

# On the Atomic Kinetic Energies in Ceramic Oxides

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## Abstract

We calculated the mean atomic kinetic energy,  $\langle Ke(X) \rangle$ , of the X atom ( $X = \text{Si}, \text{Ti}, \text{Hf}, \text{O}$ ) in some ceramic oxides,  $\text{SiO}_2$ ,  $\text{TiO}_2$  and  $\text{HfO}_2$  using the published partial vibrational density of states (PVDOS). These were simulated by means of lattice dynamics, molecular dynamics and density functional theory. The predicted values are compared to those recently obtained by electron Compton scattering (ECS), with an overall good agreement of ~4%. In accord with calculations, the ECS measurements reveal a small, but detectable, dependence of  $\langle Ke(X) \rangle$  on the fine structural details of the oxide, e.g. whether it is in a crystalline or amorphous form, and whether it exhibits surface or bulk characteristics. This study illustrates the limitations and the potential of PVDOS simulations in predicting experimental atomic kinetic energies, and can be viewed as a promising approach for elucidating valuable structural and dynamical information of ceramic oxides and other materials.

## Keywords

Ceramic Oxides, Atomic Kinetic Energy, Vibrational Density of States, Electron Compton Scattering

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## 1. Introduction

Ceramic oxides such as  $\text{SiO}_2$ ,  $\text{TiO}_2$  and  $\text{HfO}_2$  are fundamental dielectrics amongst a large family of atomic layer deposition (ALD) materials commonly used in semiconductors and micro-/nano-electronics technologies. The complexity of these technologies demands in some cases, cross-disciplinary research studies. In the materials front, understanding the origin of their unique fundamental properties at atomic and molecular levels is important for the realization

of the full potential of the fruition of eventual technological applications. Of key importance are the dynamical properties of ceramic oxides which may be studied via their vibrational spectra using IR, Raman and inelastic neutron scattering (INS) that provide fingerprints for clarifying their structure. In that respect, the vibrational density of states (VDOS), and in particular the partial VDOS (PVDOS) of specific atoms, are important to explore. An illustrative example is  $\text{HfO}_2$  which is utilized in resistive switching memories in thin film devices, exhibiting reversible metal-insulator transitions [1]. This switching phenomenon is not yet fully understood and is speculated to be governed by percolation of oxygen vacancies [2]. Understanding the hopping mechanism of the O-atoms between surface oxygen vacancies in  $\text{HfO}_2$  involves the study of hafnia PVDOS [3]. Another exemplifying case is that of amorphous silica ( $\alpha\text{-SiO}_2$ ) which is widely used in semiconductor devices and optical fibers. Due to its disordered nature, the molecular motions taking place in  $\alpha\text{-SiO}_2$ , where surface librations are a key factor [4], have not yet been completely elucidated due to current experimental limitations. Nonetheless, some valuable structural information may be achieved through computational simulations of its vibrational spectra. Recently, calculations comprising VDOS and PVDOS, were used to study average atomic kinetic energies,  $\langle\text{KE}\rangle$ , in some benchmark systems involving hydrogen bonds (HBs), e.g. in ice Ih and liquid water [5], highly compressed ice VII [6], ferroelectric crystals of the KDP-type [7], the  $\text{Rb}_3\text{H}(\text{SO}_4)_2$  superprotonic conductor [7] and water nano-confined in Beryl [8]. Very recently, the same idea was also applied for studying the anisotropy of  $\text{Ke}(\text{H})$  in the ferro- and para-electric phases of CDP ( $\text{CsH}_2\text{PO}_4$ ) [9]. A recent comprehensive review may be found in Ref. [10]. In fact, studies utilizing KE calculations go way back to the 90th utilizing nuclear resonance photon scattering NRPS [11] of  $^{15}\text{N}$  [12] and  $^{13}\text{C}$  [13]. Interestingly it was applied to study molecular orientations of gases adsorbed on Grafoil® and Papyex® [14] in various systems [15] [16] as well as in graphite intercalation compounds [17].

