

Development of a Simulation-Based Intelligent Decision Support System for the Adaptive Real-Time Control of Flexible Manufacturing Systems

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Received April 25th, 2010; revised May 19th, 2010; accepted May 27th, 2010.

ABSTRACT

This paper describes a simulation-based intelligent decision support system (IDSS) for real time control of a flexible manufacturing system (FMS) with machine and tool flexibility. The manufacturing processes involved in FMS are complicated since each operation may be done by several machining centers. The system design approach is built around the theory of dynamic supervisory control based on a rule-based expert system. The paper considers flexibility in operation assignment and scheduling of multi-purpose machining centers which have different tools with their own efficiency. The architecture of the proposed controller consists of a simulator module coordinated with an IDSS via a real time event handler for implementing inter-process synchronization. The controller's performance is validated by benchmark test problem.

Keywords: *Intelligent Decision Support System, Real Time Control, Flexible Manufacturing System, Multi-Purpose Machining Centers*

1. Introduction

A flexible manufacturing system (FMS) architecture can be characterized as a set of multi-purpose machine tools connected by automatic material handling and tool transportation devices. The material handling system has a mechanism to transport parts between machining centers. Automatic tool transportation devices can also transfer tools among tool magazines and the central tool storage area [1,2]. Any material handling system has a mechanism to transport parts and tools automatically. These systems can transfer tools among tool magazines and the central tool storage area while the system is in operation [3,4]. FMSs are essentially more flexible than the conventional manufacturing systems, mainly because of utilizing versatile manufacturing lines, redundant and reconfigurable machines, alternate routings, and flexibility in operation sequencing [5,6].

Due to different operations on a product and machine requirements to process each step of production, it is so hard to control different events that might happened at

different cells to achieve best practice of performance criteria [7]. Regarding these considerations, control of these environments plays an essential role at manufacturing systems. Control framework has been studied on FMSs in the literature and there are different methods for selecting the most appropriate control policies at each decision point [8-15]. These strategies deal with the allocation of jobs to multi-purpose machining centers which have to be made in a flexible way. Most of these studies focus on reactive strategies that enable the FMS to better deal with randomness and variability. It means that most of these FMS controllers usually use fixed and offline policies to operate the system. However, these methods do not consider many realistic constraints and dynamic changes such as tool magazine capacity, operative efficiency changes and availability of tools in the part selection and operation assignment problems. These offline methods are mainly categorized into two forms: priori reactive control and the posteriori reactive control methods. The control is planned according to the structural information, forecasts, orders, management rules

and objectives [16]. The online posteriori control adapted directly to the system for preventive deviations by controlling occurrence of events.

Improving the performance of an FMS supervised by an effective controller is still a complex task that not only is time consuming but also needs much human expertise in decision making [17]. In order to implement an adaptive controller, DSS have become an effective method for their adaptability in controlling complex and dynamic operations [18]. There have been limited investigations on IDSS for controlling such systems as a unified approach. There is a need to construct a framework in which a knowledge-based decision analysis will assist the decision process to improve the FMS control parameters.

An effective approach for reinforcement of IDSS performance is to develop an embedded simulation model that meets the desired objectives of the system [19-22]. Discrete-event simulation is a very powerful tool that can be used to evaluate alternative control policies in the manufacturing system [23-26]. Although the procedure of analyzing simulation results could rely on various guidelines and rules, decision-making still requires significant human expertise and computer resources. To efficiently use simulation in the decision process, integration of IDSS with simulation has been emphasized [27-30]. However, there have been limited investigations on integrating IDSS with the modular simulation languages as a unified approach for controlling manufacturing systems. So FMS control appears to be an excellent area for applying adaptive IDSS simulation-based controller.

This research focuses on developing a simulation-based intelligent expert system with dynamic rules contemplating tool and machine flexibility control. For implementing inter-process synchronization in real-time control of FMS, the proposed IDSS receives online results from simulation module and different scenarios of control parameters with simulation replication action. The outline of the paper is as follows. Section 2 describes adaptive flexibility control on FMS shop floor. Section 3 deals with FMS adaptive controller architecture to build IDSS. Sections 4 present experimental study to validate the effectiveness of the proposed system. Finally, conclusions are made in Section 5.

2. Adaptive Flexibility Control on FMS Shop Floor

2.1 Adaptive Control Mechanism

Adaptive supervisory implies selection of an appropriate control policy based on the current state of the workcell. Regarding dynamic control of manufacturing systems, jobs are dispatched to machining centers using dispatch-

ing rules at the specific moment based on the available information. Afterwards, appropriate tool is mounted in machining center according to the tooling strategy [31]. Because of the flexible characteristics of FMSs, control decisions should be applied as soon as possible based on the real time state of the system. An FMS adaptive controller has to deal with the dynamic environment in which the system operates to seize online machines and tools redundancy capabilities, alternative routing and hazard control remedy.

2.2 FMS Shop Floor Flexibility Control Functions

The most commonly accepted definition of flexibility is the ability to take up different positions or alternatively the ability to adopt a range of states [32]. Many different authors have defined many different types of flexibilities (machine, process, product, operation, routing, volume, production and expansion flexibility) in the literature [33-37]. Here we consider the flexibility control function as machine flexibility and tool flexibility. Browne *et al.* [38] defined machine flexibility as the ease of change to process a given set of part types. Buzacott [39] clarifies machine flexibility as the ability of the system to cope with changes. There are three technical constraints related to a machining center: number and capacity of machine-tools, local input/output buffer (LIB/LOB) size and operative efficiency. Das and Nagendra [40] define machine flexibility of a machining center as the ability of performing more than one type of processing operation efficiently. Therefore, machine flexibility is measured by the number of operations that a workstation processes and the time needed to switch from one operation to another. The more operations a workstation processes and the less time switching takes, the higher the machine flexibility becomes [37]. **Figure 1** shows the proposed adaptive flexibility control functions of the FMS shop floor.

