

Empirical Investigation of Threats to Loyalty Programs by Using Models Inspired by the Gordon-Loeb Formulation of Security Investment

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Abstract

Loyalty program (LP) is a popular marketing activity of enterprises. As a result of firms' effort to increase customers' loyalty, point exchange or redemption services are now available worldwide. These services attract not only customers but also attackers. In pioneering research, which first focused on this LP security problem, an empirical analysis based on Japanese data is shown to see the effects of LP-point liquidity on damages caused by security incidents. We revisit the empirical models in which the choice of variables is inspired by the Gordon-Loeb formulation of security investment: damage, investment, vulnerability, and threat. The liquidity of LP points corresponds to the threat in the formulation and plays an important role in the empirical study because it particularly captures the feature of LP networks. However, the actual proxy used in the former study is artificial. In this paper, we reconsider the liquidity definition based on a further observation of LP security incidents. By using newly defined proxies corresponding to the threat as well as other refined proxies, we test hypotheses to derive more implications that help LP operators to manage partnerships; the implications are consistent with recent changes in the LP network. Thus we can see the impacts of security investment models include a wider range of empirical studies.

Keywords

Loyalty Program, Security Investment, Gordon-Loeb Model, Liquidity, Information Security Economics

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1. Introduction

Loyalty programs (LPs) are structured marketing efforts that reward, and therefore encourage, customers' loyalty [1]. LPs have proliferated in recent years as companies seek to acquire and retain customers, increase customer spending, and encourage the purchase of additional products [2]. However, some studies such as [3] argued that since most firms now utilize LPs, they are no longer effective in contributing to competitive advantage. Consequently, many firms are attempting to redesign LPs to enhance their effectiveness. In particular, in order to increase customers' loyalty, point exchange or redemption services have matured worldwide. For example, Points.com¹ is a major point exchange or redemption service in the U.S. In Japan, point exchange network is expanding, which enables customers to redeem points from one LP to another LP [4]. However, these services attract not only customers but also attackers whose aim is to obtain monetary benefits. In fact, there are an increasing number of LP incidents worldwide, as shown in Section 2.

When we consider security investment to reduce the damages caused by such incidents, we need to assess the features of LP network from the viewpoint of the efficacy of security investment. In order to answer to the above question, Jenjarrussakul and Matsuura [5] conducted an empirical study of LPs. Their study was performed inspired by the Gordon-Loeb model [6]-[8] of security investment; they considered damage, expense (or security investment), threat, and vulnerability as four fundamental factors when they developed their empirical analysis model. In particular, they provided security-liquidity implications by using the *liquidity* of an LP as a metric of threat. This analysis is possible because threat (defined as the probability of a threat occurring) and vulnerability (defined as the conditional probability that a threat once realized would be successful) are handled separately.

However, the definition of the liquidity itself is not deeply studied. The possibility of using other metrics is not well considered, either. In this paper, we investigate this threat metric more deeply by considering different metrics based on an observation of actual security incidents on LP systems.

Our work to be reported in the rest of this paper is inspired by this primary study [5], but there are important differences as follows. First, the liquidity definition is reconsidered, and a more intuitively convincing one is introduced. Second, we observe actual security incidents more deeply and give more implications that help LP operators to manage partnerships; the implications are consistent with recent changes in the LP network. Minor changes over the proxies used to test hypotheses also help our empirical study.

The rest of this paper is organized as follows. In Section 2, we see major incidents on LPs, which occurred worldwide, and their characteristics. In Section 3, we describe related and previous works. In Section 4, the data used in our empirical analyses are shown. In Sections 5, 6 and 7, different threat metrics and liquidity definition are investigated. Lastly, Section 8 concludes the paper.

2. Incidents on Loyalty Programs

In the U.K., compromised credentials enabled the theft of users' miles from the British Airways loyalty program in March 2015 [9]. In the U.S., Hilton Hotel rewards points were stolen in November 2014 [10]. This case happened because the login process was weak. Hackers can not only sell the stolen accounts or redeem the points but can also buy expensive items at Hilton shopping mall. About 10,000 accounts of American Airlines and United Airlines loyalty programs were compromised in December 2014 [11]. A March 2015 report [12] says "with Starbucks, hackers were somehow (still unclear) able to obtain customer usernames and passwords that opened up access to payment methods, which were used to refill gift card balances and transfer out gift card funds. Hackers can then sell these gift card balances to other people." In these cases, hackers are said to have used ID-password lists for mimicking successful authentications.

There is an increasing number of LP security incidents in Japan as well [13]. **Table 1** shows a list of major security incidents of LPs in Japan collected from web news articles that describe some characteristics of the attackers' behaviors: they often 1) attempt to go through the web login authentication mechanisms, 2) make malicious attempts in one or two days, and 3) attempt to steal the compromised accounts' points and redeem them into certain LP points. Regarding the third characteristic, it should be noted that Amazon Gift Card and iTunes Gift Code are often chosen as the redemption destinations by attackers. Their codes can be sold and eventually converted into real money. This is the first possible reason why attackers often choose those gifts. The second possible reason is that most attackers live outside Japan. Both Amazon and iTunes services are provided

¹<u>https://www.points.com/</u>.