The calculations of  $\langle\text{KE}\rangle$  in these early studies relied on discrete characteristic frequencies of the system as measured using IR, Raman and inelastic n-scattering (INS). Only recently, with the advent of computational capabilities, a new approach was adopted, relying on the continuum of vibrational states (phonons) of the studied atom. The continuum, represented by the pVDOS of the atom is simulated by using DFT, molecular (MD) and lattice (LD) dynamics. Altogether, the validity of the above approach is strongly justified by the very good agreement obtained with photon-, neutron- and electron scattering techniques in many systems. In fact, ECS has been shown to be a powerful tool for testing KE calculations [18] [19] [20] [21] [22] including cases such as  $\text{TiO}_2$  [21] and  $\text{SiO}_2$  [34] ceramics. It was thus interesting to see to what extent this approach could be utilized, to distinguish between different ceramic forms of  $\text{TiO}_2$  and  $\text{SiO}_2$ .

The ECS uses electrons with incident energies in the range 2 to 40 keV, and its capabilities were recently illustrated for low Z-elements using samples such as

H<sub>2</sub>O [23], NH<sub>3</sub> and CH<sub>4</sub> [24]. The measured <KE> values in these molecular systems closely agreed with those predicted using a semi-empirical (SE) method. This later method assumes the harmonic approximation (HA) and a decoupling between the various modes contributing to <KE>, the input data are taken from experiment [10]. Note that the SE approach utilizing simulated PVDOS was found to correctly reproduce Ke(H) values even in strongly anharmonic systems such as in KDP type crystals [7], Rb<sub>3</sub>H(SO<sub>4</sub>)<sub>2</sub> [7] and H<sub>2</sub>O@Beryl [8], indicating that anharmonicity has probably only small effect on the atomic kinetic energy [10].

In the present study we utilize the SE approach to deduce Ke(X) values of the atomic constituents in SiO<sub>2</sub>, TiO<sub>2</sub>, HfO<sub>2</sub>, by using their literature simulated PVDOS, and show that they are in good agreement with recent ECS measurements. An attempt is made to assign the measured values to specific structural characteristics of the studied oxides.

## 2. Experimental Details

Full experimental details of the ECS technique may be found elsewhere. [18] [19] [20] [21] [22] Here we just mention that the ECS measurements involved the use of electron beams with energies ( $E_e = 1$  to 40 keV) having low thermal spread and high resolution electron spectrometers. The mean kinetic energy of the scattering atom Ke(X) causes a Doppler broadening  $\Delta e$  of the scattered electrons; the two are related by  $\Delta e = \sqrt{\frac{4}{3} Ke(X) Er(X)}$ , with  $Er(X)$  the recoil energy of the X atom caused by the scattered electron. In the following we explain how the atomic kinetic energies were calculated.

## 3. Mean Atomic Kinetic Energy Calculations

In a molecular solid the distribution of the vibrational states (phonons) is described by the VDOS in which each atom takes a fraction. Theoretically, the participation of each atom in the total VDOS is best described by projecting the simulated total VDOS on that atom, *i.e.* by the partial VDOS (PVDOS) hereby denoted by  $g_x(\nu)$ . The kinetic energy Ke(X) of the X atom in a molecular solid is contributed by the external (translational and rotational (libration) modes) and internal molecular vibrations of the building block molecule and may be expressed as: [25]

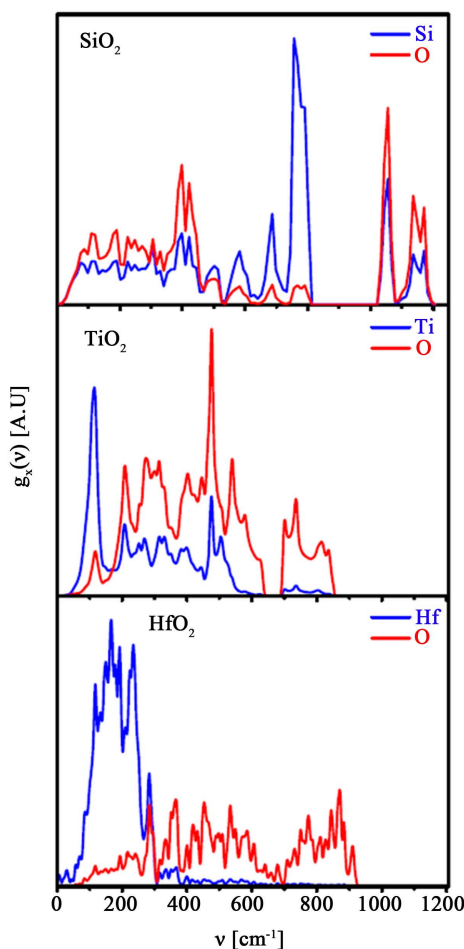
$$Ke(X) = \frac{3}{2} \int_{\nu_0}^{\nu_f} g_x(\nu) \alpha(\nu) d\nu / \int_{\nu_0}^{\nu_f} g_x(\nu) d\nu \quad (1)$$

With  $\alpha(\nu, T) = \frac{h\nu}{2} \left[ \left( e^{h\nu/kT} - 1 \right)^{-1} + \frac{1}{2} \right]$  the kinetic energy of a quantum harmonic oscillator of frequency  $\nu$  with  $\nu_0$  and  $\nu_f$  the boundaries of  $g_x(\nu)$ , T the thermodynamic temperature and k the Boltzmann constant.

