

# Chesapeake Bay Tidal Characteristics

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## Abstract

The basic knowledge of tidal characteristics in Chesapeake Bay is a prerequisite to understand the tidal processes in Chesapeake Bay. The tidal characteristics in Chesapeake Bay were assessed in this paper using basic tidal hydraulic analysis. Tidal elevation, currents and salinity data of Chesapeake Bay from National Oceanic and Atmospheric Administration (NOAA) were retrieved, and analyzed to understand Chesapeake Bay tide. General knowledge of location, geometry, tides, freshwater inputs, wind, salinity, etc in Chesapeake Bay was described. Sediment distribution of Chesapeake Bay was briefly described and discussed. Amplitude and phase of the selected major constituent, form factor, phase difference between tide elevations and currents at a few tidal elevation stations within Chesapeake Bay were calculated. Tidal prism was figured out using cubature method. The analysis approach could also be used as a source of reference for basic tidal study in other tide-affected field.

**Keywords:** Chesapeake Bay, Tidal Characteristics

## 1. Introduction

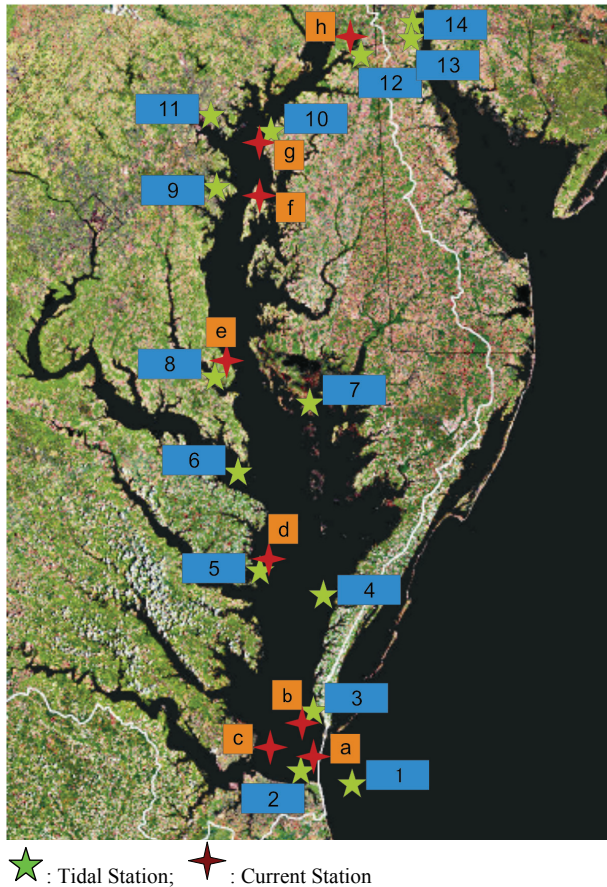
Chesapeake Bay encountered a severe environmental suffering during past a few decades, due to nitrogen, phosphorus and sediment pollution. It has been recognized that environmental quality factors are directly dependent on the tides in the Bay [1].

Chesapeake Bay is the largest bay in US. The Chesapeake Bay and its tributaries are the best studied estuaries in the world [2]. The Chesapeake Bay “main stem”, defined by tidal zones, is approximately 195 mi (315 km) long and 3.5 to 35 mi (5.6 to 56 km) wide, and has a surface area of nearly 4,400 mi<sup>2</sup> (11,601 km<sup>2</sup>). The main stem is entirely within Maryland and Virginia. Nearly 50 rivers, with thousands of tributary streams and creeks, drain the approximately 64,000 mi<sup>2</sup> (166,000 km<sup>2</sup>) forming the Chesapeake Bay Basin. The basin contains more than 150,000 stream miles (241,500 km) in the District of Columbia and parts of six states: New York, Pennsylvania, Maryland, Virginia, West Virginia, and Delaware [3]. **Figure 1** shows the location of Chesapeake Bay in accordance with “NOAA Tides and Currents”. In addition, the fourteen tidal elevation stations and seven tidal current stations are indicated (see **Table 1** for details).

The Chesapeake estuary is a drowned river and it is partially mixed. The depths are relatively shallow, so that

mixing of at least moderate magnitude extends to the depths. In the total estuary approximately 50% of the system is less than 20 ft (6 m) deep, 35% has depths greater than 30 ft (9 m), 18% greater than 40 ft (12 m), and only 8% greater than 60 ft (18.3 m) [2].

Tides and freshwater inputs from the various tributaries of the Chesapeake Bay control the hydraulics of the bay [1]. National Research Council (2004) mentioned that three main factors influencing Chesapeake Bay’s circulation: freshwater inflow, the geometry of the basin, and tidal strength. Due to its small depth-length ratio, Chesapeake Bay accommodates slightly more than one semidiurnal tidal wave at all times, which results in a special tidal characteristics within Chesapeake Bay. Although the Bay has more than 50 tributary rivers, only 3—the Susquehanna, Potomac, and James—account for more than 80% of the total freshwater input, with Susquehanna accounting for nearly half of the total (49%). All Eastern Shore Rivers combined contribute less than 4% of the total. In the average year, the total amount of freshwater discharged into the Bay (71 km<sup>3</sup> or 17 mi<sup>3</sup>) is roughly equivalent to the tidal mean volume of the Chesapeake Bay estuarine system (76 km<sup>3</sup> or 18 mi<sup>3</sup>)—the combined volume of the Bay proper and its tributary estuaries. The flows of the Bay’s major rivers are typical of mid-latitude rivers: high discharges in spring, pro-



**Figure 1. Chesapeake bay map.**

duced by snow melt and spring rains; low flows in late summer and early fall, followed by moderate flows through-out the remainder of the year [4]. Fresh water in Chesapeake Bay has a mean residence time of 7 months [5].