Date	LP	Redemption destination	# of malicious redemptions	Damage (USD)	Source
2012.4.14-16	G Point	Amazon Gift Card	442	13,258	[14]
2013.3.26	T Point	other accounts of T point	-	-	[15]
2013.12	Rakuten Super Point	electric money	-	24,590	[16]
2014.1.19	Potora	-	-	-	[17]
2014.1.31-2.2	JAL Mileage Bank	Amazon Gift Card	65	>20,000	[18]
2014.3	Suica Point Club	-	-	-	[19]
2014.2	Hatena	Amazon Gift Card	-	-	[20]
2014.3.7-9	ANA Mileage Club	iTunes Gift Code		5,328	[21]
2014.3	Oki Doki Point Program	T point	Some	-	[22]
2014.4.19-29	Sony Point	Playstation store ticket, mora music card ID	273	6,172	[23]
2014.5.27-6.4	niconico point	-	19	1,423	[24]
2014.6.16-19	Hatena	Amazon Gift Card	0 (of 3 applications)	-	[25]
2014.6.23	CAPAT	-	203	-	[26]
2014.7.4	Anpara	-	60	-	[27]
2014.7.11-28	Poin-talk	prizes, other point programs	568	4,918	[28]
2014.8	Suica Point Club	-	-	-	[29]
2014.1	D STYLE WEB	-	47	-	[30]
2014.11	Hearcon	-	291	-	[31]
2014.12.23	morappo (mixi)	-	332	3,566	[32]
2015.5.17-6.29	AIP	-	33	1,228	[33]
2015.7.4-6	Life Media	Amazon Gift Card, iTunes Gift Code	0 (of 25 applications)	0	[34]
2015.7	Orico Point	T Point	156	-	[35]
2015.7.11	Prize Prize	Point-on PON	Some	-	[36]
2015.8.4	Lodging Net Point	Amazon Gift Card	123	2,418	[37]

 Table 1. Major LP security incidents in Japan.

internationally with their head offices outside Japan, so attackers can avoid investigations by Japanese police. As the third possible reason, it should be noted that Amazon and iTunes are not willing to publish the redemption algorithms; without their disclosure, we cannot trace and find who stole the points.

3. Related Works

3.1. Loyalty Programs

Effectiveness of LPs is well investigated in the management area [3]. Also, some research focuses on Japanese LPs. For example, the research has been conducted on the characteristics of Japanese LP network [38], the factor which leads LP partnership [39], LP network's economic reliability [40] and the network's impact on marketing performances [4]. These works do not consider LP security problems.

LP security issues were first economically researched by Jenjarrussakul and Matsuura in 2014 [5]. They show two implications: the impact of LP security incidents gets lower if stronger security requirements in web authen-

tication process are satisfied, and it is higher if the liquidity of the LP points gets higher. Our work is inspired by this primary study, but there are some important differences as mentioned in Section 1.

3.2. Virtual Currency and Security

European Central Bank defined virtual currency as "a type of unregulated, digital money, which is issued and usually controlled by its developers, and used and accepted among the members of a specific virtual community" and pointed out that LP points or miles can satisfy the definition [41]. Other representative virtual currencies include cryptocurrency and game currency. Regarding cryptocurrency, Bitcoin is the main research target [42]-[45]. Although these works handle security problems, they do not consider the relation between Bitcoin and LP systems. Massively multiplayer online games (MMOGs) currencies are also virtual currencies with security issues that have been researched without considering the relationship between the currencies and LP systems [46]-[50].

4. Data Collection

We retrieved the LP network structure from Poitan.net, a portal site of Japanese LP networks where users can search possible routes of point redemption, find the market value of each LP point, and so on (see **Appendix A.1**). Each LP operator's capital size was retrieved from each LP operator's website. The data of the security investment, damage amount and security requirements are the same as those in [5]. **Table 2** summarizes the data used in our study.

5. Point Liquidity and Number of Partners

5.1. Hypothesis Development

Reference [5] shows an important implication: an LP with higher liquidity suffers a bigger impact from incidents. However, the definition of the liquidity in [5] was not intuitively convincing as described in **Appendix C**. It may be more convincing if *liquidity* is defined more simply as:

$$liquidity_i = GoPartner_i \tag{1}$$

where $GoPartner_i$ is the number of partners into which one can redeem points from LP_i . In order to examine this definition, we set the following hypothesis:

H1. An LP with more outgoing partners suffers greater damage.

