

# Research on LFS Algorithm in Software Network

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## ABSTRACT

*Betweenness centrality helps researcher to master the changes of the system from the overall perspective in software network. The existing betweenness centrality algorithm has high time complexity but low accuracy. Therefore, Layer First Searching (LFS) algorithm is proposed that is low in time complexity and high in accuracy. LFS algorithm searches the nodes with the shortest to the designated node, then travels all paths and calculates the nodes on the paths, at last get the times of each node being traveled which is betweenness centrality. The time complexity of LFS algorithm is  $O(V^2)$ .*

**Keywords:** LFS, Software Network, the Shortest Path, Betweenness Centrality

## 1. Introduction

It is over fifteen years since Norman Fenton outlined the need for a scientific basis of software measurement. Such a theory is a prerequisite for any useful quantitative approach to software engineering, although little attention has been received from both practitioners and researchers. Measurement is the process that assigns numbers or symbols to attributes of real-world entities. Unfortunately, many empirical studies of software measurements lack a forecast system that combines measurements and parameters in order to make quantitative predictions. How can we overcome these limitations?

Here we present a new approach to software engineering based on recent advances in complex networks. As a typical parameter and an important global statistics, betweenness centrality can meet the needs of researchers to know the inter-reaction of software network from the overall perspective. The definition of betweenness centrality is the times of a node being traveled in all the shortest paths of the software network and it reflects the influence of the node in the whole network.

The existing betweenness centrality algorithms are either based on the shortest path or merely approximate algorithm [1-3], and both have its own shortcomings. First, the traditional shortest path algorithm has high time complexity and costs too much time to be available in large network, which makes it impossible to put the algorithms into practice. The research on approximation of betweenness centrality is unavailable for low accuracy which brings great obstacle for further study [4,5].

As mentioned in [6], the average path length is similar to normal distribution with the mean of 15.21. LFS algorithm is proposed based on this method.

The dissertation contains three parts: First, take Dijkstra algorithm as example to conclude shortcomings of traditional algorithms. Then, propose LFS algorithm. At last, compare these two algorithms to show the advantages of LFS algorithm.

## 2. Traditional Dijkstra Algorithm

The complexity of betweenness centrality comes from calculating the shortest path between each two nodes in network, and the time complexity of Dijkstra is  $O(n^3)$ . The existing algorithms based on the shortest path contain Dijkstra, Floyd-Warshall, and Johnson. Dijkstra is the most popular and classic algorithm.

The idea of Dijkstra is like this. Abstract the network into a graph, Put the isolated nodes (the nodes with out-degree and in-degree being both 0) in set  $V$  and the nodes having been traveled in set  $S$ , then calculate the shortest path from  $v_i$  to any node in the graph. Move the node  $v_k$  with the shortest path from  $V-S$  to  $S$  till  $V-S$  is empty.

① Initialization: Set up a two-dimensional array  $a$  to mark whether the shortest path has been found out between the two nodes. Set up a none-dimensional array to store the betweenness centrality. Set up a adjacency matrix arcs with 1 if there exist edge between the nodes, else with  $\infty$ .  $V$  is a set of all nodes and  $S$  is a set of all marked nodes. The value from  $v_i$  to  $v_j$  is initializes as

follows:

$$D[j]=arcs[vi][j] \quad v_j \in V$$

Then put  $v_i$  into  $S$ .

② Pick up  $v_k$  which satisfies

$$D[k]=\min\{D[j] \mid v_j \in V-S\}$$

$v_k$  is the end point of the shortest path starting from  $v_i$ .

Put  $v_k$  into  $S$ .

③ Calculate the length of the shortest path from  $v_i$  to each accessible node in set  $V-S$

$$D[k]+arcs[k][m]<D[m]$$

and revalue the  $D[m]$  as

$$D[k]+arcs[k][m]=D[m]$$

④ Add 1 to betweenness centrality of nodes if only they are on the shortest path from  $v_i$  to any node in the graph. Then mark these nodes being travelled in the two dimensional array  $a$ . Repeat ②, ③  $n-1$  times. At last, it gets all the shortest paths from  $v_i$  to the other nodes in the graph.

⑤ It is the end.

Repeat the process for  $n$  times and get the shortest path between each two nodes. Since each time contains a two-cycle, the time complexity of Dijkstra is  $O(V^3)$ . The space complexity is  $T(V^2)$ .