As illustrated in **Figure 1**, tool flexibility can be defined as getting the right tool, to the right place at the right time [34,41]. The need for tooling strategies originates from the high variety and number of cutting tools that are typically found in automated manufacturing systems. The adoption of appropriate tool management policies that consider alternative tools allows the desired part mix and quantities to be manufactured efficiently while achieving improved performance [42]. At machine tool level, there are two technical constraints related to tool allocation: tool magazine capacity and tool life. Due to tool magazine capacity, there is a restriction on the number of operations that can be processed in a single tool setup. On the other hand, if tools can be loaded and unloaded while the machine is running, the capacity of the tool magazine can be assumed to be unlimited [32,43].

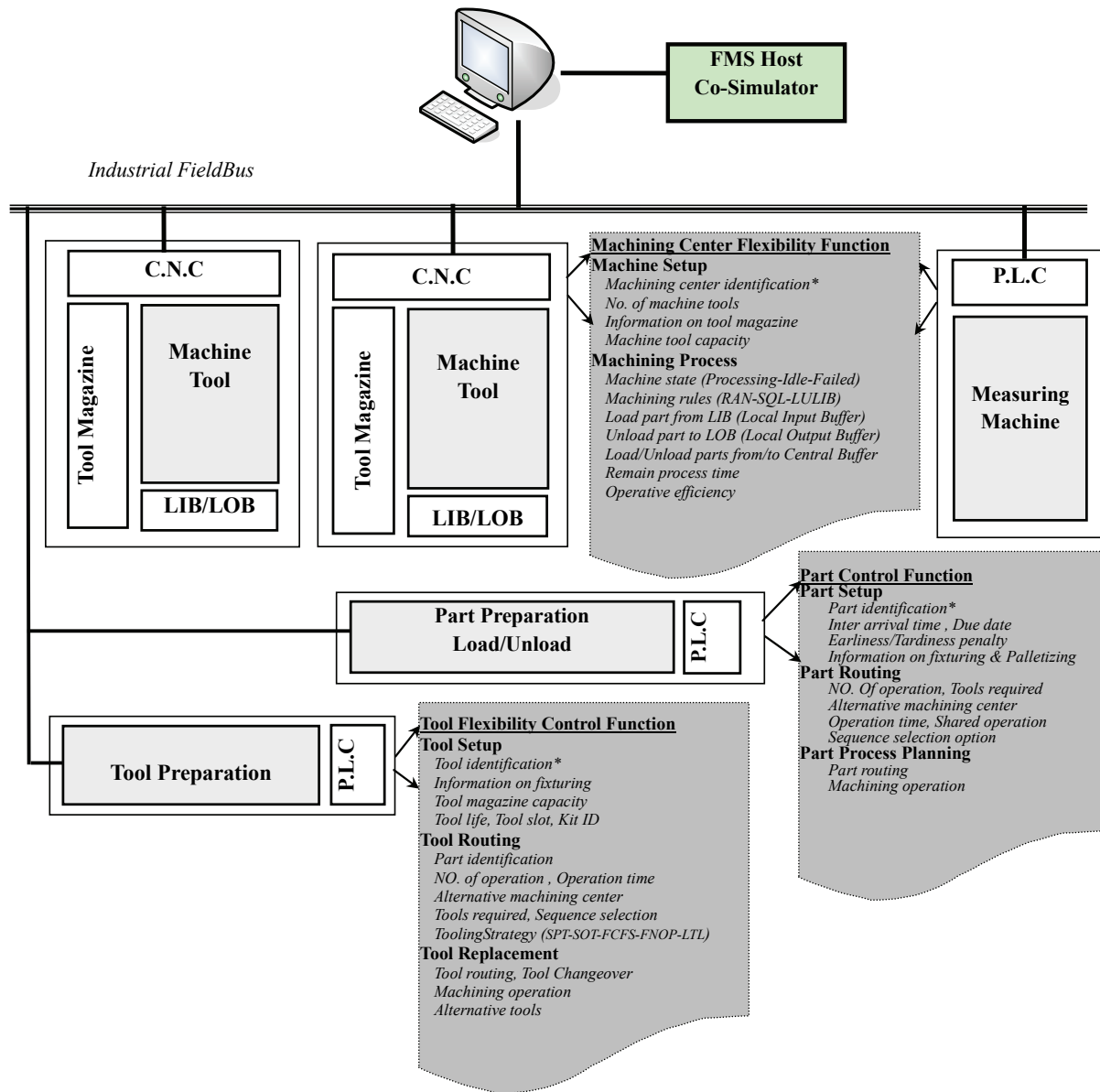


Figure 1. FMS shop floor flexibility control functions

The tool magazine capacity is an influential factor in determining the flexibility of the system. A proper tool management is needed to control processing of parts and enhance the flexibility to variety of parts. It is important to design a tool management control function so that the proper tools are available at the right machine at the desired time for processing of scheduled parts.

The work-order processing and part control system essentially drives other control functions. This module concerns the determination of a subset of part types from a set of part types for processing.

A number of criteria can be used for selecting a set of part types for processing (*i.e.* due date, inter arrival time,

requirement of tools, operation time, shared operation, operations sequence).

3. FMS Adaptive Controller Architecture

3.1 FMS Configuration Parameters

The following notations and criteria are utilized in developing the rule-based model of the FMS controller addressed in this research. **Table 1** represents the notations.

These parameters are defined in such a way that contains information about the previous control functions on a platform of multi-purpose machines. In other words, definition of these parameters considers machine and tool