5.2. Model

In order to test H1, the following linear regression model is set:

$$\frac{\log(damage_i)}{\log(capital_i)} = \beta_0 + \beta_1 \frac{\log(expense_i)}{\log(capital_i)} + \beta_2 GoPartner_i + \beta_3 sec_score_i + u_i$$
(2)

where i is an index that indicates each LP, $damage_i$ is the annual damage amount of the overall IT security

Table 2. Data used in our study.	
Data	Details
LPs	82 Japanese LPs, which were selected by Jenjarrussakul and Matsuura [5] among 207 Japanese LPs registered at Poitan.net in Feb. 2014. For details, see Appendix B.1.
Security investment and damage amount of security incident	Retrieved from Information Processing Census (2012), the statistical data by METI (Ministry of Economics, Technology and Industries) of Japan [51].
Exchange network	Retrieved at Poitan.net in Dec. 2014.
Security requirement	Retrieved by Jenjarrussakul and Matsuura [5] in Apr. 2014; they investigated security re- quirements in each process of registration, login authentication and back-up authentication. For more details, see Appendix B.3.3 .
Capital size	Retrieved from every LP operator's web page in Feb. 2015. Each capital size is shown in Appendix B.1.

incidents of LP_i 's operator, $capital_i$ is the capital size of LP_i 's operator, $expense_i$ is the annual IT security expense of LP_i 's operator, sec_score_i is the security requirement level of the LP_i 's authentications, and u_i is the model's error term, assumed to be independent of the observed covariates. For more calculation details of these proxies, see **Appendix B.3**. Correlations between variables are shown in **Table 3**.

5.3. Results

To test *H*1, let the null hypothesis be $\beta_2 = 0$ in Equation (2). *H*1 is accepted if this null hypothesis is rejected. The estimated result of Equation (2) is shown in **Table 4**. The coefficient of *GoPartner_i* is significantly positive, so the null hypothesis $\beta_2 = 0$ is rejected, and *H*1 is accepted. Additionally, the coefficient of *sec_score_i* is significantly negative. This result is consistent with the results of [5].

6. Does Time Required for Redemption Affect the Damage?

6.1. Hypothesis Development

A redemption request is not always approved quickly; it may take one week or longer. If the LP operators have more time to give approval, they may notice suspicious redemption applications and reject them with higher chances. Thus attackers may prefer quicker redemption to avoid the risk of being detected. In fact, the incidents surveyed in Section 2 suggest this preference. So let us consider the following hypothesis.

H2. If an LP has more outgoing partners with short redemption time, the damage from incidents is bigger.

6.2. Data and Descriptive Statistics

Figure 1 shows the histogram of the time required for redemptions of all the exchange routes of 274 LPs and **Table 5** shows the descriptive statistics. **Table 6** shows the descriptive statistics regarding the 82 selected LPs.

6.3. Model

To test H2, we set the linear regression model as follows:

$$\frac{\log(damage_i)}{\log(capital_i)} = \beta_0 + \beta_1 \frac{\log(expense_i)}{\log(capital_i)} + \beta_2 GoPartner_{i,N} + \beta_3 (GoPartner_{i,90} - GoPartner_{i,N}) + \beta_4 sec_score_i + u_i$$
(3)

Table 3. Correlations between the variables in Equation (2). To save space, the following notation is used: Idam is $log(damage_i)$, lcap is $log(capital_i)$, lex is $log(expense_i)$, GoPartner is *GoPartner*_i, and SecScore is *sec_score*_i.

	ldam/lcap	lex/lcap	GoPartner	SecScore
ldam/lcap	1.000	-	-	-
lex/lcap	0.790	1.000	-	-
GoPartner	0.204	0.090	1.000	-
SecScore	-0.491	-0.417	0.025	1.000

Table 4. Results of the linear regression by Equation (2). The notations are the	he same as in Table 3 .
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Variable	Coef.	Std. Err	Prob.	
С	-0.218	0.091	0.020	**
lex/lcap	1.107	0.117	0.000	***
GoPartner	0.002	0.001	0.029	**
SecScore	-0.054	0.019	0.006	***
Adj. R ²	0.677			

Indicates significance at 5% level. *Indicates significance at 1% level.

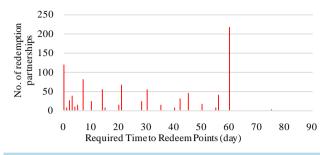


Figure 1. Histogram of the time required for redemption in December 2014.

Table 5. Descriptive statistics of the time required for redemption.

# of nodes	Min	Max	1 st Quartile	3 rd Quartile	Mean	Median
1265	0	90	7	56	30	28

Table 6. Descriptive statistics of the number of outgoing partners regarding the 82 selected LPs. Go_N represents the number of partners into which one can redeem points from each LP within *N* days.