### 3. LFS Algorithm

According to the description to Dijkstra, it has a three-cycle and find out the shortest path between each two nodes which, then add 1 to between centrality of the nodes being on the path. The application range is limited for its high time complexity and the time consumption is unavailable when it is applied into large network of thousands of nodes. To solve this problem, the dissertation proposed a new algorithm (LFS) with the help of the features of software network.

As a number of papers mentioned [7–9], the length of shortest path between each two nodes wouldn't exceed a constant. For example, [1] says the average of the length is 15.21. Based on this method, LFS is proposed. Starting from a node in the network, put the connected nodes with the shortest path of 1 into array, and then put that of 2 into the array and so on till that of  $n$  in the array but there's no connected node with shortest path of  $n+1$ . Add 1 to the nodes on the paths which just have been found. The time complexity of LFS is the summation of length of all the shortest path between each two nodes, that is  $O(V^2)$ . Compared with Dijkstra, the time complexity of LFS is reduced obviously.

The preparation of LFS is similar to Dijkstra: abstract the network into a graph, set up an adjacent list which makes single-link lists for all non-isolated nodes in the graph and the  $i$ -list contains the nodes directly connected to the non-isolated node  $v_i$ . Each node is composed by two parts: neighboring nodes field ( $adjvex$ ) and linking field ( $nextarc$ ). The neighboring nodes field marks where

the nodes connected to node  $v_i$  are in the graph and the linking field marks the next node. Each single-link has a head node which is composed of data field ( $data$ ) and linking field ( $firstarc$ ). Data field marks the number of  $v_i$  in the graph and linking field marks the first node that is connected to  $v_i$ .

① Initialization: Set up a two-dimensional array  $c$  initialized maximum to store the length of the shortest path between each two nodes in the graph, then set up a one-dimensional array  $bc$  initialized 0 to store the betweenness centrality of each node.  $V$  is the number of non-isolated nodes in the graph.

② Set up array  $a$  and  $b$ .  $a$  is used to restore the end node of the shortest path.  $b$  is used to restore the number of nodes with the same starting node and the same length and put the starting point into  $a$  and put  $la=0$  into  $b$ . At last, set the relative element 0 in array  $c$ .

③ Judge whether it is the end of array  $a$ . If it is, turn to ⑧; else turn to ④.

④ Check out the number of nodes with the length of shortest path  $la$ , and set it to be  $n$ .

⑤ Travel the next node in array  $a$  and the find out all child nodes which are connected to this node (parent node) directly. If the value from starting node to this node in array  $c$  is bigger than  $la$ , set the value from the starting node to this node and the value from this node to starting node in array  $c$  to be  $la+1$ , then put the id of parent node and the id of child node into  $a$ . The same nodes being put into an  $m$  times means that there are  $m$  shortest paths from the starting node to this node. Add 1 to  $num$  which is the number of nodes on layer  $la+1$ . Because the id of parent node can be found by the id of child node, the shortest paths from the starting node to the other nodes in array  $a$  can be found, then add 1 to the nodes on each shortest path.

⑥ repeat ⑤  $n-1$  times.

⑦ put  $num$  into array  $b$ ,  $la=la+1$ , turn to ③.

⑧ repeat ②-⑦  $V-1$  times.

⑨ It is the end.

According to the description above, the time complexity of LFS is the summation of all the shortest path in the network, that is  $O(V^2)$ . And  $V$  is the number of non-isolated nodes in the network. The space complexity is  $T(V^2)$  which is equal to that of Dijkstra.

The comparison between the time complexity and space complexity of Dijkstra and LFS:

**Table 1. Time complexity and space complexity of Dijkstra and LFS**

algorithm	time complexity	space complexity
Dijkstra	$O(V^3)$	$T(V^2)$
LFS	$O(V^2)$	$T(V^2)$

#### 4. Performance Evaluations

Dijkstra takes breadth-first method to travels all the nodes in the software network, find out all the shortest paths, obtain the nodes on the shortest path, [10–12] and calculate betweenness centrality. Dijkstra has a three-cycle which makes the time complexity is so high that it is a fatal shortcoming when applied into large-scale software network.

LFS only has one-cycle, and travels nodes in the network one by one, then find out the shortest path from starting node to the other nodes. The time complexity of LFS is  $O(V^2)$  and the space complexity is  $T(V^2)$ . Depending on what mentioned above, LFS has great advantages both in time complexity and in space complexity.

With the development of computer science, the computer memory becomes bigger and bigger which can satisfy all kinds of demands and no longer need to be considered. So we spend no more time on discussing space complexity and merely pay attention to time complexity.