Wind is also reported as an important energy input in Chesapeake Bay. Zhong and Li [6] proposed that tidal and wind forcing appears to have nearly equal importance in Chesapeake Bay. Chesapeake Bay is classified as a partially-stratified estuary [7].

The main channel is of 5 to 7 km (4.4 mi) width and 23 m (75 ft) depth at the mouth of the Chesapeake Bay [8]. Bathymetries in the Upper Chesapeake Bay are characterized by a steep east-west slope and a relatively gentle north-south slope. A narrow and deep navigation channel exceeding 9 m (30 ft) follows the contour of the eastern coast, bounded to the west by broad banks [9]. The Chesapeake & Delaware Canal runs 14 miles long, 450 feet wide and 35 feet deep across Maryland and Delaware, connecting the Delaware River with the Chesapeake Bay and the Port of Baltimore. The C&D Canal is owned and operated by the U.S. Army Corps of Engineers, Philadelphia District.

The mean tidal range decreases from 0.9 m (3 ft) at the

Bay's entrance (Chesapeake BBT) to a minimum of 0.3 m (1.0 ft) at Annapolis, then rises to 0.7 m (2.3 ft) at the head. Average tidal current amplitudes decrease from a maximum of 1.03 m/s (3.38 ft/s) at the mouth to a minimum of 0.13 m/s (0.43 ft/s) in the middle Bay, but increase to 0.59 m/s (1.94 ft/s) at Baltimore in the upper Bay [6].

The tidal and current range on the eastern shore is generally higher than that on the corresponding western shore, which is mostly explained as the result of earth rotation. However, Wang and Chao [9] proposed that the deep channel is the root cause of the current intensification, while the earth's rotation does not play a crucial role.

The salinity increases from zero at the head of the estuary to nearly that of seawater at the mouth. In the upper Chesapeake Bay and in each tributary estuary there are considerable seasonal variations in salinity which diminish in magnitude in magnitude toward the mouths of these estuaries [2].

**Figures 2 and 3** are one-month and three-day tides at Chesapeake Light (8638979), respectively. These two plots reveal that the tide is predominantly driven by semidiurnal constituent. The magnitudes of Spring and Neap tide ranges are approximately 1.7 m (5.6 ft) and 0.7 m (2.3 ft), respectively, as shown in **Figure 2**. Also, the mean tide range is around 1.2 m (3.9 ft).

The understanding of tidal characteristics is the premise to learn tidal and sediment transport processes in estuarine areas. Investigation on hydrodynamic environment of the bay is in favor of comprehending pollutant transport and mechanism of deep water zone maintaining [10]. Therefore, it is desirable to perform a general basic tidal study in Chesapeake Bay in order to further understand the tidal characteristic in Chesapeake Bay. In addition, the basic tidal analysis approaches can be optionally used in other estuaries.

## 2. Tidal Characteristics within Chesapeake Bay

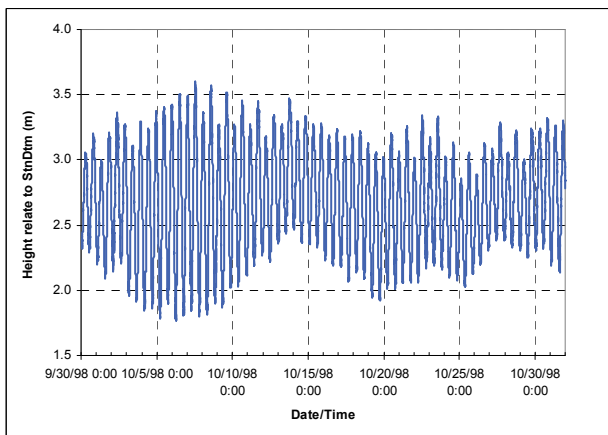
### 2.1. Stations and General Issues

**Table 1** lists the tidal stations (See **Figure 1** for the locations) and **Table 2** describes their tidal characteristics.  $M_2$  constituent is obviously the dominant constituent with the next largest constituent being an order of magnitude less in amplitude. Annapolis has the lowest  $M_2$  tidal elevation, while the higher tide occurs at both the entrance of the Bay and the C&D Canal. Also, the tide on eastern shore has the higher amplitude than that on western shore. In addition, Salas-Monreal and Valle-Levinson [11] provided the mean depths of transects through a few stations.

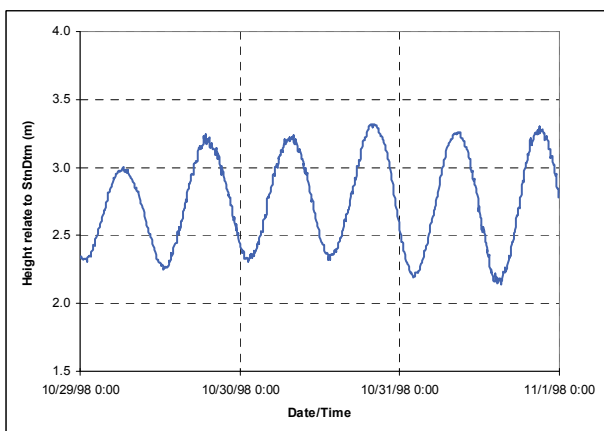
**Table 1. Tidal characteristics at water elevation stations.**