	Min	Max	1 st Quar.	Median	3 rd Quar.	Ave.	Std. Dev.
Go_0	0	9	0	0	1	0.890	1.61
Go ₅	0	16	0	1	2	1.77	2.79
Go ₁₀	0	19	0	1	3	2.44	3.72
Go ₂₀	0	19	0	1	3	2.44	3.72
Go ₃₀	0	26	0	2	4	3.15	4.54
Go ₄₅	0	37	0	2	7	4.55	6.41
G0 ₆₀	0	39	1	3	9	6.33	7.85
Go ₉₀	0	40	1	3	9	6.50	7.94

where $GoPartner_{i,N}$ is the number of partners into which one can redeem points from LP_i within N days and the other variables are the same as those in Equation (2). Correlations between variables are shown in Table7.

6.4. Results and Discussion

The estimated results of Equation (3) for N = 0, 5, 10, 30, 45, 60 are shown in **Table 8**. When N is 0 or 5, β_3 is significantly positive, but β_2 does not show any significances. This means that if an LP suffers greater damage if it has more point-redeeming partners over the time threshold, 0 or 5 days. On the other hand, when N is 45 or 60, β_3 shows no significance but β_2 is significantly positive. This suggests that a LP suffers more damage when it has a larger number of point-redeeming partners under the time threshold, 45 or 60 days. When N is 10 or 30, no significances were provided.

These results suggest that the number of outgoing partners that require at least 45 days for redemption does not affect the liquidity. Although it is not supported if the threshold time is 5 days, *H*2 is supported if the threshold time is 45 days. It is shown that the damage gets bigger if the LP has more partnerships with shorter redemption times. Thus we find that redemption time has some effects on liquidity, and hence, on the threats to LPs.

7. Do Specific Partners Affect the Damage?

7.1. Hypothesis Development

Table 9 and Figure 2 show the number of LPs (out of the 82 selected LPs) from which one can redeem points

		(a) $N = 0$)		
	ldam/lcap	lex/lcap	Go_0	Go_{90} - Go_0	SecScore
ldam/lcap	1.000	-	-	-	-
lex/lcap	0.790	1.000	-	-	-
Go_0	0.273	0.247	1.000	-	-
Go_{90} - Go_0	0.164	0.044	0.380	1.000	-
SecScore	-0.491	-0.417	-0.314	0.058	1.000
		(b) <i>N</i> = :	5		
	ldam/lcap	lex/lcap	Go_5	G090-G05	SecScore
ldam/lcap	1.000	-	-	-	-
lex/lcap	0.790	1.000	-	-	-
Go_5	0.223	0.255	1.000	-	-
G090-G05	0.152	0.000	0.333	1.000	-
SecScore	-0.491	-0.417	-0.192	0.112	1.000
		(c) $N = 1$	0		
	ldam/lcap	lex/lcap	Go_{10}	Go_{90} - Go_{10}	SecScore
ldam/lcap	1.000	-	-	-	-
lex/lcap	0.790	1.000	-	-	-
Go_{10}	0.320	0.265	1.000	-	-
Go_{90} - Go_{10}	0.075	-0.047	0.379	1.000	-
SecScore	-0.491	-0.417	-0.184	0.153	1.000
		(d) $N = 3$	0		
	ldam/lcap	lex/lcap	Go_{30}	Go ₉₀ -Go ₃₀	SecScore
ldam/lcap	1.000	-	-	-	-
lex/lcap	0.790	1.000	-	-	-
Go_{30}	0.289	0.210	1.000	-	-
G090-G030	-0.001	-0.121	0.379	1.000	-
SecScore	-0.491	-0.417	-0.100	0.196	1.000
		(e) $N = 4$	5		
	ldam/lcap	lex/lcap	Go_{45}	G090-G045	SecScore
ldam/lcap	1.000	-	-	-	-
lex/lcap	0.790	1.000	-	-	-
Go_{45}	0.294	0.171	1.000	-	-
G090-G045	-0.081	-0.117	0.278	1.000	-
SecScore	-0.491	-0.417	-0.088	0.234	1.000

Table 7. Correlations between the variables in Equation(3) for different values of *N*. Go_N represents $GoPartner_{i,N}$ and other notations are the same as in **Table 3**.

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(f) $N = 60$						
	ldam/lcap	lex/lcap	Go_{60}	G090-G060	SecScore	
ldam/lcap	1.000	-	-	-	-	
lex/lcap	0.790	1.000	-	-	-	
Go_{60}	0.204	0.090	1.000	-	-	
G090-G060	0.034	0.006	0.123	1.000	-	
SecScore	-0.491	-0.417	0.021	0.063	1.000	

Table 8. Results of the regression by Equation (3) for N = 0, 5, 10, 30, 45, 60. The notations are the same as in Table 7.