We get satisfying result with the help of HP computer which is composed of Core Duo 6300 CPU, 1.86GHz Frequency, DDR2 667 1GB Memory and Windows XP SP2 Operation System.

In order to verify that LFS has great advantages in time complexity, 22 samples are selected and sorted ascending which can justify whether LFS is applicable to software of different sizes. The comparison of time consumption between Dijkstra and LFS is shown as follows:

DT is the time cost by calculating betweenness cen-

trality of the software by Dijkstra, and WT is that by LFS. Time units are seconds. DT/WT which marks advantages of LFS in time consumption is the ratio of DT and WT.

Since both Dijkstra and LFS are related to the number of non-isolated nodes in the software network, the relation between these two kinds of algorithm is shown through the number of non-isolated nodes by the following figures. Figure 1 shows the time cost by these two algorithm when measure the same software. Figure 2 shows the multiples that LFS saved when compared to Dijkstra.

As shown in Figure 1, when the number of non-isolated nodes goes up, the time consumption of Dijkstra appears a clear upward trend, while the time consumption of LFS changes smoothly. And the larger the number of non-isolated nodes the more obviously the difference appears, which approves that the times consumption would not increase as quickly as the number of nodes, but Dijkstra is on the contrary.

As shown in Figure 2, Dijkstra cost more than 10 times even tens of times of time than LFS when they are applied into the same software. With the growth of the number of nodes, the curve has a clear upward trend although it is fluctuant sometimes. It approves that the advantages of LFS in time complexity appears more and more obviously as the software becomes larger and larger under the same circumstance, which says that LFS is especially fit for large-scale software network.

**Table 2. The comparison of time consumption between Dijkstra and LFS**

software	number of nodes	number of edges	number of non-isolated nodes	DT (s)	WT (s)	DT/WT
waimea	116	193	86	0.359	0.032	11.22
kicad	212	300	180	0.609	0.110	5.54
ktorrent	263	335	217	3.313	0.250	13.25
rhythmbox	366	342	252	8.349	0.531	15.72
filezilla	431	577	358	5.500	0.563	9.77
licq	574	633	491	12.110	1.282	9.45
freemind	713	933	562	53.172	1.812	29.34
espgs	1339	1271	955	150.094	7.063	21.25
abiword	1300	2124	1167	384.391	11.531	33.34
ArgoUML	2031	2217	1731	747.093	31.718	23.55
kdegraphics	2014	3498	1749	1036.781	44.688	23.20
mysql-5.0.56	3132	3837	2182	1685.828	54.453	30.96
mysql_6.0.6	3793	5368	2889	3131.318	104.531	29.96
kdepim	3518	4447	3008	2933.594	136.047	21.56
koffice	4580	5892	3883	4853.296	185.891	26.11
linux	7343	6045	4238	6756.612	296.313	22.80
resin	5076	7875	4261	10613.281	389.072	27.28
node	5418	11451	5418	13693.187	553.985	24.72
firefox	9261	15533	5781	18167.438	725.530	25.04
firefox	7100	48236	7100	24267.391	942.793	25.74
Mozilla	8354	13878	7195	37298.863	1315.750	28.35
firefox	10115	17469	8830	120818.089	3152.580	38.32