Table 1. FMS configuration parameters and performance criteria

FMS configuration parameters			
Notation	Definition	Notation	Definition
P_i	i -th production order, $1 \leq i \leq p$	OE_{ijkl}	Operative efficiency of O_{ij} on M_{kl}
O_{ij}	j -th operation of order P_i , $1 \leq j \leq n_i$	DD_{P_i}	Due date of P_i
M/C_k	k -th machining centers, $1 \leq k \leq m$	T_{ij}	Time for processing operation O_{ij}
M_{kl}	l -th machine of M/C_k , $1 \leq l \leq L_k$	α_i	Penalty weight for P_i when ACT_i is less than DD_{P_i}
IAT_i	inter arrival time between P_i and P_{i-1}	β_i	Penalty weight for P_i when ACT_i is greater than DD_{P_i}
TMC_{kl}	Tool magazine capacity of M_{kl}	n_i	The number of P_i operations.
TL_{hkl}	Tool life of h -th tool of M_{kl} (time based)	RE_i	The number of operation remain to complete P_i
TM_{hkl}	h -th tool of M_{kl} tool magazine	$MinU$	Minimum utilization
MS_{ij}	Set of machines which can handle O_{ij}	$MaxU$	Maximum utilization
LIB_{kl}	Local input buffer size of M_{kl}	ST_{ij}	Standard time of O_{ij} with 100% operative efficiency
LOB_{kl}	Local output buffer size of M_{kl}	TP	Throughput
PTH	Duration of planning time horizon	RTO_{ij}	Number of required Tool for O_{ij}
t	Current time	ETT_{ij}	Elapsed time between O_{ij} and its latter operation
Simulator outputs performance criteria			
Notation	Definition	Notation	Definition
TBD_{kl}	Time between departures on M_{kl}	TIT_{kl}	Total idle time of M_{kl}
ACT_i	Actual cycle time of order P_i	TWT_i	Total waiting time of P_i
Z_i	Total penalty of P_i	MU_{kl}	Machine M_{kl} utilization
$OS_i(t)$	Set of operations of P_i processed until t	$OS_{kl}(t)$	Set of operations processed on M_{kl} until t
QM_{kl}	Queue size of M_{kl}	CT_{kl}	Completion time in M_{kl}
TU_{hkl}	Tool usage of h -th tool of M_{kl} (time based)	BU_{kl}	Buffer usage of M_{kl}

Table 2. Binary control flags

Variable	Definition	Variable	Definition
OA_{ijkl}	Equal to 1 if O_{ij} is assigned to M_{kl} , otherwise it is equal to 0	MIU_{kl}	Equal to 1 if machine M_{kl} is in use; otherwise it is equal to 0
TML_{hijkl}	Equal to 1 if TM_{hkl} load to perform O_{ij} on M_{kl} and equal to 0 if unloads RTM_h	BSA_{kl}	Equal to 1 if buffer space of M_{kl} is available; otherwise it is equal to 0
PC_i	Equal to 1 if P_i complete otherwise it is equal to 0	MB_{kl}	Equal to 1 if machine M_{kl} is bottleneck; otherwise it is equal to 0
λ_i	Equal to 1 if ACT_i is less than DD_{P_i} , otherwise it is equal to 0	OD_{ijkl}	Equal to 1 if O_{ij} is done on M_{kl} , and depart it; otherwise it is equal to 0
APO_i	Equal to 1 if P_i should be scheduled next otherwise it is equal to 0	PA_i	Equal to 1 if P_i arrive otherwise it is equal to 0
OW_{ij}	Equal to 1 if O_{ij} is waiting for process; otherwise it is equal to 0		

flexibility characteristics of an FMS. **Table 2** shows the binary control flags (BCF's).

3.2 Simulation-Based Intelligent Decision Support System

Figure 2 shows the combination between simulation and intelligent decision support system as for FMS adaptive control. The figure shows the cooperation between IDSS and the simulator module. The current configuration parameters of the FMS are read by user interface and are used as the input data to build conceptual model. The simulation model will evaluate the current shop performance, such as actual cycle time, tool and buffer utilization. This process continues until a satisfying and controllable shop floor configuration is reached.

The system presents details of the architecture, components and functions of a FMS decision-making controller. The proposed controller consists of a simulator model coordinate rule based IDSS with a real time mechanism. The simulation output data are fed to the knowledge-based system as input data. The rule-based IDSS analyzes output of simulation model to control the real-time status of FMS. Once the IDSS makes recommendations, the simulation model is adjusted accordingly and the process is repeated. The simulation and IDSS components cooperate with each other until the control goals are achieved. Since the primary objective is to improve the throughput of the shop floor, a simulation analysis assisted by decision process is carried out. The status of the cell, machines, part orders, the availability

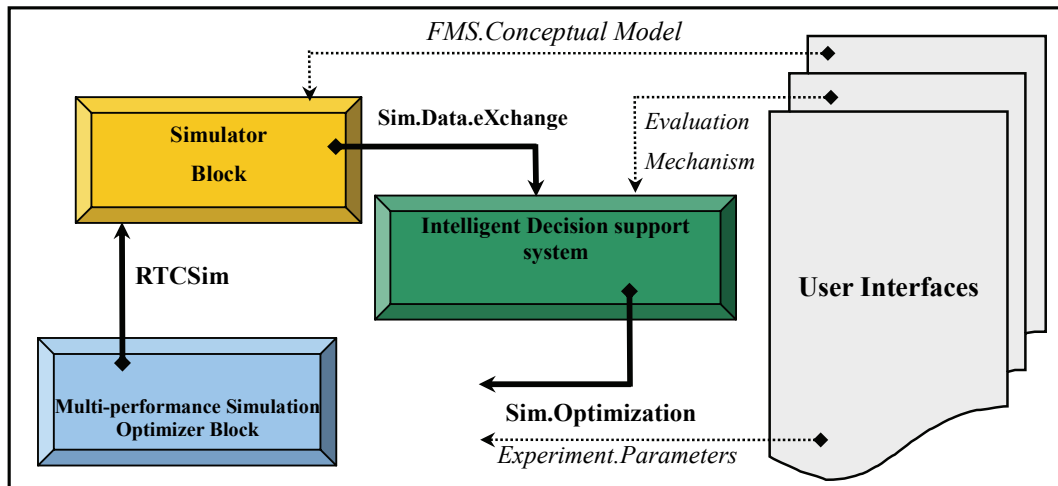


Figure 2. The structure of simulation-based IDSS for FMS adaptive control

of operators and system control flags are recorded in separate databases. Sequence of jobs is used to control the flow of parts through the system. The first step to estimate the performance criteria is assigning the operations to machines and scheduling the operations on each machine.

The above posteriori adaptive control mechanism employs a simulator block to predict different performance criteria of the FMS conceptual model. The simulator contains the discrete event simulation model and is able to measure several FMS performance criteria depending on the different inputs. The simulation results are then forwarded between external interfaces belonging to different external models. On the other hand, these interfaces han-

dle the necessary communications with the simulation and coordinate IDSS control signal transformations into the simulator.