	N = 0				<i>N</i> = 5				<i>N</i> = 10			
Variable	Coef.	Std. Err	Prob.		Coef.	Std. Err	Prob.		Coef.	Std. Err	Prob.	
С	-0.219	0.093	0.0212	**	-0.238	0.0908	0.0106	**	-0.221	0.0931	0.0202	**
lex/lcap	1.11	0.119	0.000	***	1.14	0.116	0.000	***	1.11	0.120	0.000	***
Go_N	0.00148	0.00475	0.763		-0.00259	0.00268	0.337		0.00147	0.00212	0.489	
Go_{90} - Go_N	0.00197	0.00103	0.0607	*	0.00316	0.0011	0.0054	***	0.00214	0.0133	0.110	
SecScore	-0.0543	0.0192	0.0061	***	-0.0602	0.0191	0.0023	***	-0.0550	0.0195	0.0063	***
Adj. R ²	0.677				0.690				0.677			

	<i>N</i> = 30				N = 45				N = 60			
Variable	Coef.	Std. Err	Prob.		Coef.	Std. Err	Prob.		Coef.	Std. Err	Prob.	
С	-0.222	0.0934	0.0199	**	-0.209	0.0919	0.0261	**	-0.217	0.0919	0.0206	**
lex/lcap	1.11	0.120	0.000	***	1.09	0.118	0.000	***	1.11	0.117	0.000	***
Go_N	0.00162	0.00137	0.242		0.00259	0.00113	0.0253	**	0.00187	0.000881	0.0367	**
Go_{90} - Go_N	0.00241	0.00199	0.230		-9.98E-06	0.000227	0.997		0.00467	0.0122	0.704	
SecScore	-0.0550	0.0194	0.006	***	-0.0503	0.0195	0.0118	**	-0.0544	0.0192	0.0059	***
Adj. R ²	0.677				0.680				0.677			

*Indicates significance at 10% level. **Indicates significance at 5% level. ***Indicates significance at 1% level.

Table 9. Number of LPs (out of the 82 selected LPs) from which one can redeem points into Amazon and iTunes for $N = 0$,	,
5, 10, 30, 45, 60, 90.	

	N = 0	<i>N</i> = 5	N = 10	<i>N</i> = 30	N = 45	N = 60	<i>N</i> = 90
Amazon	4	6	10	14	15	16	17
iTunes	3	5	9	14	14	15	16
Amazon or iTunes	5	7	11	16	17	19	20
Amazon and iTunes	2	4	8	12	12	12	13

into Amazon Gift Cards and iTunes Gift Codes with respect to the time required for redemption. As we mentioned in Section 2, attackers seem to prefer Amazon Gift Cards and iTunes Gift Codes for malicious redemptions. Taking alliances with specific partners might expose an LP to bigger threats. So we set the following hypothesis.

H3. An LP that takes partnership with Amazon or iTunes suffers greater damage.

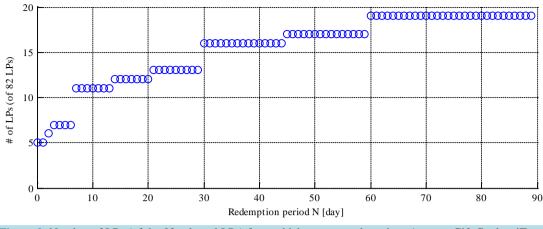


Figure 2. Number of LPs (of the 82 selected LPs) from which one can redeem into Amazon Gift Card or iTunes Gift Code within *N* days.

7.2. Model

To test H3, we set the linear regression model as follows:

$$\frac{\log(damage_i)}{\log(capital_i)} = \beta_0 + \beta_1 \frac{\log(expense_i)}{\log(capital_i)} + \beta_2 GoToAorI_{i,N} + \beta_3 (GoToAorI_{i,90} - GoToAorI_{i,N}) + \beta_4 sec_score_i + u_i$$
(4)

when N < 90, and

$$\frac{\log(damage_i)}{\log(capital_i)} = \beta_0 + \beta_1 \frac{\log(expense_i)}{\log(capital_i)} + \beta_2 GoToAorI_{i,90} + \beta_3 sec_score_i + u_i$$
(5)

when N = 90, where $GoToAorI_{i,N}$ is the binary value representing whether one can redeem points from LP_i to an Amazon Gift Card or iTunes Gift Code within N days (1 if possible, 0 otherwise), and the other variables are the same as in Equation (2).

Correlations between the variables in Equation (4) and Equation (5) are shown in Table 10.

7.3. Results and Discussion

The estimated results for N = 0, 5, 10, 30, 45, 60, 90 are shown in Table 11.

When N = 10,45,90, β_2 is significantly weakly positive at 10% level. When N is 10 or 45, β_3 does not show any significance. This means that H3 is weakly supported for the redemption time, 10, 45 and 90 days. Additionally, it suggests that availability of redemption into Amazon or iTunes does not affect the damage if one has to wait more than 45 days to complete the transaction. When N = 30 or N = 60, the p-values of β_2 are rather small, although it is insufficient for the 10%-level weak support. On the other hand, when N = 0 or N = 5, β_3 is significantly positive and β_2 is insignificant. This means if an LP has an outgoing partnership with Amazon or iTunes and the redemption takes more than 0 or 5 days, it suffers more damage, while we cannot see any relation between the damage and the availability of 0 or 5-day redemption. While it differs from the intuition, the same discussion as in Section 6.4 can be applied.