Station	Station ID	Latitude (N)	Latitude (W)	location
Chesapeake Light Tower	8638979	36°54.3'	75°41.8'	Ocean
Chesapeake BBT	8638863	36°58.0'	76°6.8'	
Kiptopeke	8632200	37°9.9'	75°59.3'	Lower bay
Rappahamcock Light	8632837	37°32.3'	76°0.9'	
Windmill Point	8636580	37°36.9'	76°17.4'	
Lewisetta	8635750	37°59.8'	76°27.9'	
Bishops Head	8571421	38°13.2'	76°2.3'	Mid bay
Solomons Isand	8577330	38°19.0'	76°27.1'	
Annapolis	8575512	38°59.0'	76°28.9'	
Tolchester Beach	8573364	39°12.8'	76°14.7'	Upper bay
Baltimore**	8574680	39°16.0'	76°34.7'	
Chesapeake City	8573927	39°31.6'	75°48.6'	
Reedy Point	8551910	39°33.5'	75°34.4'	C&d canal
Delaware City	8551762	39°34.9'	75°35.3'	

Note: \* For C&D canal tide analysis only; \*\* For salinity discussion only



**Figure 2. One-month ocean tide at Chesapeake light.**



**Figure 3. Three-day ocean tide at Chesapeake light.**

**Table 3** gives the Chesapeake Bay current stations from Chesapeake Bay Port (See **Figure 1** for the locations).

The relative importance of the diurnal and semidiurnal tidal constituents and tide classification can be expressed in terms of form factor as shown in **Table 2** [12], which is defined as,

$$F = \frac{K_1 + O_1}{M_2 + S_2}$$

where  $K_1$ ,  $O_1$ ,  $M_2$ , and  $S_2$  are the amplitudes of the corresponding tidal constituents. In terms of the form factor,  $F$ , the tides may be roughly classified as shown in **Table 4**.

The calculated form factors reveal that semidiurnal tide is almost throughout Chesapeake Bay except for the standing wave in three upper Bay stations (Annapolis, Tolchester Beach, and Baltimore) with higher latitudes.

The natural fundamental period  $T_n$  can be calculated as below,

$$T_n = \frac{2s}{\sqrt{gh}}$$

where  $s$  is the length of Chesapeake Bay, 320 km;  $g$  is the gravity acceleration,  $9.81\text{m/s}^2$ ,  $\bar{h}$  is the mean depth of Chesapeake Bay, 5 m [13]. The calculated natural fundamental period  $T_n$ , 25.38 hours, is closer to the diurnal tidal period, thus, amplification of diurnal tide could be observed. In accordance with Schwartz [14], the diurnal tide could be amplified at near the semidiurnal nodal area where semidiurnal tide range is small (see **Figure 4**). In accordance with **Figure 4**, Windmill Point is located near the semidiurnal nodal area, around  $-230$  km ( $-149$  mi) from the upstream end. The form factor at Windmill Point, representing mixed mainly semidiurnal tide, is slightly higher than those at adjacent stations with semidiurnal tide as shown in **Table 2**. Consequently, approximate nodal area locations of Windmill Point might be a reason for the observed a little bit amplification of diurnal signal at Windmill Point. Referring to Huang *et al.* [9], as Rappahamcock Light and Bishop Head have higher  $M_4/M_2$  than other stations within Chesapeake Bay, shallower tidal wave would be assumed at these two locations. Therefore, more attentions might have to be paid to there due to probable significant sediment transport processes around these two stations.

**Figure 4** is the calculated  $M_2$  tidal amplitudes in Chesapeake Bay with friction by superposition of the incident and reflective waves. The friction is represented by an exponential function [15]— $\exp(-\mu x)$  ( $\mu$  is the amplitude damping coefficient;  $x$  is the travel distance starting from the mouth of the Bay, m). Then, the super

**Table 2. Tidal characteristics at water elevation stations.**

Station	Depth(m)	Amplitude of Constituents (m)							Form Factor
		M2	S2	K1	O1	M4	M6	M8	
Chesapeake Light Tower	18.30								
Chesapeake BBT	9.14	0.380	0.069	0.058	0.045	0.005	0.006	0.000	0.229
Kiptopeke	7.70	0.388	0.068	0.059	0.046	0.005	0.005	0.000	0.230
Rappahamcock Light		0.239	0.034	0.041	0.030	0.014	0.005	0.000	0.260
Windmill Point		0.175	0.030	0.030	0.023	0.009	0.003	0.000	0.259
Lewisetta	8.50	0.184	0.028	0.023	0.019	0.004	0.003	0.000	0.198
Bishops Head		0.267	0.033	0.042	0.029	0.018	0.002	0.001	0.237
Solomons Island	15.00	0.171	0.026	0.027	0.023	0.005	0.003	0.000	0.254
Annapolis		0.139	0.022	0.059	0.048	0.004	0.003	0.000	0.665
Tolchester Beach	5.30	0.174	0.024	0.069	0.058	0.004	0.000	0.000	0.641
Baltimore**		0.159	0.023	0.069	0.056	0.008	0.000	0.000	0.687
Chesapeake City		0.434	0.059	0.032	0.014	0.026	0.009	0.003	0.093
Reedy Point		0.773	0.100	0.089	0.068	0.055	0.033	0.007	0.180
Delaware City		0.744	0.100	0.095	0.068	0.060	0.033	0.006	0.193

Note: \* For C&D canal tide analysis only; \*\* For salinity discussion only The depths data at the stations are excerpted from Salas-Monreal and Valle-Levinson (2008).