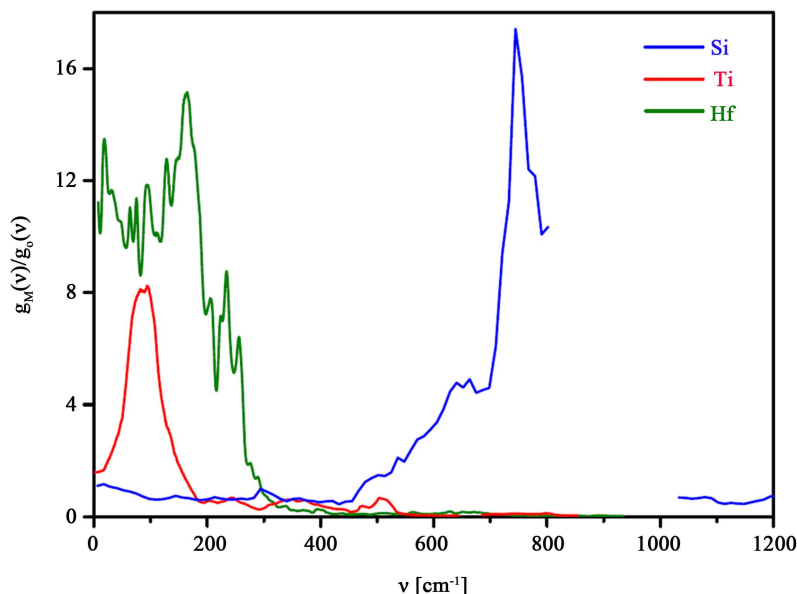
## 4. Results and Discussion

In the literature, various calculations of the total VDOS of XO<sub>2</sub> type oxide were

made. Only in few, the PVDOS of its atomic constituents is simulated, from which  $Ke(X)$  and  $Ke(O)$  were deduced. **Figure 1** depicts representative PVDOS simulated for the present studies. Note that in silica some modes occur in the  $1000 - 1200 \text{ cm}^{-1}$  region while those of titania and hafnia the modes terminate at about  $900 \text{ cm}^{-1}$ . Another feature common to all PVDOS is that the O-atom, being the lighter partner, systematically shares the major part of the high frequency phonon states. Along other phonon states the situation is less regular: In silica, the Si atom shares the major part of the mid phonon states and vice versa at lower energies. This situation is illustrated in **Figure 2** which shows the ratios between the PVDOS of the heavier element and of oxygen in all three oxides. It may be noted that the heavier the element, the larger part it shares in the low phonon states while on going to higher phonon states the situation reverses. Here too, the silica behaves differently, where along the low frequency phonons, up to  $\sim 400 \text{ cm}^{-1}$ , the Si and O atoms share nearly equal fractions of the kinetic energy. On crossing  $\sim 400 \text{ cm}^{-1}$  the kinetic energy fraction of Si steeply increases. This indicates that in the vibrations of  $\text{SiO}_2$ , the Si atom moves against the two oxygens ( $\text{O}_2$ ) which has a higher mass, a situation which differs from that of the other oxides.



**Figure 1.** Simulated PVDOS of X (Si, Ti, Hf) and O atoms in  $\alpha$ -silica, [28] titania [29] (rutile) and hafnia [3].



**Figure 2.** Ratio between the simulated VDOS of the X element ( $X = \text{Si}, \text{Ti}, \text{Hf}$ ) and of the oxygen atom in  $\alpha$ -silica [28] (blue), titania (rutile) [29] (red) and hafnia [3] (green). The discontinuity between 800 and 1020  $\text{cm}^{-1}$  in silica is due to the fact that no modes occur along this energy band (see Figure 1).