In Japan, some of the LP operators who experienced damages by malicious redemption into Amazon Gift Cards or iTunes Gift Codes introduced countermeasures; they either temporarily stopped their alliance with Amazon and iTunes or introduced phone authentication regarding the redemption into. This recent trend is supported by the above result of our empirical analysis.

8. Concluding Remarks

In this paper, we revisit the empirical models used in a former study [5] regarding the security of loyalty

		(a) N =	= 0		
	ldam/lcap	lex/lcap	$GoAI_0$	GoAI ₉₀ -GoAI ₀	SecScore
ldam/lcap	1.000	-	-	-	-
lex/lcap	0.790	1.000	-	-	-
$GoAI_0$	-0.054	-0.019	1.000	-	-
GoAI ₉₀ -GoAI ₀	0.488	0.385	-0.126	1.000	-
SecScore	-0.491	-0.417	-0.055	-0.361	1.000
		(b) <i>N</i> =	= 5		
	ldam/lcap	lex/lcap	GoAI ₅	GoAI ₉₀ -GoAI ₅	SecScore
ldam/lcap	1.000	-	-	-	-
lex/lcap	0.790	1.000	-	-	-
$GoAI_5$	0.007	0.073	1.000	-	-
GoAI90-GoAI5	0.476	0.339	-0.138	1.000	-
SecScore	-0.491	-0.417	-0.149	-0.304	1.000
		(c) <i>N</i> =	: 10		
	ldam/lcap	lex/lcap	$GoAI_{10}$	$GoAI_{90}$ - $GoAI_{10}$	SecScore
ldam/lcap	1.000	-	-	-	-
lex/lcap	0.790	1.000	-	-	-
$GoAI_{10}$	0.320	0.234	1.000	-	-
GoAI ₉₀ -GoAI ₁₀	0.212	0.205	-0.144	1.000	-
SecScore	-0.491	-0.417	-0.243	-0.224	1.000
		(d) <i>N</i> =	= 30		
	ldam/lcap	lex/lcap	$GoAI_{30}$	GoAI ₉₀ -GoAI ₃₀	SecScore
ldam/lcap	1.000	-	-	-	-
lex/lcap	0.790	1.000	-	-	-
GoAI ₃₀	0.296	0.259	1.000	-	-
GoAI ₉₀ -GoAI ₃₀	0.271	0.193	-0.116	1.000	-
SecScore	-0.491	-0.417	-0.243	-0.263	1.000
		(e) <i>N</i> =	: 45		
	ldam/lcap	lex/lcap	GoAI ₄₅	GoAI ₉₀ -GoAI ₄₅	SecScore
ldam/lcap	1.000	-	-	-	-
lex/lcap	0.790	1.000	-	-	-
GoAI ₄₅	0.377	0.296	1.000	-	-
GoAI ₉₀ -GoAI ₄₅	0.123	0.129	-0.104	1.000	-
SecScore	-0.491	-0.417	-0.272	-0.226	1.000

Table 10. Correlations between variables in Equations (4) and (5) for different values of *N*. $GoAI_N$ represents *GoToAorI*_{*i*,*N*} and other notations are the same as in **Table 3**.

		(f) <i>N</i> =	= 60		
	ldam/lcap	lex/lcap	$GoAI_{60}$	GoAI ₉₀ -GoAI ₆₀	SecScore
ldam/lcap	1.000	-	-	-	-
lex/lcap	0.790	1.000	-	-	-
$GoAI_{60}$	0.391	0.321	1.000	-	-
GoAI ₉₀ -GoAI ₆₀	0.100	0.083	-0.064	1.000	-
SecScore	-0.491	-0.417	-0.329	-0.129	1.000

(g) N = 90

	ldam/lcap	lex/lcap	GoAI ₉₀	SecScore
ldam/lcap	1.000	-	-	-
lex/lcap	0.790	1.000	-	-
$GoAI_{90}$	0.410	0.336	1.000	-
SecScore	-0.491	-0.417	-0.357	1.000

Table 11. Results of the linear regression by Equations (4) and (5) for N = 0, 5, 10, 30, 45, 60, 90. The notations are the same as in Table 10.