**Table 3. Chesapeake bay current stations.**

Station	Station ID	Location
a. Cape Henry LB '2CH'	cb0102	
b. York Spit LBB 22	cb0201	Lower Bay
c. Thimble Shoal LB '18'	cb0301	
d. Rappahannock Shoal Channel LBB '60'	cb0801	Mid Bay
e. Cove Point LNG Pier	cb1001	
f. Chesapeake Channel LBB '92'	cb1101	Upper Bay
g. Tolchester Front Range	cb1201	
h. Chesapeake City	cb1301	C&D Canal

**Table 4. Tide classification.**

Form Factor, F	Types of Tide
0~0.25	Semidiurnal
0.25~1.50	Mixed Mainly Semidiurnal
1.50~3.00	Mixed Mainly Diurnal
>3.00	Diurnal

position of the incident and reflective waves can be expressed as,

$$\eta(t, x) = a_{M_2} \cos(\sigma t - kx) = A \{ \exp(-\mu(s+x)) \cos(\sigma t - kx) + \exp(-\mu(s-x)) \cos(\sigma t + kx) \}$$

where  $\eta(t, x)$  is water surface profile for the integrated wave, m;  $a_{M_2}$  is the  $M_2$  constituent amplitude, m,  $A$  is

the  $M_2$  constituent amplitude of the progressive wave at the entrance, m;  $K$  is wave number,  $m^{-1}$ ;  $\sigma$  is wave angular frequency,  $s^{-1}$ . Therefore, the  $M_2$  constituent amplitude within Chesapeake Bay is,

$$a_{M_2} = A \{ \exp(-\mu(s+x)) + \exp(-\mu(s-x)) \cos 2kx \}$$

Both the  $M_2$  constituent amplitudes at CBBT (0.380 m at -320 km) and Tolchester Beach (0.174 m at -40 km) are used to figure out the damping coefficient,  $\mu = 1.65 \times 10^{-6}$ , which adjusts the amplitudes of both incident and reflective waves along the travel distance. Similar to Boon [13], **Figure 4** represent that two minimum tidal amplitudes occur at around -80 km (-50 mi) and -230 km (-143 mi) from the upstream end, which approximately corresponding to somewhere close to Annapolis and Windmill Point, respectively. The amplitudes at both Windmill Point and Annapolis are relative low comparing with other stations, which matches the result as shown in **Figure 4**. Because of friction and energy dissipation, the amplitude at the upper Bay is generally lower even with the effect of reflection in accordance with **Table 2** and **Figure 4**, although the  $M_2$  constituent amplitude at upper Bay might be overestimated in **Figure 4** due to the assumed constant damping coefficient,  $\mu$ . In brief, there are two areas with lower  $M_2$  constituent amplitude, and a generally decrease of the amplitude of the dominant  $M_2$  constituents, as tide moves upstream. Standing wave characteristics and narrowness at Chesapeake City result in higher  $M_2$  tide there.

**Figure 5** depicts the 3-day salinity at three stations,



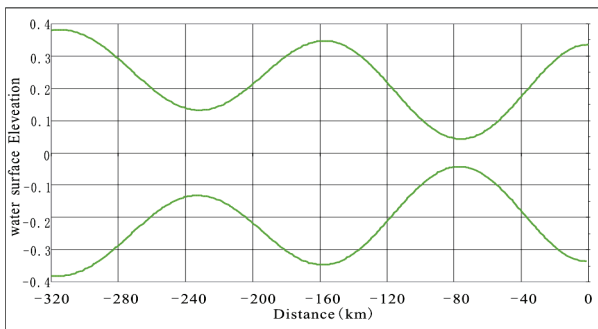
and the salinity decreases gradually from the mouth (~22 ppt at CBBT) up to the upper Chesapeake Bay (~6 ppt at Baltimore). The salinity at CBBT is more sensitive to the tidal elevation, while the salinities at Lewisetta and Baltimore are almost constant in this short time period. The peak salinity at CBBT is in response to the water surface elevation to some extent in accordance with **Figure 5**.

For this partially mixing Bay, seasonal-varied freshwater flow might be most influencing factor affecting salinity distribution in Chesapeake Bay.

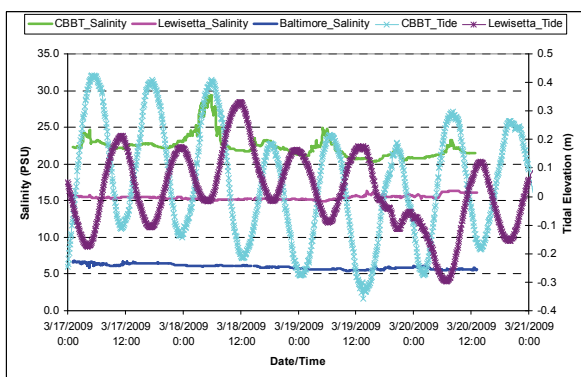
The deep channel, along with earth rotation and freshwater effects (due to predominant freshwater from Western Shore), might make a lower salinity on western shore. Stronger stratification could be observed at upper end with lower tidal velocity. Vertical stratification is not discussed in detail for data deficiency.

In recent decades, Chesapeake Bay has had widespread water quality problems due to fine sediment. Sediment distribution is usually dominated by hydraulic condition and material origin [10]. Tidal current, freshwater, wind, etc could be the factors affecting the process of sediment transport and the distribution of sediment. Without considering freshwater input, **Table 5** shows the calculated near bed velocity amplitude of tidal stations based on dominant  $M_2$  constituent. The near bed velocity amplitude can be expressed as

$$V_b = \frac{a_{M_2} g k}{\sigma} \frac{1}{\cosh(kh)}$$



**Figure 4. Calculated  $M_2$  constituent tidal amplitudes in Chesapeake Bay with friction.**



**Figure 5. Salinity in Chesapeake Bay**

where  $V$  is near bed velocity amplitude at the location of the station, m/s;  $h$  is water depth, m. The higher the velocity amplitude, the more important the sediment process at the station. In accordance with the criteria, the sediment process at both lower Bay and C&D Canal is significant. **Table 5** also depicts that velocity amplitude at the bed on the eastern shore is generally higher than that on the corresponding western shore due to the higher amplitude of  $M_2$  constituent. Therefore, the gradient of bottom shear stress from eastern shore to western shore could be assumed for a general sediment transport estimate.

