

An Overview of Principal Component Analysis

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Received May, 2013.

ABSTRACT

The principal component analysis (PCA) is a kind of algorithms in biometrics. It is a statistics technical and used orthogonal transformation to convert a set of observations of possibly correlated variables into a set of values of linearly uncorrelated variables. PCA also is a tool to reduce multidimensional data to lower dimensions while retaining most of the information. It covers standard deviation, covariance, and eigenvectors. This background knowledge is meant to make the PCA section very straightforward, but can be skipped if the concepts are already familiar.

Keywords: Biometric; PCA; Eigenvector; Covariance; Standard Deviation

1. Introduction

Biometrics is derived from Greek words “bio” meaning life and metrics meaning the term biometrics is derived from the Greek words bio meaning “life” and metrics meaning “to measure” [1]. Biometrics refers to the identification or verification of a person based on his/her physiological and/or behavioral characteristics [2]. Several verification and identification based biometrics have evolved based on various unique aspects of human body, ease of acquiring the biometric, public acceptance and the degree of security required [3].

Principal component analysis (PCA), also known as Karhunen-Loeve expansion, is a classical feature extraction and data representation technique widely used in the areas of pattern recognition and computer vision such as face recognition [4]. The strategy of the Eigenfaces method consists of extracting the characteristic features on the face and representing the face in question as a linear combination of the so called ‘eigenfaces’ obtained from the feature extraction process [5]. The principal components of the faces in the training set are calculated. Recognition is achieved using the projection of the face into the space formed by the eigenfaces [6]. A comparison on the basis of the Euclidian distance of the eigenvectors of the eigenfaces and the eigenface of the image under question is made [7]. If this distance is small enough, the person is identified [8]. On the other hand, if the distance is too large, the image is regarded as one that belongs to an individual for which the system has to be trained [9]. Principal component analysis is a statistics

technical [10]. PCA used for reduce dimension vector to better recognize images [11]. PCA is a useful statistical technique that has found application in fields such as face recognition and image compression, and is a common technique for finding patterns in data of high dimension [12]. Before getting to a description of PCA, this tutorial first introduces mathematical concepts that will be used in PCA. It covers standard deviation, covariance, and eigenvectors [13]. This background knowledge is meant to make the PCA section very straightforward, but can be skipped if the concepts are already familiar [10, 14]. The basis of the eigenfaces method is the Principal Component Analysis (PCA). Eigenfaces and PCA have been used by Sirovich and Kirby to represent the face images efficiently [15, 16].

2. PCA Algorithm

Following are steps involve;

Step 1: Column or row vector of size N^2 represents the set of M images ($B_1, B_2, B_3 \dots B_M$) with size $N \times N$

Step 2: The training set image average (μ) is described as

$$\mu = \frac{1}{m} \sum_{n=1}^M B_n \quad (1)$$

Step 3: the average image by vector (W) is different for each trainee image

$$W_i = B_i - \mu \quad (2)$$

Step 4: Total Scatter Matrix or Covariance Matrix is calculated from Φ as shown below:

$$C = \sum_{n=1}^M w_n w_n^T = A A^T, \tag{3}$$

where $A = [W_1 W_2 W_3 \dots W_n]$

Step 5: Measure the eigenvectors U_L and eigenvalues λ_L of the covariance matrix C .

Step6: For image classification, this feature space can be utilized. Measure the vectors of weights

$$\Omega^T = [w_1, w_2, \dots, w_M], \tag{4}$$

whereby,

$$H_k = U_k^T (B - \mu), k = 1, 2, \dots, M' \tag{5}$$

3. The Important of PCA in Face Recognition

The statistical information published in the area of facial recognition technology utilizing the PCA method reveals the significance of using this method for identifying and verifying facial features [8]. **Figure 1** below reveals the amount of publications that have used the words ‘face recognition’ and ‘PCA’ in their headings [17]

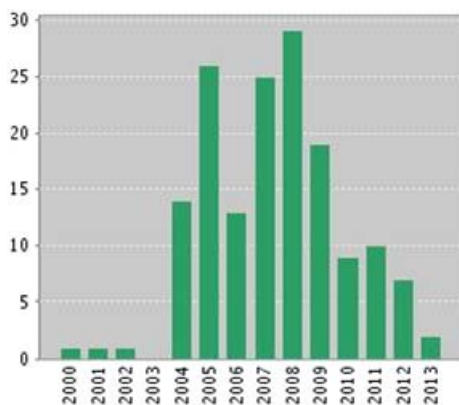


Figure 1. Number of publication utilizing [15].

Table 1 shows features about principal component analysis.

4. Advantage and disadvantage of PCA

PCA’s key advantages are its low noise sensitivity, the decreased requirements for capacity and memory, and increased efficiency given the processes taking place in a smaller dimensions; the complete advantages of PCA are listed below:

- 1) Lack of redundancy of data given the orthogonal components [19, 20].
- 2) Reduced complexity in images’ grouping with the use of PCA [19, 20]
- 3) Smaller database representation since only the trainee images are stored in the form of their projections on a reduced basis [19].
- 4) Reduction of noise since the maximum variation

basis is chosen and so the small variations in the background are ignored automatically [19].

Table 1. The features of PCA are shown in the table below [18].

Feature	Principal component analysis
Discrimination between classes	PCA manages the entire data for the principal components analysis without taking into consideration the fundamental class structure.
Applications	PCA applications in the significant fields of criminal investigation are beneficial
Computation for large datasets	PCA does not require large computations
Direction of maximum discrimination	The directions of the maximum discrimination are not the same as the directions of maximum variance as it is not required to utilize the class information such as the within class scatter and between class scatter
Focus	PCA examines the directions that have widest variations
Supervised learning technique	PCA is an unsupervised technique.
Well distributed classes in small datasets	PCA is not as powerful as other methods.

Two key disadvantages of PCA are:

- 1) The covariance matrix is difficult to be evaluated in an accurate manner [19].
- 2) Even the simplest invariance could not be captured by the PCA unless the training data explicitly provides this information [4].

5. Conclusions

The PCA method is an unsupervised technique of learning that is mostly suitable for databases that contain images with no class labels. A detailed description of the PCA technique utilizing in face recognition has been provided. As mentioned above, the PCA method’s advantages and disadvantages have also been explained in this study.

6. Acknowledgment

The work we presented in this paper has been supported by the University Technology Malaysia.

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