

Application of random walk model to fit temperature in 46 gamma world cities from 1901 to 1998

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Received 2 October 2010; revised 3 November 2010; accepted 6 November 2010.

ABSTRACT

Very recently, we have applied the random walk model to fit the global temperature anomaly, CRUTEM3. With encouraging results, we apply the random walk model to fit the temperature walk that is the conversion of recorded temperature and real recorded temperature in 46 gamma world cities from 1901 to 1998 in this study. The results show that the random walk model can fit both temperature walk and real recorded temperature although the fitted results from other climate models are unavailable for comparison in these 46 cities. Therefore, the random walk model can fit not only the global temperature anomaly, but also the real recorded temperatures in various cities around the world.

Keywords: Gamma World Cities; Global Warming; Modeling; Random Walk; Temperature Change

1. INTRODUCTION

During our recent studies on the potential influence of global warming on the evolution of proteins from influenza A virus [1-5], we noticed that the temperature fluctuates around the temperature trend. On the one hand, these fluctuations can be easily attributed to random effects; on the other hand, these fluctuations might imply that we might need a random model to describe the temperature pattern because the output of any deterministic model is generally a smooth curve.

Without smooth temperature trend, the temperature behaves irregularly either to increase or to decrease for some period of time, from where we could not find out a clear pattern in temperature change along the time course. The irregular ups and downs appear similar to the random walk, which firstly came into our mind. The random walk comes from the observation of tossing a

single coin: although theoretically each side of coin has 0.5 chances to be up or down, the tossing of coin sequentially results in either head up or tail up for several times continuously rather than each tossing generates alternative result. The addition of sequentially tossed results would be a random walk [6]. Computationally each tossing of coin can be done with the generation of random numbers, which can be classified as 1 or -1 if a random number is larger or smaller than its previous one. As the generation of random numbers is through the Monte-Carlo simulation with different seeds, thus the random walk is a model with its own model parameter, seed.

Therefore, we can consider the random walk model as alternative model to fit the temperature because it can produce a really fluctuated curve. Following that, we applied the random walk model to fit the global temperature anomaly, CRUTEM3, and got a very encouraging result [7]. Since then, an intensive literature search indicates that Gordon noticed the similarity between global warming and random walk in 1991 [8].

Likely, the random walk could provide an alternative model to describe the temperature, however, two questions raised here are whether the random walk model can be applied only to the global temperature anomaly not to local temperature and whether the random walk model can be applied only to the anomaly not to really recorded temperature.

In order to answer these questions, we need to use the random walk model to fit the real recorded temperature in different places around the world. In this study, we apply the random walk model to fit the temperature in 46 gamma world cities from 1901 to 1998.

2. MATERIALS AND METHODS

2.1. Data

Forty-six gamma world cities are chosen according to

Wikipedia [9]. However, the number of these cities and their order are changed frequently due to the characteristics of Wikipedia, thus the cities were dated in February, 2010.

The temperatures recorded in these 46 cities from 1901 to 1998 based on 0.5° by 0.5° latitude and longitude grid-box basis cross globe are obtained from the website of Oak Ridge National Laboratory [10].

The latitudes and longitudes of these 46 gamma world cities are determined using Get Lat Lon [11].

2.2. Temperature Walk

At first, we use the simplest random walk model, which starts at zero and at each step moves by ± 1 with equal probability [6]. In other words, the simplest random walk can be considered as a sequential result of tossing a fair coin, by which we record the head as 1 and the tail as -1 , and then we add the results along the time course.

For this purpose, we need to convert the temperature into the temperature walk as shown in **Table 1**. When the temperature at certain year is higher than its previous one, we classify it as 1, otherwise we classify it as -1 , and then we add them as the random walk does.

2.3. Generation of Random Walk

We use the SigmaPlot [12] to generate random sequence for the random walk. Technically, the generation of random walk is quite simple: we generate random number either ranged from -1 to 1 or without limit, and then we classify a generated random number as 1 if it is larger than its previous one and as -1 if it is smaller than its previous one. Thereafter we add these values as a random walk.

2.4. Searching for Seed

To find a random walk that is very approximate to the temperature walk is to find a seed that can generate such a random walk. To the best of our knowledge, there is no algorithm for searching seeds by converging the difference between observed curve and the curve produced by random walk. Therefore the so-called fitting, which traditionally searches the optimum according to various algorithms, becomes to search all possible seeds in order to find out the seed that produces the random walk with the least squares between random walk and temperature walk.

