------------------|
| Circular | 1527.512 | 1213.183 | 0.01974 | 0.02012 |
| Square (0°) | 1520.253 | 1212.420 | 0.03293 | 0.03410 |
| Square (45°) | 1502.410 | 1213.031 | 0.01536 | 0.01774 |
| Elliptical (0°) | 1570.694 | 1213.093 | 0.01873 | 0.01907 |
| Elliptical (45°) | 1573.596 | 1213.240 | 0.03286 | 0.03358 |

cut-out (45°). Thus, it is seen that a square cut-out (45°) orientation can be implemented in the design in order to enhance the service life of the components.

4. Conclusions

In present study the effect of cut-outs with different geometry and orientation was studied using ANSYS 14 software. Five different cut-out geometries and orientations were introduced on hollow Inconel 718 shaft—circular (0°), square (0°), square (45°), elliptical (0°) and elliptical (45°). The shaft was subjected to a Power of 12.5 MW and torque of 23.87324 X 106 N-mm with one end fixed. The models were analyzed for principal stress, Von Mises stress along with plastic strain. The following features were observed in the analyzed models:

- The square cut-out with 45° orientation shows the least plastic strain of 0.01536. The least value of plastic strain is due to the fact that square cut-out with 45° orientation contains sides parallel and perpendicular to principal stress directions which in turn minimizes the stress concentration and reduces the plastic strain.
- The Von-Mises stress remains almost same for all cut-out geometries because non-linear analysis is being carried out. The stress is proportional to strain within elastic limit. In plastic region the stress remains constant and strain varies.
- Square cut-outs with 45° orientation may be implemented in design to improve the service life of the components.
- Further, experimental investigation of simulated models may be carried out which opens arena for further research.

Competing Interests

The authors declare that there is no conflict of interests. The work being carried out is purely for academic purpose and there are no financial gains to the authors by any means.

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