Sequence of jobs is used to control the flow of parts through the system. The first step to estimate the performance criteria of FMS is assigning the operations O_{ij} to machining centers and extracting the set $OSM_{kl}(t)$ includes operations processed on M/C_k until t . The real time adaptive control framework is based on affiliating all current events and expected future event to a time tag for process synchronization. The following pseudo-code shows the initialization phase of the simulation in order to configure the FMS conceptual model.

The initialization phase should be run in execution

```

FMSConfigParam()
  Read Number of parts, machining centers and planning horizon (p,m,PTH);
  For i: = 1 to p Read Number of parts operations and due date (ni, DDPi, IATi, αi, βi);
  For k: = 1 to m Read Number of machines at each machining centers (Lk);
  For k: = 1 to m initialize Machining Centers Resources M/Ck, Capacity;
  For k: = 1 to m
  For l: = 1 to Lk initialize Machine Tools, Tool magazine and buffers (MTkl, TMCkl, LIBkl, LOBkl);
  For i: = 1 to p
  For j: = 1 to ni
    Initialize queue used to hold part operations (Oij (Process.Queue));
    Read (processing time of each operation (Oij, Tij, STij, MSij, ETTij, RTOij);
  InitTime(t); (Initialize simulation current time)
  RealTimeInitialize(t); (Initialize inter-process synchronization)
    
```

mode using the function $RealTimeInitialize(t)$ to synchronize simulation logic with an external process of FMS controller system. The module $RTCSim(t)$ represents FMS events simulation to handle machine and tool flexibility.

The simulation clock is set to the real-time clock of the operating FMS system and all other simulation processes

are initiated by $InitProcess(O_{ij})$. Because of the randomness of processing times in each replication, the expectations of system outputs are estimated by sample means. The function $TAVG(ACT_i, TU_{hkl}, BU_{kl})$ records the values of system outputs throughout each replication and finally estimates the expectation of these statistics

RTCSim(t):

```

RealTimeRecieve(t);
  (Receive real-time actions from the DSS and passes them to simulator)
Let NREP:= 0;(simulation optimization level)
Let REPNum:= 0;(replications per simulation counter)
While REPNum < MaxREP ; (Maximum simulation replications)
  For i:= 1 to p
    Create (Pi) ; (parts entry in the simulation model)
    Set APOi= 1, OSi(t)= φ ; (Pi should be processed next)
    For j:= 1 to ni ∉ OS(t) (for remaining operations)
      Set OWij= 1; (operation Oij is waiting for process)
      For k:= 1 to m
        Machine flexibility
        For l:= 1 to Lk
          Read OEijkl; (operative efficiency of Oij on MTkl)
          DR.Select(t); (select dispatching rule from DSS)
          RVG (T(Oijkl)); (random value generator of processing time)
          InitProcess(Oij) (beginning of the simulation replication)
          TAVG (CTkl, TBDkl, ITkl, QMkl, BUkl, MUkl, TITkl)
          (records the tally variable throughout this replication)
          Return TFIN; (final simulation time)
          REPNum:= REPNum + 1; (increment replication number)
        }; //end InitProcess
      //end While
    ShutdownIPS; (terminate the simulation replication)
  DAVG (Ê[ACTi], Ê[Zi], Ê[TWTi]);
  (Return the average of time-persistent statistics throughout all replications)

```

InitProcess(O_{ij}):

```

While OWij= 1 do (Oij is waiting for process)
  {WriteIPSQueue(Oij);
  For h:= 1 to TMCkl Tool flexibility
    Read TLhkl;
    (Tool life of h-th tool of MTkl)
    TS.Select(t);
    (Tooling strategy from DSS)
    Load TMhkl;
    (h-th tool of MTkl tool magazine)
    Assign Oij ;
    (Process.NumberIn) ;
    Assign Oij (Process.LIBkl) ;
    Seize Oij (Process.Queue);
    Delay τij (Time (kl) );
    Set OAijkl= 1, MIUkl= 1;
    Dispose (P, LOBkl);
    Release M/Ckl;
    Set ODijkl= 1, APOi= 0, OWij= 0;
    Update OS(t), REi, ACTi;
  Return Flags (OAijkl, PCij, TMLhkl);
  //end While

```

through the average function $DAVG(\hat{E}[ACT_i], \hat{E}[TU_{hkl}], \hat{E}[BU_{kl}])$ over $MaxREP$ simulation replications. The number of replications per simulation ($MaxREP$) should be set to the minimum number necessary to obtain a reliable estimate of performance criteria.

Based on the results obtained at each level of optimization ($NREP$) and exchanging them with IDSS, additional number of replications may be re-simulated for each design. The expected value of FMS performance criteria are extracted under design $\bar{\rho}_{ijkl}, \bar{O}_{ijkl}$. The $\hat{E}[ACT_i | \bar{\rho}_{ijkl}, \bar{O}_{ijkl}]$, $\hat{E}[TU_{hkl} | \bar{\rho}_{ijkl}, \bar{O}_{ijkl}]$, $\hat{E}[BU_{kl} | \bar{\rho}_{ijkl}, \bar{O}_{ijkl}]$ represent the stochastic effects of system output by sample mean. The ultimate goal is to find the solution that optimizes the value of these performance criteria. The optimization procedure uses the outputs from the simulation model of previous $NREP$ to construct a response surface at each simulation optimization level of $\bar{\rho}_{ijkl}, \bar{O}_{ijkl} |_{NREP=r}$ and to extract the next level of $\bar{\rho}_{ijkl}, \bar{O}_{ijkl}$ as an input to the model.

To control the external processes of FMS, the simulator block and IDSS are synchronized via simulation data exchange $Sim.Data.eXchange(IDSS)$. The IDSS analyzes outputs of simulation model to control the real-time status of FMS after receiving these results by $RealTimeSend()$ function. The IDSS then sends appropriate control signals of beginning operation to the corresponding entities when an event is occurred. Proposing the

adaptive controller with this structure allows modeling of synchronization mechanism between FMS entities and transmission times for messages exchanged between the IDSS and simulator.

Figure 3 schematically describes the inter-process synchronization between different components of co-simulator. The approach for adaptive controller designing is built around the theory of supervisory control based on exchanging simulation outputs with an event-condition-action real time system. The proposed system uses a posteriori adaptive control mechanism that also is an online control method acting after the event occurs versus such popular reactive control method.