2.5. Fitting Recorded Temperature

Thereafter, we use a more complicated random walk model [13] to fit the recorded temperature, which is in

decimal format. In plain words, the simplest random walk comes from tossing of double-sided coin, while this random walk can be regarded as tossing of dice, which cannot be only six-sided but as many as the decimal data. In such a way, we generate random numbers, and add them to construct the random temperature, and the fitting is again to search the best seed that generates the best fit.

2.6. Comparison

We use the least squares between temperature walk and random walk, and between recorded temperature and random temperature to evaluate which seed is the best.

3. RESULTS AND DISCUSSION

Table 1 shows how we construct a temperature walk in Panama City. Its recorded temperature in 1901 was 18.8250 (cell 2, column 2), which corresponds to the starting point of temperature walk, 0, (cell 2, column 4). The temperature in 1902 was 19.8250 (cell 3, column 2), which was higher than the temperature in 1901, 18.8250, thus the temperature step was 1 (cell 3, column 3), and the temperature walk is 1 ($0 + 1$) (cell 3, column 4). In this manner, we construct the temperature walk from 1901 to 1998.

Similarly, **Table 1** also shows how we construct a random walk with generated random numbers. A good seed that we found is 0.48531. The first random number generated by this seed was 0.2629 (cell 2, column 5), which corresponds to the starting point of random walk, 0, (cell 2, column 7). The second random number generated was 0.8817 (cell 3, column 5), which is larger than the first random number, 0.2629 (cell 2, column 5). Thus the random step was 1 (cell 3, column 6), and the random walk is 1 ($0 + 1$) (cell 3, column 7).

The last column (column 8) in **Table 1** is the difference between temperature walk and random walk (random walk-temperature walk), whose squared sum is our standard to find the best fit among seeds.

Figure 1 shows the fitted results in 12 cities represented differently geographic locations around the world. As can be seen, the random walk (gray curve) mimicked the temperature walk (black curve) with very small difference. Theoretically, a completely perfect fit would have an extremely small probability. In the simplest case of random walk, this probability would be $(1/2)^{98}$. Meanwhile, the total number of our fittings were one million, which is a fraction of $(1/2)^{98}$. Thus the fact that we can find a relatively good fit within one million fittings suggests that the random walk can describe the temperature pattern from 1901 to 1998 in these cities.