Freshwater brings great amount of fine sediment, while the force resulting from freshwater flow is in both local scale and lower magnitude. Therefore, tidal force could be more important in the general sediment transport and re-distribution at Chesapeake Bay. Tidal current dominates the process of sediment transport, controlling the distribution of sediment and development of seabed [10]. The long-term annual average of suspended material contributed by the Chesapeake Bay basins is approximately 4.3 million tons per year. About 90 percent of this material came from the three largest rivers (Susquehanna, Potomac, and James). It was assumed that the great majority of the sediment supplied from the freshwater flow is fine-grained silts and clays [3]. More fine sediment is supposed to be accumulated at western shore, as freshwater inflows are located mostly close to western shore.

Consequently, differentiating sediment transport & distribution in western shore from that in eastern shore is necessary in both water quality modeling and the following restoration practice.

Sediment distribution along the length of Chesapeake Bay is even more elusive due to complex interactions among tide, freshwater input, wind, bathymetry, etc. Data indicated that the greatest sediment volume is associated with the bay mouth, which further suggests that the continental shelf has been more significant source of sediment to the Bay with high tidal velocity (see **Table 5**) than the Susquehanna River and other watershed tributaries [3]. Although sand is the predominant sediment type in the lower Bay, part is composed of clay and silt-sized material and there also is good evidence for its significant net up estuary transport [3]. Therefore, a quantification of northward Bay fine sediment transport determines the water quality in both lower Bay and other tidal-affected area. In another word, controlling the fine sediment movement in lower Bay could be an important step to improve water quality in the Bay.

## 2.2. Tide at Entrance (Chesapeake BBT)

Corresponding to the Spring and Neap tidal variations Tide range varies between 0.5 m (1.6 ft) and 1.0 m (3.3 ft)

at the entrance of Chesapeake Bay (See **Figure 6**).

**2.3. Tidal Currents**

**Figure 7** shows the general currents within Chesapeake Bay at current stations as shown in **Figure 1**. Not solely related to the tidal elevation, the magnitude of current at each station is affected but multi-factors such as cross area, freshwater flow, etc. Phase difference is noticed in accordance with **Figure 7**. Although there is no observed data at current station cb1001, which is close to narrowing Solomons Island, higher velocity could be the fact at this station for the smaller cross section.

**Figure 8** shows both the tidal elevation at Chesapeake BBT and current at cb0102. Since cb0102 is rather close to Chesapeake BBT, so the current at cb0102 could be approximately used for Chesapeake BBT. Generally, not much phase difference is observed between the tide and current, which matches the result of in-phase generated by Whitford [8]. However, wind might be the primary reason for the discrepancy during 03/18/2009 12:00–03/19/2009 06:00.

Excluding the effect of wind, **Figure 9** depicts tidal elevation at Chesapeake BBT, currents at both cb0102 and cb0301 during the period of 09/21/2008 16:00–09/22/2008 13:00 (wind speed is nearly zero). An approximate in-phase result is observed in **Figure 9**, which matches the accepted mainly progressive wave at the entrance.

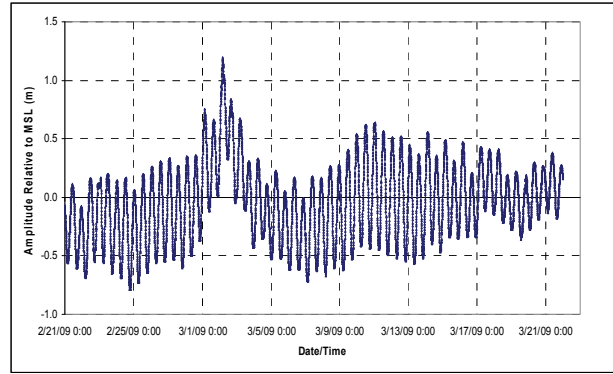
The characteristics of mainly standing waves are obviously observed at both Annapolis and Tolchester Beach as shown in **Figures 10** and **11**, respectively. Lower tidal velocity occurs at Tolchester Beach with the standing wave.

In accordance with **Figures 10** and **11**, more saw-toothed pattern tides in upper Bay indicate more upland tides.

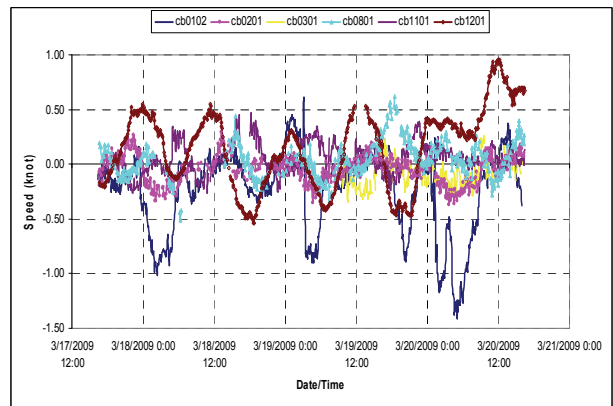
**2.4. Phase Aspect of the Tide Elevation in Chesapeake Bay**

NOAA Predicted tidal elevations at 9 stations within Chesapeake Bay are shown in **Figure 12**. The changes of the tidal amplitudes are observed along the main channel seem to be a consequence of the interaction between the tide and the Bay morphology as well as the wave reflection, and are described by the law of energy conservation [16]. It is observed that the whole bay experienced a low tide on January, 9, 2009. Comparing the tidal phase lag for  $M_2$  constituent from the entrance against the plots in **Figure 12**, it is not difficult to find that they are in good agreement.