The simulator can trigger the rule-based IDSS to generate the appropriate control policy. The simulator block sends messages to the external rule-based system to indicate simulated results from FMS by $RealTimeSend()$. The rule-based IDSS interprets these results and sends appropriate action messages back to the simulator and user to indicate the instructions to be done.

3.3 Rule Production for FMS Real Time Simulation-Based Controller

The IDSS collect the facts into appropriate data base using $CollectFact()$, which is then used for inference by simulation outputs in feed forwarding reasoning. The control framework is implemented by integration of the adaptive control rules and real time simulator for enforcing dynamic strategies of FMS shop floor control. In order to strengthen the expert system reasoning, knowledge-elic-

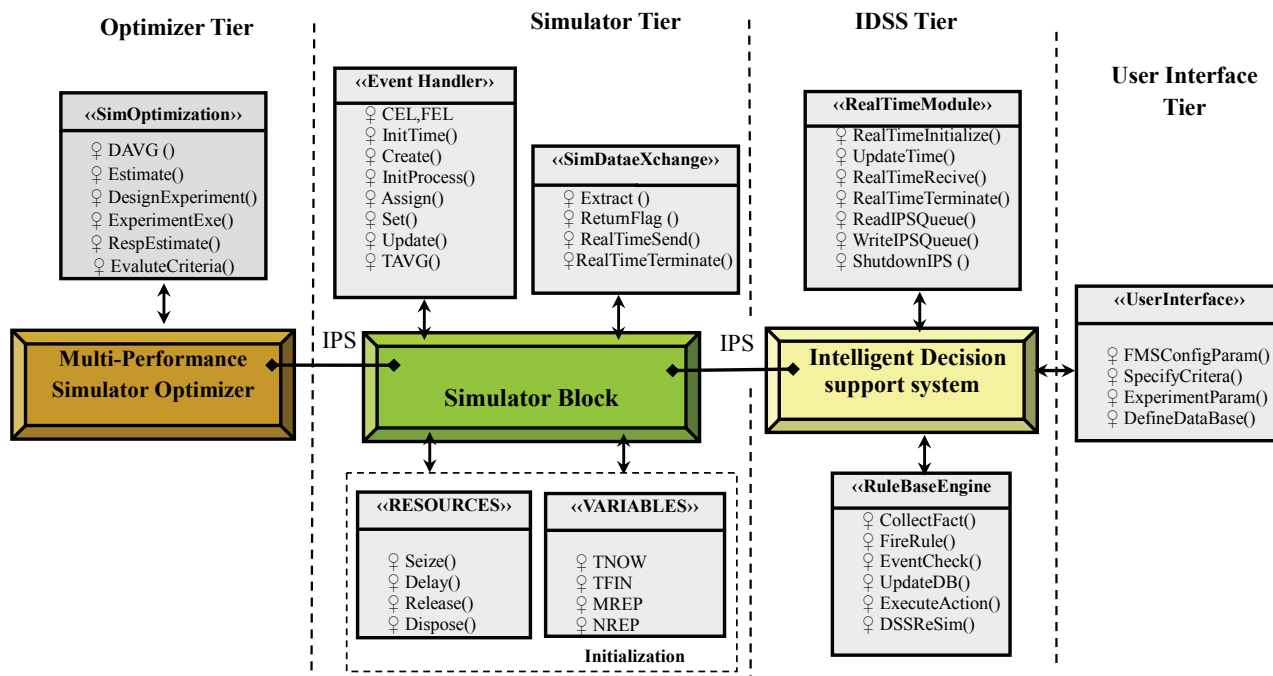


Figure 3. Real time simulation data exchange via inter-process synchronization

tation techniques are used for preventing ineffective redundancy at concurrent firing of rules and high degree of parallelism. This knowledge-based IDSS is aimed at providing a powerful control on different operations of FMS. It acts as a cell manager which may work alongside the operating cell-oriented part and tool management system. These sections describe the knowledge representation through a set of control rules. Design of IDSS controller focuses on the development of appropriate Event-Condition-Action (ECA) rules for tuning control parameters. These rules are formulated by the techniques of data gathering and knowledge elicitation to construct IDSS. The IDSS is able to obtain feedback results from the on-line system of simulator. These results are very significant and let the expert system to re-simulate if the performance criteria are not desirable.

The rules applied in this paper are structured in the following form and consist of three segments: event type, condition and action:

When $\langle \underline{Event}_1, Event_2, Event_3, \dots \rangle$
If $\langle \underline{Condition}_1, Condition_2, Condition_3, \dots \rangle$
Then $\langle \underline{Action}_1, Action_2, Action_3, \dots \rangle$

Event type: This tag specifies that analysis of condition should be done once the events take place.

Condition: This segment of ECA rules specifies a list of conditions. In order to trigger an action rule, all conditions should be satisfied. These conditions refer to a logical assertion of the FMS states extracted by the simulator module $RTCSim(t)$.

Action: This segment specifies actions which may consist of a list of operations. Whenever an action rule is triggered by an event, the operations being in its action list will be initiated sequentially. The proposed rule-based system for manufacturing execution system provides the parts sequence list to the multi-purpose machines available and then the operation assignment and task proportions of parts on related machines. The output can be manipulated by changing the rules and strategies entered at the expert system query stage. **Table 3** illustrates MES control function about dispatching rules.

For each part P_i the slack index is defined as:

$$Slack_i = DD_{P_i} - \sum_{j=1}^{n_i} ST_{ij} - t, \forall i. \text{ The function } Sort(array)$$

finds the maximum or minimum value in the array and the binary flag APO_i specifies the next scheduled part. **Table 4** illustrates MES control function for machining rules in the FMS.

The binary flag OA_{ijkl} specifies the assignment of operation O_{ij} to machine M_{kl} . **Table 5** illustrates MES control function for tooling strategy in the FMS.