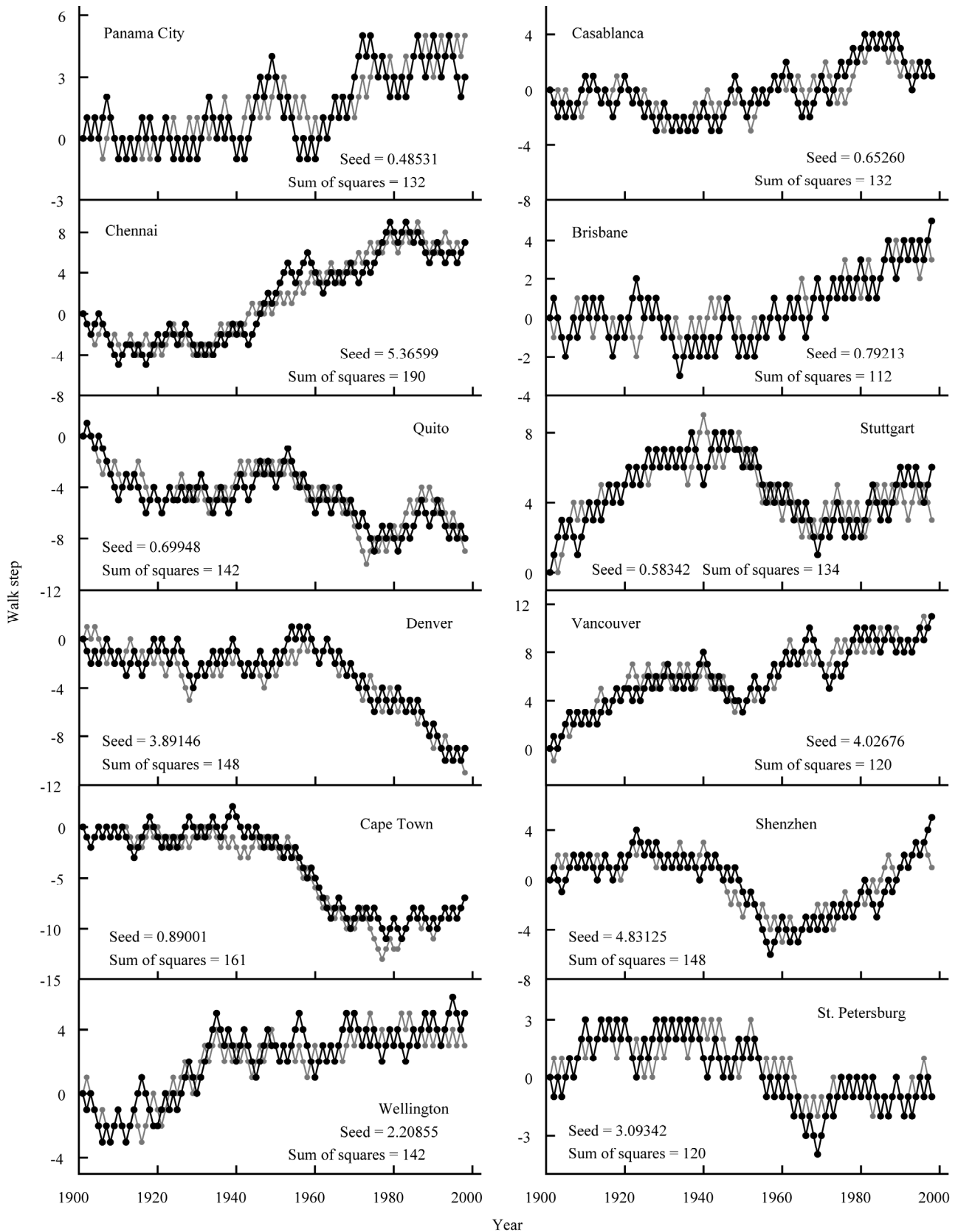


Figure 1. Comparison of temperature walk (black) with random walk (gray) in 12 cities from 1901 to 1998.

Table 1. Conversion of recorded temperature in centigrade degree into temperature walk and generation of random walk for temperature in Panama City from 1901 to 1998 (The random number is generated by SigmaPlot with the seed of 0.48531).

Year	Recorded Temperature	Temperature Step	Temperature Walk	Random Number	Random Step	Random Walk	Difference
1901	18.8250		0	0.2629		0	0
1902	19.8250	1	1	0.8817	1	1	0
1903	19.2250	-1	0	0.2996	-1	0	0
1904	19.8000	1	1	0.9392	1	1	0
1905	19.7750	-1	0	-0.1281	-1	0	0
...
1991	20.7083	-1	4	0.4440	1	4	0
1992	20.0333	-1	3	0.5661	1	5	2
1993	20.0750	1	4	-0.8129	-1	4	0
1994	20.4750	1	5	0.0808	1	5	0
1995	20.2250	-1	4	-0.8109	-1	4	0
1996	19.6917	-1	3	-0.1161	1	5	2
1997	19.6750	-1	2	-0.9795	-1	4	2
1998	20.7333	1	3	-0.3824	1	5	2

On the other hand, the temperature walk in fact answers the simplest and very basic question of whether the temperature in this year is higher (1) or lower (-1) than that in the previous year, which could arguably be the first human concept in comparison of temperature between two time points. The answer to this simplest question for years would construct the temperature walk. Therefore, we consider that the temperature walk has a very sound basis.

In fact, not only the selected cities in **Figure 1** show a good fit, but also the rest of cities were found no exception (**Table 2**), here the exception can be understood as the fitted curve has a totally opposite direction with respect to its temperature curve. We therefore consider that the random walk model can fit not only the global temperature anomaly, but also the temperatures in different locations around the world.

Figure 2 shows the fittings for the recorded temperature. The difference between **Figures 1** and **2** is that the recorded temperature was in decimal format while the temperature walk was in ± 1 format. As seen in **Figure 2**, the random walk model can fit these recorded temperatures even the temperatures in these locations have different patterns. Again, there is no exception for the fittings in all 46 gamma world cities (columns 3 and 5, **Table 2**), which furthermore demonstrate that the random walk model can fit not only the global temperature anomaly, but also the temperatures in different locations around the world.

In this study, we used the sum of least squares to com-

pare which seed produces a better fitting. Thus, a question raised here is how small the sum of least squares is that we can say the random walk model fits the temperature well. We could consider this question in three ways: 1) We have already mentioned that the probability to find the best fit for the temperature walk is $(1/2)^{98}$, and this chance cannot be found in limited time, however, some better fits can be found among our total one million fits; 2) On the other hand, the sum of least squares can be mainly used for model comparison, *i.e.* to use our sum of least squares to compare with the sum of least squares obtained from other models in fitting the temperature of this group of cities although no other results are available for comparison; 3) from modeling viewpoint, the random walk model has an advantage over other models because the random walk model has only one model parameter, whereas other models have numerous model parameters, thus theoretically the random walk model has a larger chance than other models to find out the best fit because each model parameter has a certain space to search the optimal parameter.