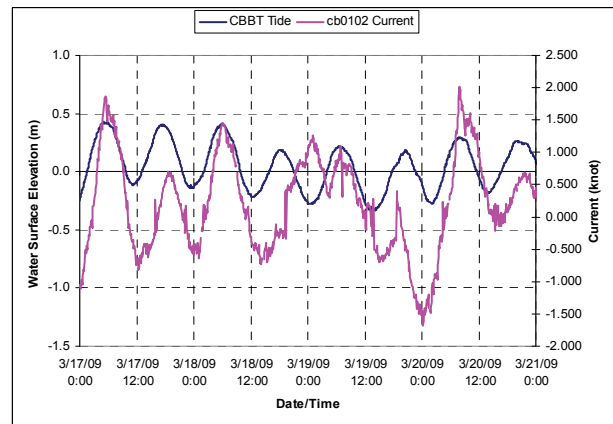
**Table 6** lists the tidal phase lag from the entrance (Chesapeake BBT) in terms of the dominated  $M_2$  constituent. **Table 7** lists the tidal phase lag from the en-



**Figure 6. Observed spring and neap tide cycle at entrance (chesapeake BBT).**



**Figure 7. Observed tidal currents within chesapeake bay.**



**Figure 8. Tide and current at the entrance with wind effect (chesapeake BBT).**

trance (Chesapeake BBT) in terms of the  $K_1$  constituent. The region from Chesapeake BBT to Lewisetta is more like a progressive wave region. However, there is a narrowing of the channel around Solomons Island, and there is only around half hour lag for  $M_2$  and two and half hours for  $K_1$ . Therefore, a standing wave is indicated and the tide is likely to be amplified around Solomon Island.

### 2.5. Tide Prism

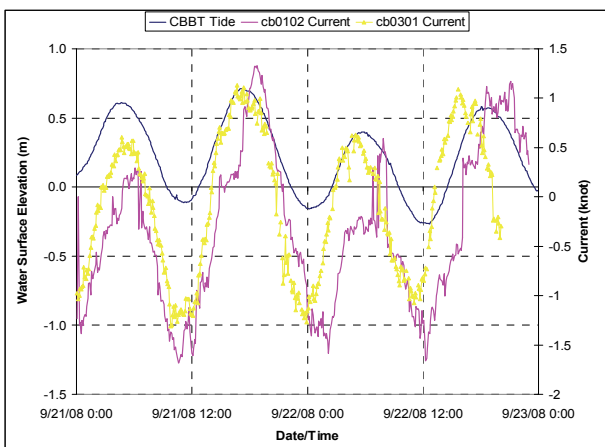
Cubature method is employed to calculate the tidal prism (03/18/2009) of Chesapeake Bay in accordance with the tide on 03/18/2009 in **Figure 12**. The identification of subareas is shown in **Figure 13**, and the tidal prism is calculated as shown in **Table 8**.

The tidal prism is about for  $M_2$  constituent is around  $1.25 \times 10^9 \text{ m}^3$  ( $4.41 \times 10^{10} \text{ ft}^3$ ) as shown in **Table 8**. Freshwater flow is around  $4,250 \text{ m}^3/\text{s}$  ( $150,000 \text{ ft}^3/\text{s}$ ) in March in accordance with USGS.

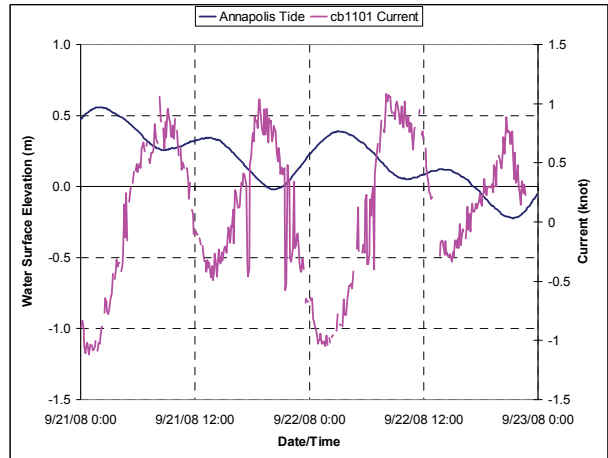
**Table 5. Near bed velocity amplitude of tidal stations based on  $M_2$ .**

Station	Depth (m)	Amplitude of Constituent	Near Bed Velocity Amplitude
		$M_2$ (m)	Vb (m/s)
Chesapeake Light Tower	18.30		
Chesapeake BBT	9.14	0.380	0.394
Kiptopeke	7.70	0.388	0.438
Rappahamock Light@	8.00	0.239	0.265
Windmill Point@	8.00	0.175	0.194
Lewisetta	8.50	0.184	0.198
Bishops Head@	8.00	0.267	0.296
Solomons Island	15.00	0.171	0.138
Annapolis@	6.00	0.139	0.178
Tolchester Beach	5.30	0.174	0.237
Baltimore **@	5.00	0.159	0.223
Chesapeake City *	10.00	0.434	0.430
Reedy Point *	10.00	0.773	0.766
Delaware City *	10.00	0.744	0.737