Operative efficiency of doing operation O_{ij} on M_{kl} is defined as OE_{ijkl} and thus tool usage can be considered as $TU_{hkl} = T_{ij} \times (1 + OE_{ijkl}), \forall h, k, l$. For each executable operation O_{ij} , the proportion of O_{ij} performed on M_{kl} is denoted as $\rho_{ijkl}(t)$, $0 \leq \rho_{ijkl} \leq 1$. IDSS monitors all events and states transition of FMS by considering ρ_{ijkl} to

Table 3. MES control function (dispatching rules)

MES Control Function: Dispatching Rules			
Dispatching Rule	When [Event]	If (Condition)	Action
Shortest Processing Time	$t \neq 0$ RealTimeRecieve()	$DR.Select(t) = SPT$	$Sort(ST_{ij}) \forall i \forall j; APO_i = 1;$
First Come First Serve	$t \neq 0$ RealTimeRecieve()	$DR.Select(t) = FCFS$	$Sort(IAT_i) \forall i; APO_i = 1;$
Operation with Least Slack	$t \neq 0$ RealTimeRecieve()	$DR.Select(t) = SLACK$ $PC_i = 0 \ \&\& \ Slack_i < 0$	$Sort(Slack_i) \forall i; APO_i = 1;$
Slack Per Remaining Work	$t \neq 0$ RealTimeRecieve()	$DR.Select(t) = S / RMOP$ $PC_i = 0 \ \&\& \ Slack_i < 0$	$Sort(Slack_i / RE_i) \forall i \forall j; APO_i = 1;$
Slack Per Remaining Work	$t \neq 0$ RealTimeRecieve()	$DR.Select(t) = S / RMWK$ $PC_i = 0 \ \&\& \ Slack_i < 0$	$Sort(Slack_i / \sum_j ST_{ij}) \forall i \forall j; APO_i = 1;$
Earliest Due Date	$t \neq 0$ RealTimeRecieve()	$DR.Select(t) = EDD$	$Sort(DD_{P_i}) \forall i; APO_i = 1;$

Table 4. MES control function (machining rules)

MES Control Function: Machining Rules			
Machining Rule	When [Event]	If (Condition)	Action
Random Selection	$t \neq 0$ RealTimeRecieve()	$MR.Select(t) = RAN$ $APO_i = 1$	$Sort(Rand M_{kl}) \forall k \forall l; OA_{ijkl} = 1;$
Shortest Queue Length	$t \neq 0$ RealTimeRecieve()	$MR.Select(t) = SQL$ $APO_i = 1$	$Sort(QM_{kl}) \forall k \forall l; OA_{ijkl} = 1;$
Lowest Utilized Buffers	$t \neq 0$ RealTimeRecieve()	$MR.Select(t) = LUB$ $APO_i = 1$	$Sort(BU_{kl}) \forall k \forall l; OA_{ijkl} = 1;$

Table 5. MES control function (tooling strategy)

MES Control Function: Tooling Strategy			
Tooling Strategy =TS	When [Event]	If (Condition)	Action
Shortest Operation Time	$t \neq 0$ RealTimeRecieve()	$TS.Select(t) = SOT$ $OA_{ijkl} = 1$	$Sort(ST_{ij}) \forall i \forall j; AssignTool(TM_{hkl}, O_{ij}) \forall i \forall j;$ $UpdateToolMag(M_{kl});$
Shortest Processing Time	$t \neq 0$ RealTimeRecieve()	$TS.Select(t) = SPT$ $OA_{ijkl} = 1$	$Sort(DD_{P_i}) \forall i; AssignTool(TM_{hkl}, P_i) \forall i;$ $UpdateToolMag(M_{kl});$
First Come First Serve	$t \neq 0$ RealTimeRecieve()	$TS.Select(t) = FDFS$ $OA_{ijkl} = 1$	$Sort(IAT_i) \forall i; AssignTool(TM_{hkl}, P_i) \forall i \forall j;$ $UpdateToolMag(M_{kl});$

dynamically rebuild new configuration and replicate simulation module $RTCSim(t)$. **Table 6** contains the rules for control of transition of different states in FMS, bottleneck detection and resolving, assigning operation to a non-bottleneck machining centers.

For each part P_i actual cycle time is defined as: $ACT_i = \sum_{j \in OS_{kl}} \left(ETT_{ij} + \frac{\rho_{ijkl} \times ST_{ij}}{OE_{ijkl}} \right)$ and the penalty is defined as:

$$Z_i = \sum_{i=1}^p [\alpha_i \lambda_i (DD_{P_i} - ACT_i) + \beta_i (1 - \lambda_i) (ACT_i - DD_{P_i})]$$

4. Experimental Study

The problem presented has been adopted in this paper to validate the proposed method by Sarin and Chen [43]. The model presents machine loading and tool allocation problem in FMS with tool life and magazine capacity. The FMS model includes tool and machine alternatives. The experiment was done on a FMS with four machining centers. **Tables 7** and **8** show tool-operation and machine-tool compatibility.

Table 9 represents the machining time of operations on alternative tools.