The random walk actually has a very deeply physical mechanism: weather is a highly multidimensional attractor of Navier-Stokes Equations of atmosphere with highly complicated boundary conditions. Worse, it is a non-autonomous system with at least two-periodic forcing, diurnal and annual. And annual measurement is a result of averaging of diurnal Poincare Maps. Given what we know about weather, this entire attractor is highly chaotic, its annual maps are likely of very fractal

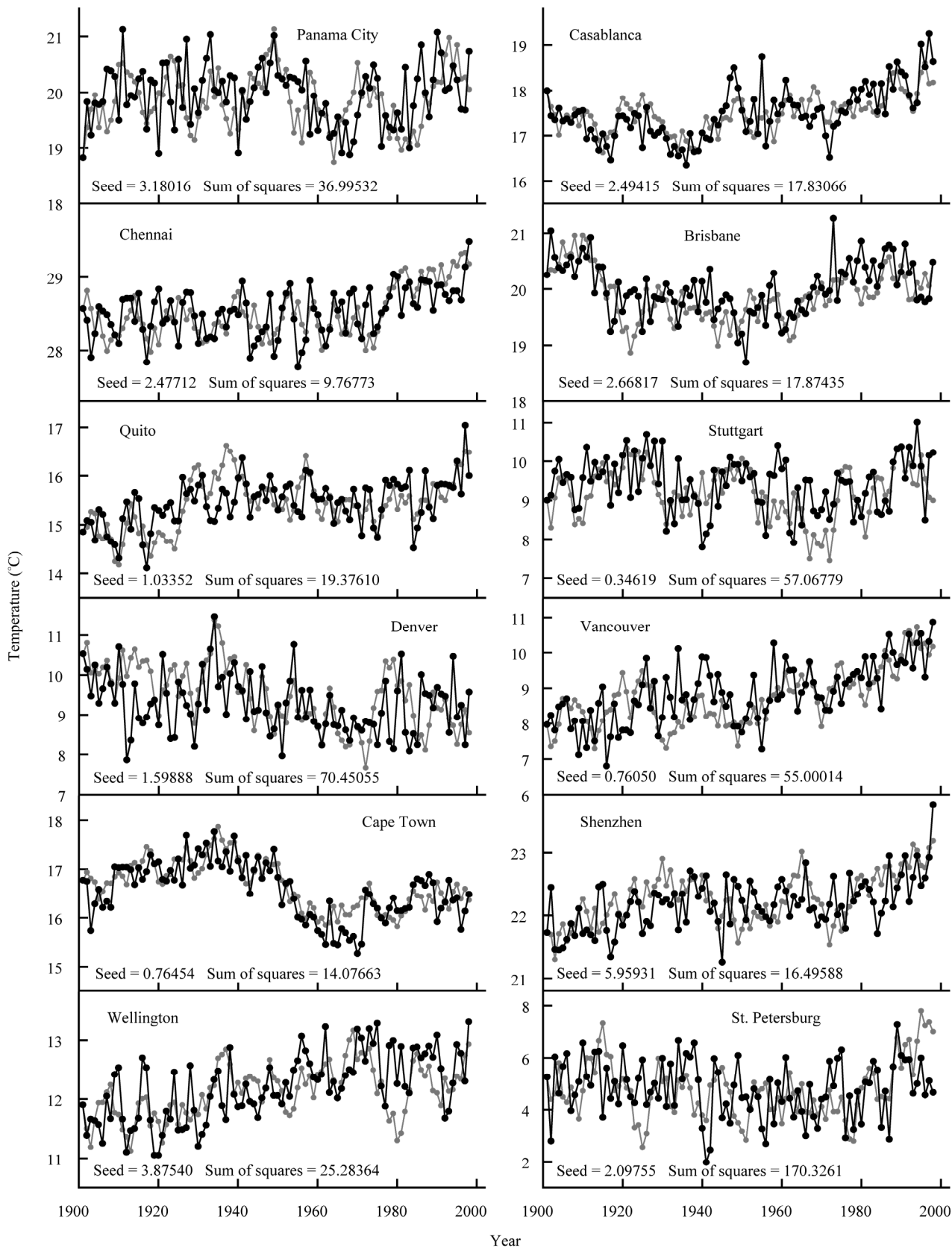


Figure 2. Comparison of recorded temperature (black) with random temperature (grey) in 12 cities from 1901 to 1998.