The simulated PVDOS of the various phases of  $\text{XO}_2$  ( $X = \text{Si}, \text{Ti}, \text{Ge}, \text{Hf}$ ) were utilized for deducing  $\text{Ke}(X)$  and  $\text{Ke}(\text{O})$  at room temperature using Equation (1). **Table 1** summarizes the calculated values together with available ECS and NRPS experimental results. Note that all simulation techniques yield fairly close KE values for the X-atoms.

The NRPS and ECS results of **Table 1** lack the  $\text{Ke}(\text{Ti})$  and  $\text{Ke}(\text{Hf})$  values respectively. This is because the NRPS method is unique in the sense that it is a random nuclear resonance process and hence can only measure the KE of a single isotope of Ti (which happens to be  $^{48}\text{Ti}$ ) in  $\text{TiO}_2$ . In ECS on the other hand, electrons are scattered from all atomic constituents of the target. Hence, a reliable extraction of the mean kinetic energy of the Hf atoms becomes problematic due to lack of knowledge of the exact shape of the Hf elastic peak [35].

It is interesting to examine in **Table 1** the values calculated by the same methodology, *i.e.* the DFT results of  $\text{SiO}_2$  and  $\text{TiO}_2$ . These are shown to be very close to each other, indicating their reproducibility, despite the differences in the specific potentials and models used. An increase in these differences should however be expected at much lower temperatures, as the effect of the zero-point motion increases.

Altogether, **Table 1** shows that the ECS results agree to less than 5%, with predicted values. Note that  $\text{Ke}(X)$  and  $\text{Ke}(\text{O})$  in molecular solids usually acquire intuitively expected values, *i.e.*  $\text{Ke}$  of the light partner is larger than the heavier one, as in ice where  $\text{Ke}(\text{H}) \sim 152 \text{ meV}$  and  $\text{Ke}(\text{O}) \sim 51 \text{ meV}$  [5] [36]. Note also that in the  $\text{HfO}_2$  result the isotopic composition of the oxygen in the sample was  $^{16}\text{O}:^{18}\text{O} = 1:3$  (a 20 nm  $\text{Hf}^{16}\text{O}_2$  surface layer grown on a 60 nm  $\text{Hf}^{18}\text{O}_2$  layer).

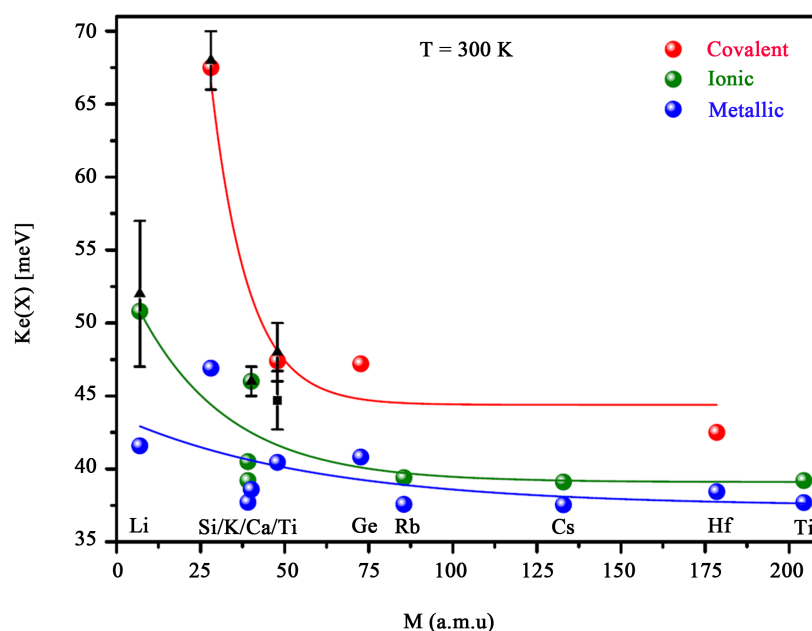
**Table 1.** Measured and calculated mean atomic kinetic energies  $\langle Ke(X) \rangle$  of the X and O atoms in  $XO_2$  ( $X = Ti, Si, Hf$ ) at 300 K. The  $TiO_2$  polymorphs include 4 high pressure phases (denoted by\*). Explicit calculation techniques and phases are indicated. Note that the  $Ke(X)$  value for any atom at  $T = 300$  K of an ideal gas is  $3kT/2 = 38.6$  meV and that the excess kinetic energy is contributed by the zero-point motion which shows up in all oxides at  $T$  as high as 300 K.