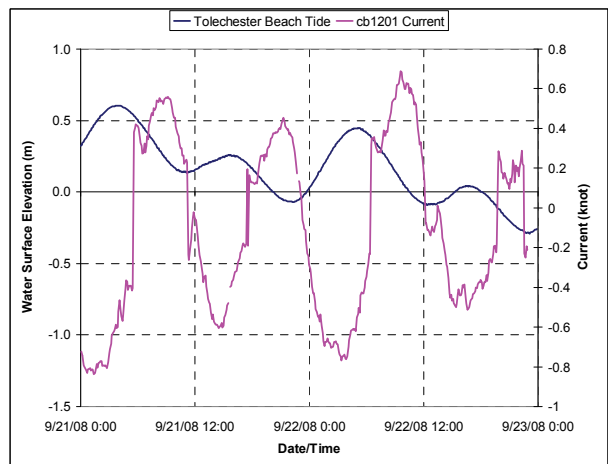
Note: @ Depth Data are assumed with uncertainty



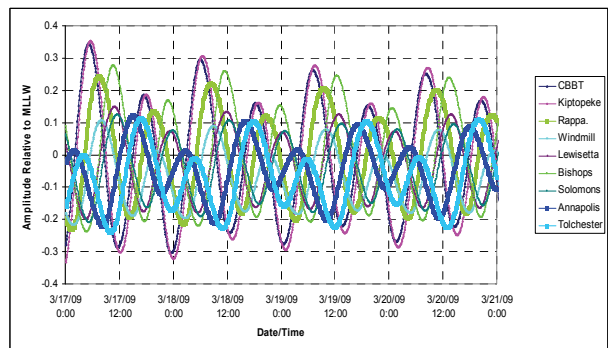
**Figure 9. Tide and current at the entrance (chesapeake BBT).**



**Figure 10. Tide and current at annapolis.**



**Figure 11. Tide and current at tolchester beach.**



**Figure 12. Predicted tides elevations within chesapeake bay.**

Therefore, freshwater volume in 12.42 hours is  $1.90 \times 10^8 \text{ m}^3$  ( $6.71 \times 10^9 \text{ ft}^3$ ) approximately. Consequently, the Canter Cremer Estuary Number can be figured out as  $N = 0.15$ , which shows that the Chesapeake Bay is partially mixed as  $N > 0.10$  in this specific time period. Consequently, the tidal prism formula [17] in terms of  $M_2$  constituent gives a lower limit of flushing time of 3.2 days.

**Table 6. Tidal phase lag for  $M_2$  from the entrance (Chesapeake BBT).**

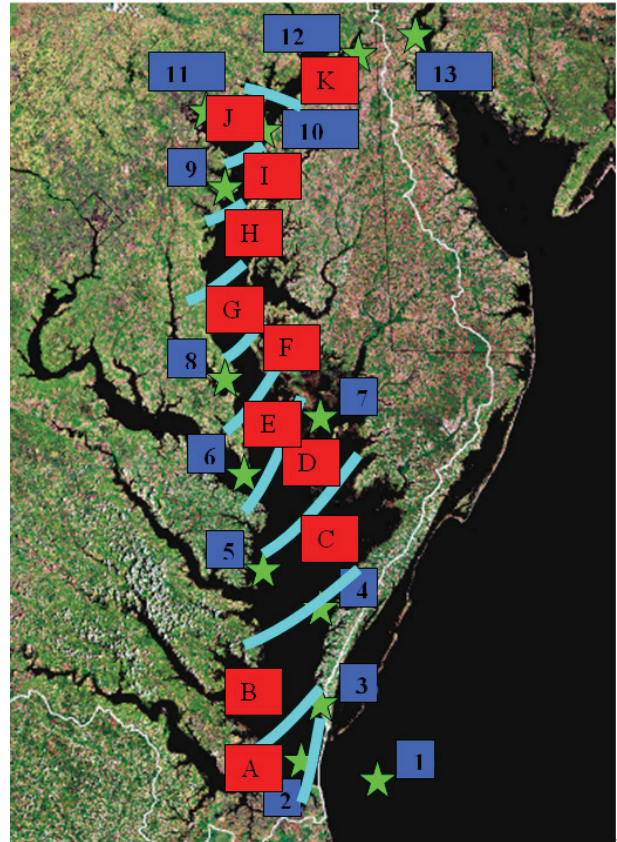
Station	Station ID	Types of Tide	Epoch (°)	Phase Lag From Entrance	
				in (degree °)	in hour
Chesapeake BBT	8638863	Semi-diurnal	21.0	0.0	0.00
Kiptopeke	8632200	Semi-diurnal	32.5	11.5	0.40
Rappahamock Light	8632837	Mixed Mainly	86.8	65.8	2.27
Windmill Point	8636580	Semi-diurnal	103.2	82.2	2.84
Lewisetta	8635750	Semi-diurnal	176.4	155.4	5.36
Bishops Head	8571421	Semi-diurnal	181.9	160.9	5.55
Solomons Island	8577330	Mixed Mainly	198.8	177.8	6.13
Annapolis	8575512	Semi-diurnal	291.6	270.6	9.34
Tolchester Beach	8573364		346.6	325.6	11.23

**Table 7. Tidal phase lag for  $K_1$  from the entrance (Chesapeake BBT).**

Station	Station ID	Types of Tide	Epoch (°)	Phase Lag From Entrance	
				in (degree °)	in hour
Chesapeake BBT	8638863	Semidi-urnal	184.9	0	0.00
Kiptopeke	8632200	Semidi-urnal	193.4	8.5	0.57
Rappahamock Light	8632837	Mixed Mainly	222.4	37.5	2.49
Windmill Point	8636580	Semidi-urnal	226.7	41.8	2.78
Lewisetta	8635750	Semidi-urnal	276.2	91.3	6.07
Bishops Head	8571421	Semidi-urnal	283.3	98.4	6.54
Solomons Island	8577330	Mixed Mainly	315.6	130.7	8.69
Annapolis	8575512	Semidi-urnal	356.7	171.8	11.42
Tolchester Beach	8573364		3.3	178.4	11.86