Table 2. Model parameters (seeds) and fitted results for fitting temperature change in 46 gamma world cities from 1901 to 1998 using random walk model.

City	Fitting of Temperature Walk		Fitting of Recorded Temperature	
	Seed	Sum of Squares	Seed	Sum of Squares
Panama City	0.48531	132	3.18016	36.99532
Casablanca	0.65260	132	2.49415	17.83066
Chennai	5.36599	190	2.47712	9.76773
Brisbane	0.79213	112	2.66817	17.87435
Quito	0.69948	142	1.03352	19.37610
Stuttgart	0.58342	134	0.34619	57.06779
Denver	3.89146	148	1.59888	70.45055
Vancouver	4.02676	120	0.76050	55.00014
Zagreb	1.90779	116	8.66967	51.31698
Guatemala City	0.24543	152	1.83630	16.95153
Cape Town	0.89001	161	0.76454	14.07663
San Jose	1.02726	97	0.14315	27.59630
Ljubljana	1.9037	148	3.84243	42.53592
Minneapolis	0.35895	152	0.36478	109.71508
Santo Domingo	4.29052	132	1.74614	12.86316
Seattle	1.42289	116	0.25169	39.26277
Manama	2.02165	124	0.68838	27.38144
Shenzhen	4.83125	148	5.95931	16.49588
Guadalajara	2.04735	146	0.36390	23.99288
Antwerp	6.65174	140	2.48303	46.55537
Kolkata	9.56581	134	5.27468	11.90250
Rotterdam	0.11644	132	2.48303	44.69400
Lagos	1.77962	144	1.69805	23.25883
Philadelphia	1.16765	120	3.33953	53.14891
Perth	0.03095	131	0.75289	26.84818
Amman	1.41563	136	0.58696	30.47234
Manchester	2.64776	113	2.66954	32.74658
Riga	3.64228	112	2.83735	144.92674
Detroit	0.00136	124	0.01219	85.23191
Guayaquil	0.72301	139	3.97256	25.55697
Wellington	2.20855	142	3.87540	25.28364
Portland	0.28335	132	0.07853	49.35406
Porto	1.92792	133	0.38211	20.36737
Edinburgh	0.77095	104	0.97533	28.76731
Tallinn	0.16784	132	2.83735	147.22377
San Salvador	1.06139	184	3.05414	16.39708
St. Petersburg	3.09342	120	2.09755	170.32610
Port Louis	0.08480	136	3.02959	6.53177
San Diego	2.18277	250	0.12773	44.65777
Calgary	1.37753	100	1.11564	139.44530
Almaty	2.39794	164	9.93285	93.91648
Birmingham	0.45373	142	0.95604	53.31933
Islamabad	5.62339	110	0.91978	33.98368
Doha	0.64310	135	0.70169	27.9417
Vilnius	0.33912	116	0.53868	130.0170
Colombo	7.06029	184	2.74576	5.83075

nature, and invariant measure of these maps are likely a fractal-dimensional sieves with a hyperbolic point at every location. The annual iteration of this map is like a coin tossing [14].

Still, the random walk could be viewed as the Drunkard's walk [15] as the climate change seems to be a complex process, and the drunkard walk is also used to describe complex processes. It should be obvious that climate change is a complex process, for the climate change involves many factors that are not reducible to exactly one thing. And the climate affects the ecosystem that is a complex process itself.

On the other hand, the random mechanism in random walk model is different from other random factors in modeling, where the random factors were mainly considered as a minor factor [16].

At this moment, we have no way to know whether or not the random walk model works better than other climate models, simply because the results of temperature fitting in these cities using other climate models are not available for comparison.

In conclusion: we use the random walk model to fit the temperature change in 46 gamma world cities from 1901 to 1998, and the results show that the random walk model can fit both the temperature walk and recorded temperature in different cities worldwide. This study confirms that the random walk model can be used to analyze the temperature change, which suggests that the random mechanism could be a factor driving the temperature change in these cities. The use of random walk to fit the temperature change is still at very early stage nevertheless more studies are needed in order to better understand the temperature change and its modeling.

4. ACKNOWLEDGEMENTS

This study was partly supported by Guangxi Science Foundation (07-109-001A, 08-115-011, 09322001 and 2010GXNSFA013046). The authors wish to thank Dr Hong Zhang at Biyee SciTech Inc., MA, USA for helpful discussion. The authors also wish to thank Dr Alexei A. Predtechenski at Standard Microsystems Corporation, Austin, TX, USA for his discussion and support in internet discussion group.

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