| X          | Technique | Phase  | $\langle Ke(X) \rangle$ [meV] |               |      |
|------------|-----------|--|-------------------------------|---------------|------|
|            |           |  | X                             | O             | Ref. |
| $^{28}Si$  | MD        | Amorphous Silica                                     | 68.8                          | 71.9          | [4]  |
|            | DFT       | Vitreous (fused) Silica ( $v-SiO_2$ )                | 67.3                          | 64.0          | [26] |
|            | LD        | $\alpha$ -Cristobalite                               | 68.7                          | 66.3          | [27] |
|            | DFT       | $\alpha$ -Quartz                                     | 65.2                          | 62.2          | [28] |
|            |           | <b>Average</b>                                       | <b>67.5</b>                   | <b>66.1</b>   |      |
|            | ECS       | Amorphous Silica                                     | <b>68 ± 2</b>                 | <b>61 ± 3</b> | [21] |
|            |           | Anastase   | 47.4                          | 54.6          | [29] |
|            |           | $TiO_2$ II* ( <i>Columbite</i> )                     | 47.1                          | 54.3          | [29] |
|            |           | MI* ( <i>Baddeleyite</i> )                           | 48.0                          | 56.2          | [29] |
|            | DFT       | OI* ( <i>Orthorhombic-I</i> )                        | 48.1                          | 57.1          | [29] |
| $^{48}Ti$  |           | OII* ( <i>Cotunnite</i> )                            | 47.6                          | 57.0          | [29] |
|            |           |  | 46.3                          | 53.9          | [29] |
|            |           | Rutile   | 47.3                          | 56.2          | [30] |
|            |           |  | 44.8                          | 54.5          | [31] |
|            | MD        | Amorphous Rutile                                     | 48.7                          | 58.1          | [32] |
|            |           | Rutile Nanoparticle                                  | 49.0                          | 58.1          | [32] |
|            |           | <b>Average</b>                                       | <b>47.4</b>                   | <b>56.0</b>   |      |
|            | NRPS      | Rutile   | <b>44.7 ± 2</b>               |               | [33] |
|            | ECS       | Polycrystalline Rutile                               | <b>48 ± 2</b>                 | <b>53 ± 3</b> | [34] |
|            | DFT       | 1:7 (4-fold:3-fold) $^{16}O$ vacancies               | <b>42.5</b>                   | <b>62.5</b>   | [3]  |
| $^{178}Hf$ | ECS       | 20/60 nm $Hf^{16}O_2$ / $Hf^{18}O_2$ surface bilayer |                               | <b>63±3</b>   | [35] |

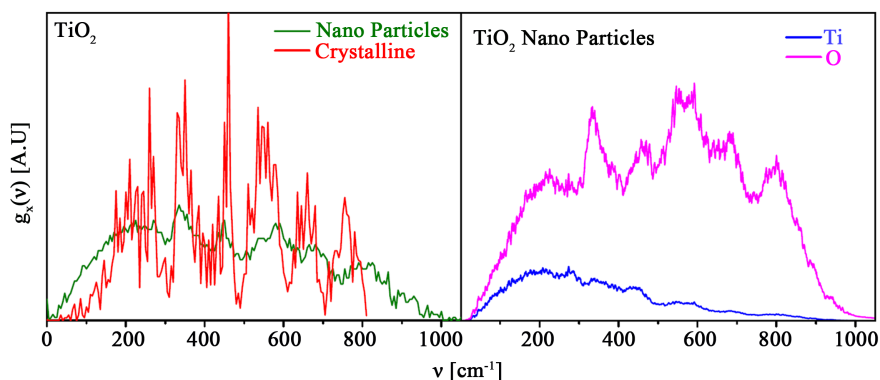
In cases where only the total VDOS is available, the use of Equation (1) yields the average kinetic energy  $\langle KE \rangle$  per atom of the compound, which is valuable for testing the ECS measured values. By combining the measured INS low [37] and high [38] phonon frequencies of  $v-SiO_2$  at room temperature,  $\langle KE \rangle = 63.9$  meV is deduced which agrees with the average measured ECS values of  $\alpha$ -Silica, being  $63.3 \pm 2$  meV. Following the same procedure for  $Ke$  deduced from the DFT of  $v-SiO_2$ , [26] yields  $\langle KE \rangle = 65.1$  meV which agrees with experiment to within 1.8% [37] [38].