	N = 0				<i>N</i> = 5				<i>N</i> = 10				N = 30			
Variable	Coef.	Std. Err	Prob.		Coef.	Std. Err	Prob.		Coef.	Std. Err	Prob.		Coef.	Std. Err	Prob.	
С	-0.179	0.0930	0.0585	*	-0.179	0.0910	0.053	*	-0.205	0.0936	0.0318	**	-0.205	0.0936	0.0318	**
lex/lcap	1.05	0.120	0.000	***	1.05	0.117	0.000	***	1.09	0.121	0.000	***	1.09	0.121	0.000	***
$GoAI_N$	-0.0120	0.0284	0.674		-0.0137	0.0244	0.575		0.0389	0.0215	0.0749	*	0.0247	0.0185	0.186	
GoAI90-GoAI	0.0468	0.0196	0.0197	**	0.0557	0.0200	0.0067	***	0.018	0.0233	0.441		0.0523	0.0337	0.125	
SecScore	-0.0405	0.0196	0.0425	**	-0.0423	0.0192	0.0311	**	-0.0428	0.0199	0.0351	**	-0.0407	0.0201	0.0465	**
Adj. R ²	0.682				0.693				0.670				0.671			

	N = 45				N = 60				N = 90			
Variable	Coef.	Std. Err	Prob.		Coef.	Std. Err	Prob.		Coef.	Std. Err	Prob.	
С	-0.203	0.0937	0.0338	**	-0.205	0.0940	0.0322	**	-0.205	0.0933	0.031	**
lex/lcap	1.09	0.121	0.000	***	1.09	0.121	0.000	***	1.09	0.120	0.000	***
$GoAI_N$	0.0331	0.0183	0.0741	*	0.0295	0.0178	0.102		0.0295	0.0175	0.0958	*
$GoAI_{90}$ - $GoAI_N$	0.00578	0.0380	0.880		0.0282	0.0634	0.657		N/A	N/A	N/A	
SecScore	-0.0444	0.0201	0.0302	**	-0.0427	0.0201	0.0365	**	-0.0427	0.0199	0.035	**
Adj. R ²	0.670				0.668				0.668			

*Indicates significance at 10% level. ***Indicates significance at 5% level. ****Indicates significance at 1% level.

programs. In the models, the choice of variables is inspired by the Gordon-Loeb formulation of security investment: damage, investment, vulnerability, and threat. The liquidity of LP points corresponds to the threat in the formulation and plays an important role in the empirical study because it captures a particular feature of LP networks. However, the actual proxy used in the former study is artificial due to the fact that its original definition is not LP-wise but industry-wise. In this paper, we reconsidered the liquidity definition based on a further observation of LP security incidents. By using newly defined proxies corresponding to the threat as well as other refined proxies, we conducted hypothesis testing to derive more implications. We show the damage from LP incidents grows if partnerships with short redemption times or with Amazon or iTunes are accepted. These implications will help LP operators manage partnerships. In fact, these findings are consistent with recent trends in the LP network. Thus we can see the impacts of security investment models include a wider range of empirical studies in the economics of information security.

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Appendix A. Poitan.net

Poitan (http://poitan.net) provides information on more than 200 LPs in Japan, such as estimated real-currency values of LP points, exchange/conversion rates between different LPs and how long the conversion would take. Suppose that a consumer would like to convert a certain amount of ANA (All Nippon Airways, a star alliance member) miles, say, 20,000 miles, into JAL (Japan Airlines, a one-world alliance member) miles. In response to this query, Poitan shows some possible conversion routes. For example, on December 25, 2015, Poitan said there were 87 possible routes. One of the possible routes with the best rate was as follows:

1) Convert 20,000 ANA miles (estimated value is 30,000 JPY (Japanese Yen)) into 20,000 JQ Card Points² points (estimated value is 20,000 JPY). This would take about 60 days.

2) Convert 20,000 JQ Card points into 20,000 Epos Card Points³ (estimated value is 20,000 JPY). This would take about 3 days.

3) Convert 20,000 Epos Card Points into 10,000 JAL miles (estimated value is 15,000 JPY). This would take about 60 days.

Appendix B. Data and Proxies for Empirical Analyses

B.1.82 Selected LPs

Table A1 shows the 82 selected LPs. *LP ID* indicates the LP's ID of Poitan.net. You can access the information of an LP via http://dir.poitan.net/(.*).html, where (.*) is its ID number.

B.2. Industry

Table A2 shows the nine industries which operate LPs in Japan.

B.3. Calculations of the Proxies

Our empirical studies were conducted based on the Gordon-Loeb security investment model [6], which considers the following four parameters as fundamental parameters: *expense*—the amount of security investment, *damage*—the amount of damage when the attack occurred, *threat*—the probability that an attack occurs, and *vulnerability*—the conditional probability that a threat once realized would be successful. When we consider the security of LP systems, one possible interpretation of the four parameters is as follows: *Expense* is the expense on IT security countermeasures by the LP-operating company; *Damage* is the amount of damage from IT incidents; *Threat* is considered to be high if the LP points' liquidity is high because higher liquidity implies more chances of achieving criminal benefits by malicious conversion of LP points or their redemption and it can be a main attractive factor; *Vulnerability* is considered to be lower if the online user authentication system of an LP is implemented in a more secure manner.

This appendix shows how we set and calculate each proxy based on this interpretation, other than threat.