Table 6. MES control function

MES Control Function: States, Bottleneck, Assigning		
When [Event]	If (Condition)	Action
$t \neq 0$ $PA_i = 1; \forall i$	$MIU_{kl} = 0; \forall k, l$	<i>Initialization(initial config. parameters);</i> <i>DefineDB(); SpecifyCriteria(); RTCSim(t);</i> <i>UpdateTime(t); SimDataeXchange(IDSS);</i>
$t \neq 0$ <i>ReadIPSQueue(O_{ij})</i>	$MB_{kl} = 0; \exists k, l, PA_i = 1$	<i>RealTimeRecieve (OS_{kl}(t), OS_i(t), $\rho_{ijkl}(t)$, BCF);</i>
$t \neq 0$ <i>ReadIPSQueue(O_{ij})</i>	$MIU_{kl} = 1; \forall k, l \quad BSA_{kl} = 0; PC_i = 0$	<i>RealTimeRecieve (OS_{kl}(t), OS_i(t), $\rho_{ijkl}(t)$, BCF);</i> <i>UpdateTime(t);</i>
$t \neq 0$ <i>ReadIPSQueue(O_{ij})</i>	$MIU_{kl} = 0; \exists k, l \quad BSA_{kl} = 1$ $OA_{ijkl} = 1; \forall j \notin OS_i(t); PC_i = 0$	$MIU_{kl} = 1;$ <i>RealTimeRecieve (OS_{kl}(t), OS_i(t), $\rho_{ijkl}(t)$, BCF);</i> <i>UpdateTime(t);</i>
$t \neq 0$ <i>ReadIPSQueue(O_{ij})</i>	$MIU_{kl} = 0; \exists k, l \quad BSA_{kl} = 0; PC_i = 0$	<i>RealTimeRecieve (OS_{kl}(t), OS_i(t), $\rho_{ijkl}(t)$, BCF);</i> <i>UpdateTime(t);</i>
$t \neq 0$ <i>RealTimeRecieve()</i>	$n[OS_{kl}(t)] > (\sum_{i=1}^p n_i) / L_k; \exists k, l$	$MB_{kl} = 1$
$t \neq 0$ <i>RealTimeRecieve()</i>	$TBD_{kl} > (PTH / MinU); \forall k, MIU_{kl} = 1$	$MB_{kl} = 1$
$t \neq 0$ <i>RealTimeRecieve()</i>	$[(TBD_{kl} > TBD_{k(l-1)}) \& (U_{kl} < U_{k(l-1)})]$ $MIU_{kl} = 1$	$MB_{kl} = 1$
$t \neq 0$ <i>RealTimeRecieve()</i>	$MU_{kl} < MinU; \forall k, l \quad MIU_{kl} = 1$	$MB_{kl} = 1$
$t \neq 0$ <i>RealTimeRecieve()</i>	$MB_{kl} = 0 \& MIU_{kl} = 0; \exists k, l$ $OA_{ijkl} = 1; \forall j \notin OS_i(t)$	$MIU_{kl} = 1;$ <i>RealTimeSend (OS_{kl}(t), OS_i(t), $\rho_{ijkl}(t)$, BCF);</i> <i>UpdateTime(t); SimDataeXchange(IDSS);</i>
$t \neq 0$ <i>RealTimeRecieve()</i>	$PC_i = 0; \forall i$ $MB_{kl} = 1$	$OA_{ijkl} = 1; \forall l' \neq l$ <i>RealTimeSend (OS_{kl}(t), OS_i(t), $\rho_{ijkl}(t)$, BCF);</i> <i>UpdateTime(t); SimDataeXchange (IDSS);</i>
$t \neq 0$ <i>RealTimeRecieve()</i>	$(MU_{kl} < MU_{k'l'}; \exists k, k', l, l') \parallel (MU_{kl} < MinU);$ $MU_{kl} = MU_{k'l'} = 0; \exists k, k', l, l'; PC_i = 0$	$OA_{ijkl} = 1; \forall j \notin OS_i(t); MIU_{kl} = 1$ <i>RealTimeSend (OS_{kl}(t), OS_i(t), $\rho_{ijkl}(t)$, BCF);</i> <i>UpdateTime(t); SimDataeXchange(IDSS);</i>

States transition control rules

Bottleneck detection

Assigning operation to non-bottleneck

Table 7. Tool-operation compatibility

Part/Tool	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
P ₁	O ₁₁	1	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	O ₁₂	0	0	0	1	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0
	O ₁₃	0	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0
	O ₁₄	0	0	0	0	0	0	0	0	0	1	0	0	1	0	0	0	0	0	0
P ₂	O ₂₁	1	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	O ₂₂	0	0	0	0	0	0	0	1	0	0	0	0	0	0	1	0	0	0	0
	O ₂₃	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	1	0	0	0
	O ₂₄	0	0	0	1	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0
P ₃	O ₃₁	0	0	0	0	0	0	0	0	0	0	1	0	0	1	0	0	0	0	0
	O ₃₂	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	0	1	0	0
	O ₃₃	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0	0	1	0
	O ₃₄	0	0	1	0	0	0	0	0	0	0	0	0	1	0	0	0	0	0	0
P ₄	O ₄₁	0	1	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	0	0
	O ₄₂	0	0	0	0	1	0	0	0	0	0	0	0	0	0	0	0	0	0	1
	O ₄₃	0	0	0	0	0	0	0	0	0	0	0	1	1	0	0	0	0	0	0
	O ₄₄	0	0	0	0	0	1	1	0	0	0	0	0	0	0	0	0	0	0	0
Tool life	25	21	25	20	22	25	25	22	20	25	18	20	21	25	17	20	20	21	22	24

Table 8. Machine-tool compatibility

Machine/Tool	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20
M ₁₁	1	0	1	0	1	0	1	0	0	1	0	1	0	0	0	1	0	0	0	0
M ₂₁	1	0	1	1	0	1	1	0	0	1	1	0	0	1	0	0	0	0	1	1
M ₃₁	0	1	0	1	0	1	0	1	1	0	0	1	0	0	0	0	1	0	0	0
M ₄₁	0	0	0	0	1	0	0	0	1	0	1	0	1	0	1	0	0	1	0	0

Table 9. Machining time on alternative tools (T_{ij}) for parts

Part No	P ₁								P ₂							
Operation No	O ₁₁		O ₁₂		O ₁₃		O ₁₄		O ₂₁		O ₂₂		O ₂₃		O ₂₄	
Tool No	1	2	4	7	6	10	13	1	3	8	16	10	17	4	12	
M ₁₁	104			68		84		114	114		25	106			96	
M ₂₁	110		120	130	110	76		126	98			66		116		
M ₃₁		101	106			118							29	112	84	
M ₄₁							100			119						
Standard Time	95	98	105	60	104	72	95	112	91	115	18	60	20	107	82	

Part No	P ₃								P ₄							
Operation No	O ₃₁		O ₃₂		O ₃₃		O ₃₄		O ₄₁		O ₄₂		O ₄₃		O ₄₄	
Tool No	12	15	9	18	11	19	3	14	2	4	5	20	13	14	7	8
M ₁₁	67						82				137				68	
M ₂₁					117	47	85	110		114		38		115	53	
M ₃₁	102		90						49	140						87
M ₄₁		134	120	40	132						118		120			
Standard Time	60	127	84	30	115	40	50	100	42	109	113	35	115	115	53	85