Finally, it may be seen that  $Ke(X)$  in oxides systematically decreases with increasing mass of X. Note also that the OX bonds in oxides (Table 1) are strong covalent bonds and may be compared with  $Ke$  values of moderate ionic com-

pounds (as in KDP type ferroelectrics and super-protonic conductors [7]) and in weak metallic bonds. An interesting  $Ke(X)$  behavior emerges as depicted in **Figure 3** showing the average calculated values and the ECS results of **Table 1** including those of Li and Ca (in carbonate forms) [21]. In addition, estimates of  $Ke(X)$  for pure metallic Debye solids are given in **Figure 3** (see Ref. [7]) showing that  $Ke$  of covalently bonded metals in the present study are clearly higher than those in ionic and metallic solids. This observation strengthens the validity of our approach of deducing atomic  $Ke$  values. It is interesting to see if the atomic kinetic energy is sensitive to structural differences. Ghuman *et al.* [32] used MD and LD to study the VDOS of 3 nm rutile and amorphous  $TiO_2$  nanoparticles. Representative results are given in **Figure 4**.



**Figure 3.** Calculated (full circles) and experimental (ECS-triangles, NRPS-Square) room temperature kinetic energies of the elements in the oxide samples (current study-red), in ferroelectrics and protonic superconductors (green [7] [21]) and in pure metals. [7] Solid curves are drawn to lead the eye.



**Figure 4.** Left: Total VDOS of 3 nm rutile particles (green) and of rutile supercell (red). Right: PVDOS of the Ti (blue) and O (magenta) atoms in rutile nanoparticles.

**Figure 4** shows that nanoparticles feature a smeared blue shifted VDOS (by ca.  $200\text{ cm}^{-1}$ ) compared to that of the crystalline form (the supercell calculation), which could indicate a stronger Ti-O stretching in the nano-particles form. Moreover, the O atom shares the major part of the VDOS along the whole phonon states regime. By introducing the data of **Figure 4** into Equation (1) we find (**Table 1**) that  $\text{Ke}(\text{Ti})$  in the crystalline (rutile) form is 54.9 meV (averaged over 3 independent DFT simulations), in good agreement with the ECS measurement ( $53 \pm 3\text{ meV}$ ). In the nanoparticle and amorphous forms however, the MD simulated  $\text{Ke}(\text{H})$  is found to be the same, 58.1 meV. With fair statistical significance, such higher value may be understood as due to the extension of the VDOS towards more energetic phonons, as mentioned above. Contrary to titania, the case of Hafnia may poorly hint for an opposite behavior: as in titania, the total VDOS of the amorphous form was found to be smeared and blue shifted (by ca.  $100\text{ cm}^{-1}$ ) compared to the crystalline form, [39]. However the deduced  $\langle\text{KEs}\rangle$  (not shown in **Table 1**) in amorphous and crystalline forms are 50.9 and 51.6 meV respectively. The case of silica is less definitive (**Table 1**); while  $\text{Ke}(\text{Si})$  in amorphous silica (68.8 meV) is very close to the fused form (67.3 meV), it is also practically the same as that of the crystalline polymorph  $\alpha$ -Cristobalite (68.7 meV), and is higher than the other crystalline polymorph  $\alpha$ -Quartz (65.2 meV).

## 5. Summary

We show that the study of atomic kinetic energies, KE, of ceramic oxides using ECS scattering is a potentially valuable tool for understanding their molecular/lattice vibrations and dynamical behavior. This may be achieved by utilizing various theoretical modeling platforms such as LD, MD and DFT for high quality simulations of the partial and total VDOS. These were used for predicting Ke and comparing with ECS and NCS measured values. The methodology presented here may be applied for example to ceramic oxide based solid electrolytes, e.g.  $\text{ZrO}_2$ , for which it is of great interest to explore the dynamics of structural atoms, mainly of oxygen, near vacancies. Of interest is also the velocity or characteristic frequency of the ions near vacancies. Both may be important factors in enhancing the electrical current, nonetheless leaving the solid insulating for electrons. Calculating the  $\text{Ke}(\text{O})$  in crystalline electrolytes and its dependence on the concentration of the alloying cations, can thus provide a valuable test for the above suggested mechanism. It is our hope that ECS will evolve and improve in accuracy to make it possible to elucidate valuable structural information of ceramic oxides and inorganic materials of scientific and technological interest.

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