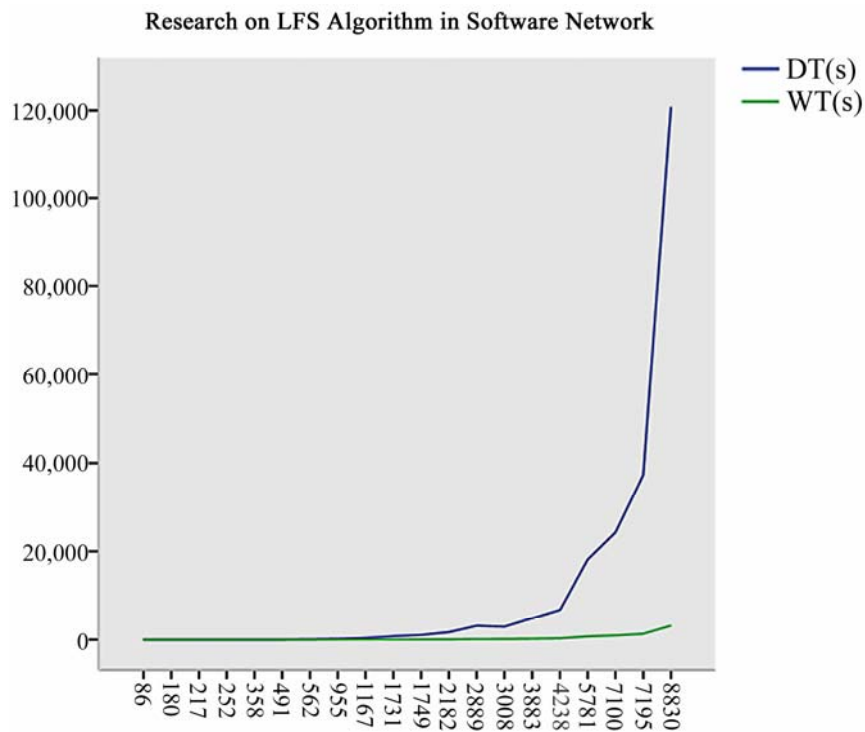


Figure 1. The time cost by Dijkstra and LFS

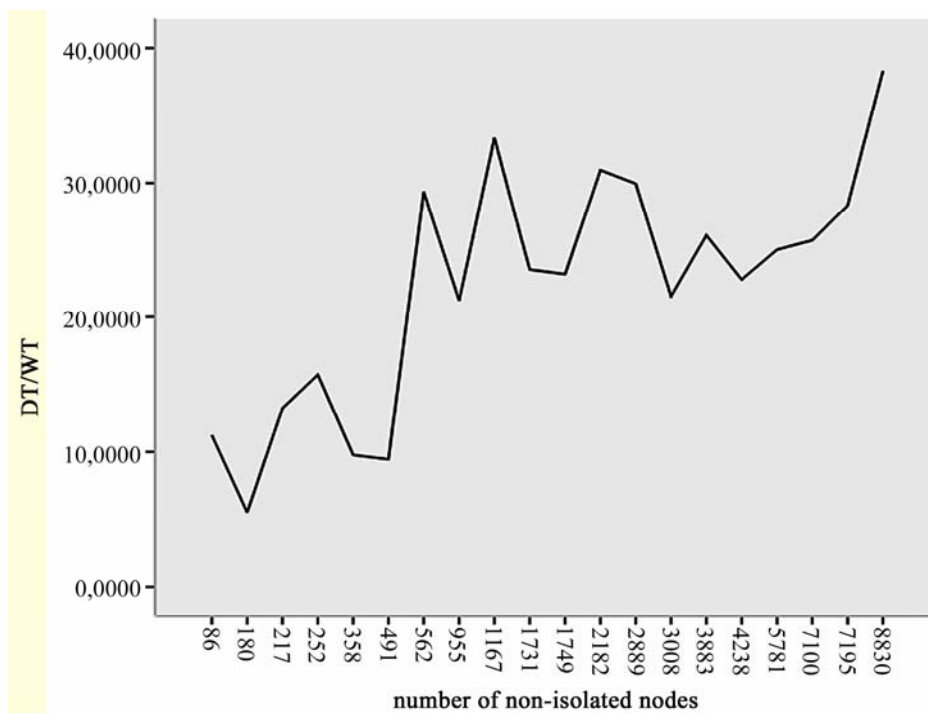


Figure 2. The multiples that LFS saved when compared to Dijkstra

As shown in Figure 2, the value of DT/WT shows an upward trend in volatility. Due to the relationship between the time complexity of LFS algorithm and the

complexity of the network itself, the value of DT/WT depends on the size of the network which is equals to the sum of the length of the entire shortest path. When

the software network is a little more complex and the lengths of shortest paths between some nodes are relative longer, LFS algorithm's time complexity will increase. For the same reason, when a more uniform distribution of the network and the lengths of shortest paths between some nodes are relative shorter, the advantage of LFS is fully reflected that the time complexity of LFS drops to relative small and the time consumption comes down too, but Dijkstra doesn't have such feature. Therefore, the value of DT/WT shows an upward trend in volatility. However, the curve appears an upward trend from the whole.

As mentioned above, the low time complexity of LFS can meet the needs of starting research on large-scale software and solve the problems brought by time complexity in the software measurement. At the same time, the accurate data obtained will bring accurate and reliable conclusion in practical research work.

## 5 Conclusions

LFS can solve a series of problems brought by the traditional algorithm. It has advantages both in time complexity and accuracy which are so important in practical research work that may result in disaster conclusion without it. LFS improve the efficiency and the accuracy to calculate the betweenness centrality, which ensures the further research to be continued smoothly.

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