Table 10. Machining efficiency for parts on alternative tools

Order No	P ₁								P ₂							
Operation No	O ₁₁		O ₁₂		O ₁₃		O ₁₄		O ₂₁		O ₂₂		O ₂₃		O ₂₄	
Tool No	1	2	4	7	6	10	13	1	3	8	16	10	17	4	12	
OE ₁₁ (%)	91			88		86		98	80		70	56			85	
OE ₂₁ (%)	86		88	46	95	95		89	93			91		91		
OE ₃₁ (%)		97	99			88							69	95	98	
OE ₄₁ (%)							95			96						
Standard Time	95	98	105	60	104	72	95	112	91	115	18	60	20	107	82	

Order No	P ₃								P ₄							
Operation No	O ₃₁		O ₃₂		O ₃₃		O ₃₄		O ₄₁		O ₄₂		O ₄₃		O ₄₄	
Tool No	12	15	9	18	11	19	3	14	2	4	5	20	13	14	7	8
OE ₁₁ (%)	90						61				82				78	
OE ₂₁ (%)					98	85	59	91		96		92		100	100	
OE ₃₁ (%)	59		93						86	78						98
OE ₄₁ (%)		95	70	75	87						96		96			
Standard Time	60	127	84	30	115	40	50	100	42	109	113	35	115	115	53	85

Table 11. Operation assignment and task proportion (ρ_{ijkl}) and tool load

Part/Machine	M ₁₁	M ₂₁	M ₃₁	M ₄₁
P ₁	O ₁₁	0.27 (1)		0.73 (2)
	O ₁₂	0.81 (7)		0.19 (4)
	O ₁₃		0.78 (6)	0.22 (6)
	O ₁₄	0.12 (10)	0.88 (10)	
P ₂	O ₂₁	0.89 (1)	0.11 (3)	
	O ₂₂	0.79 (16)		0.21 (8)
	O ₂₃		0.75 (10)	0.25 (17)
	O ₂₄	0.22 (12)		0.78 (12)
P ₃	O ₃₁	0.91 (12)		0.09 (12)
	O ₃₂			0.79 (9)
	O ₃₃		1 (19)	
P ₄	O ₃₄	0.35 (3)	0.65 (14)	
	O ₄₁		0.66 (4)	0.34 (2)
	O ₄₂		0.48 (20)	
	O ₄₃		1 (12)	0.52 (5)
	O ₄₄	0.45 (7)	0.33 (7)	0.22 (8)

Table 12. Difference between the proposed method and the heuristic method of [43]

	Total Actual Cycle Time	Total Idle Time	Total Time between Departure	Total Waiting Time	Penalty
Proposed system	2703	441	35	127	48.5
Classis mathematical method	3108	731	63	463	154
					(Earliness)
					(Tardiness)

Table 13. Statistical analysis of difference between the proposed and mathematical method

		Actual Cycle Time	Idle Time	Time between Departure	Waiting Time
Sample Size = 384	Mean	2705.68	442.936	34.360	128.226
	StDev	16.68	9.932	2.029	10.436
	SEMean	0.85	0.507	0.104	0.533
	T-Value	-472.54	-568.36	-276.55	-628.64
	P-Value	0.000	0.000	0.000	0.000

Table 10 represents machining efficiency of operation allocation on alternative tools.

It is assumed that due date ($DD = 2800$), $\alpha_i = \beta_i = 0.5$, and $LIB_{kl} = LOB_{kl} = 15$. Tool magazine capacity and tool life are considered 20 and 100, respectively. Manufacturing execution system also includes dispatching rules (SPT), tooling strategies (FCFS) and machining rules (SQL). Table 11 shows the operation assignment and task proportion according to the rules of the proposed method.

Table 12 represents the difference of total actual cycle time, total idle time, total time between departures and total waiting time between the proposed rule-based system and the mathematical method.

The solution obtained from proposed method creates a balanced and controlled actual cycle time on machining centers. The proposed approach outperforms the heuristic method in terms of the total actual cycle time, total idle time, total time between departures and total waiting time. The proposed system presents 48.5 units of earliness penalty despite the 154 unit of tardiness penalty of mathematical method. To show the effects of difference between the proposed method outputs and classic mathematical method, statistical analysis is given as shown in Table 13.

The aforementioned results verify and validate the FMS shop floor links to the supervisory control of machine and tool flexibility. Different scenarios of performance criteria levels demonstrate effectiveness of the proposed method for the system control. The proposed method is also efficient in terms of the computation time which is highly important for the real time control of a manufacturing system. The proposed real-time simulation-based intelligent decision support system provides a real time control mechanism for improving performance of a flexible manufacturing shop floor.

5. Conclusions

This paper presents an intelligent decision support system to tackle the production control of a FMS. Development of the present knowledge-based system is aimed at integrating an ECA rule-based system and a simulator module to ease the cell adaptive supervisory control. A novel architecture of this intelligent adaptive controller prototype which is based on a real-time simulator core has been developed and presented to validate the proposed approach.

The FMS shop floor data are gathered and stored into the appropriate databases over time. The adaptive control mechanism employs a real time discrete event simulator to predict performance of the given system during the remaining time of planning horizon. The current state of the FMS performance criteria from the simulator is then stored on the appropriate databases. The proposed method provides an applicable and efficient framework for real-time control of the shop floor in flexible manufacturing system. The criteria considered to measure performance of the system shows that the proposed approach is effective and efficient in controlling shop floor. The main contributions of this paper can be summarized as follows.

- 1) Designing real time ECA rules according to feed forward reasoning with the high degree of granularity.
- 2) Reinforcement of the expert system reasoning technique using data mining and knowledge-elicitation techniques.
- 3) Proposed method constitutes the framework of adaptive controller supporting the co-ordination and co-operation relations by integrating a real time simulator and an IDSS for implementing dynamic strategies.
- 4) Avoiding ineffective redundancy at concurrent firing of rules and high degree of parallelism
- 5) The simulation based IDSS uses a posteriori adap-

tive control mechanism that also is an online control method acting after the event occurs versus such popular reactive control method.

As a result, the proposed system is suitable for different control frameworks on an existing flexible manufacturing system considering the physical constraints and the production objectives. Furthermore, the system illustrates the potential of using the intelligent rule-based DSS for adaptive control of modern industrial plants. Future researches may concentrate on the application of other types of flexibility in shop floors using simulation-based predictive controllers.

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