**2.6. C&D Canal Analysis**

The Canal could be regarded as open to Chesapeake Bay (Left end open). **Figure 14** shows the observed tidal elevations at Chesapeake City and Reedy Point located on C&D Canal.  $M_2$  constituent is the dominant constituent at both these two stations in accordance with **Table 2**. Consequently, information on the progressive wave in C&D Canal is summarized in **Table 9**. Ideally, the tidal elevation at Chesapeake City would be nearly zero for its location on node, and the standing waves at both stations are in phase. However, some distortions on both ampli-



**Figure 13. Subarea map**

**Table 8. Tidal prism calculation using cubature method**

Subarea	Area Fraction	Phase Range		Phase Range	Volume Entering or Leaving (km <sup>3</sup> )
		Contour 1	Contour 2		
A	0.10	0.61	0.62	0.62	0.71
B	0.12	0.62	0.17	0.40	0.55
C	0.16	0.17	0.06	0.12	0.21
D	0.12	0.06	-0.14	-0.04	-0.06
E	0.12	-0.14	-0.08	-0.11	-0.15
F	0.08	-0.08	-0.26	-0.17	-0.16
G	0.06	-0.26	-0.15	-0.21	-0.14
H	0.06	-0.15	-0.04	-0.10	-0.07
I	0.06	-0.04	0.05	0.01	0.00
J	0.06	0.30	0.15	0.23	0.16
K	0.06	0.35	0.18	0.27	0.18
Tidal Prism					1.25

tude and phase occur due to the imperfect reflection resulting from Upper Chesapeake Bay’s morphology.

**Figure 15** represents that an approximate 90° phase difference exists between tidal elevation and current at Chesapeake City due to the effect of standing wave.



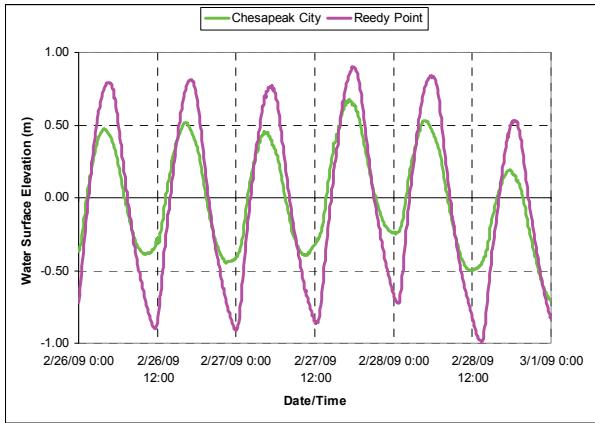


Figure 14. Observed tidal elevations in Chesapeake Bay & Delaware Bay Canal.

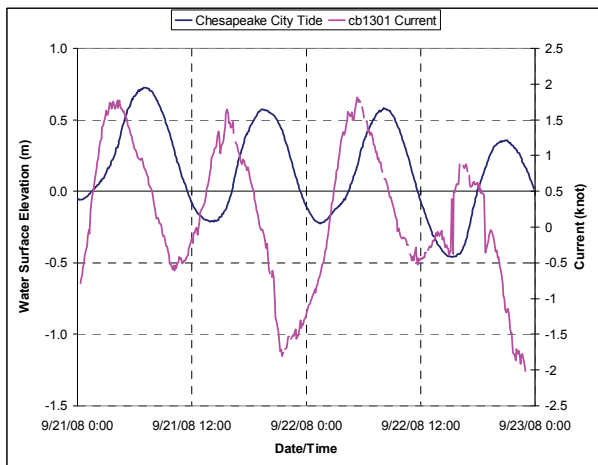


Figure 15. Tide and current at Chesapeake City.

Table 9. Progressive wave in C&D canal.

	Canal Tide
Amplitude (m)	0.75
Time Period, T (hour)	12.42
Wavelength, L (m)	457404
Wave Celerity, C (m/s)	10.23
Canal Length, l (m)	22531
Water Depth, h (m)	11.93
h/L	2.61E-05
Wave Type	Long
Wave Number, k	1.37E-05
Wave Frequency, $\sigma$	0.00014
Maximum Vel. (m/s)	0.72

### 3. Conclusions

This paper performs basic tidal analyses of Chesapeake

Bay so as to represent a basic tidal analysis approach and provide tidal information for the understanding of tide, sediment transport, and other processes in Chesapeake Bay.

The general distributions of tidal and current ranges, salinity probably result from deep channel, earth rotation, and freshwater discharge. A brief description of general sediment distribution in Chesapeake Bay was represented in this paper in accordance with tidal characteristics and Langland and Cronin [3]. Wind has a significant impact on the tides in Chesapeake Bay.

Taking friction into considered, dominant semidiurnal  $M_2$  constituent tidal elevations within Chesapeake Bay were computed to compare against the actual  $M_2$  amplitudes, and they are found in good agreement. Higher  $M_2$  amplitude was observed at Chesapeake City due to standing wave and the narrowing of C&D Canal.

Removing the effect of wind, mainly progressive wave at the entrance and mainly standing waves are at upper Chesapeake Bay were observed.

The changes of the tidal amplitudes are the consequence of the interaction between the tide and the bay morphology as well as the wave reflection.

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