B.3.1. Damage

As is shown in **Table A3**, METI's numerical data of IT damage represent only the ranges because of its questionnaire design [52]. So we calculated the average damage size for every industry and every capital size level by using the middle value of the range (e.g. 0.75 million JPY for the range "0.5 million to 1 million") with an exception at the edge (*i.e.* we use 200 million JPY for the range "over 100 million." This method is also used by METI [51].

Then, from each LP's industry and capital size, we calculate its damage. We set this damage size as $damage_i$ where $i = 1, 2, \dots, 82$ indicates each respective LP. For example, if LP₁'s industry is "Information Service" and its capital size is "under 50 million JPY", $damage_1 = 1875000$.

This proxy calculation differs from [5] in the following three points. 1) Reference [5] ignored firms which answered "did not suffer information security incidents," but we consider them as zero because it is more accurate. 2) In [5], they calculated the average damage considering only the industrial categorization, but we also considered the capital size for segmentation. 3) Reference [5] used *impact = damage*_{IND_i} * *rank*_i as the proxy

²JQ Card Point is a reward program of a credit card provided by a Japanese railway company.

³Epos Card Point is a reward program of a credit card provided by one of the biggest department store in Japan, Marui.

Table A1. List of the 82 Selected LPs (Part 1). LP ID indicates registered ID at Poitan, Industry ID indicates each industry (details are in **Appendix B.2**), and Capital size is each LP operator's capital size. Security score shows a security requirement level calculated by the methods described at **Appendix B.3.** N/A means that we cannot access the corresponding information.

LP ID at Poitan	Name of LP	Industry ID	Capital size (JPY)	Security score
1	JAL Mileage bank	20	355,845,000,000	0.667
2	ANA Mileage club	20	25,000,000,000	0.667
15	Mitsui Sumitomo card	23	34,030,000,000	0.667
29	G-Point	19	296,000,000	0.333
30	Net Mile	19	N/A	0.000
31	J-Point (changed to "My green stamp")	19	100,000,000	0.167
32	Outlet Point	26	1,527,000,000	0.500
34	Biccamera	22	18,402,380,000	0.167
36	Rakuten	19	1,095,300,000	0.000
38	Cecile	22	2,000,000,000	0.167
39	Belle Maison	22	20,359,000,000	0.167
42	Amazon Gift Voucher	22	N/A	0.000
43	T Point	19	100,000,000	0.333
44	Jbook	22	4,340,000,000	0.000
45	Honto	22	4,340,000,000	0.000
46	NTT Docomo	17	949,679,500,000	1.000
47	au	17	141,851,000,000	1.000
48	NTT communication	17	211,700,000,000	1.000
62	Ponta	26	2,381,578,000	0.500
63	Mitsubishi Tokyo UFJ Bank	23	1,711,900,000,000	0.667
66	Manex Stock Company	23	12,200,000,000	0.833
70	Starbucks Card	22	8,548,090,000	0.333
71	Matsumoto Kiyoshi	22	21,086,000,000	0.500
74	Rakuten Edy	19	1,840,000,000	1.000
78	Risona Bank	23	50,400,000,000	1.000
81	Yamada Denki	22	71,050,000,000	0.000
92	Recruit	26	10,000,000,000	0.000
97	Sony Finance	19	N/A	1.000
98	Sony point	9	100,000,000	0.167
100	Daiwa Stock Company	23	100,000,000,000	1.000
101	Circle K Sunkus	22	8,380,400,000	0.000
103	Chobi Rich	26	65,700,000	0.167
110	ANA JCB Card	23	10,616,100,000	0.800

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123 Sofmap 22 100,000,00 0.167 126 Bidders 19 10,397,000,000 0.167 127 Softbank Mobile 17 177,251,000,000 0.660 131 Web Money 19 495,784,000 1.000 133 Locca 20 100,000,000,000 0.667 134 J-WEST Card 20 100,000,000,000 0.667 138 Times 26 8,219,000,000 0.167 144 PeX 19 198,000,000 0.500 149 nanaco Point 23 7,500,000,000 0.500 152 Sucia point Cubb 20 200,000,000,000 N:A 155 Chocum point 17 306,578,542 0.000 160 JP BANK Card 23 3,500,000,000 0.167 163 Central Nippon Expressway Company 20 65,000,000,000 1.000 164 SBI Point 23 81,681,000,000 1.000 206 <td< th=""><th>Continued</th><th></th><th></th><th></th><th></th></td<>	Continued				
127 Softbank Mobile 17 177.251.000,000 0.600 131 Web Money 19 495.784.000 1.000 133 Locca 20 100.000.000,00 0.667 134 J-WEST Card 20 100.000.000,00 0.667 138 Times 26 8.219.000,000 0.167 146 PEX 19 198.000,000 0.500 148 namaco 23 7.500.000,000 0.500 152 Snica point club 20 200.000,000,00 0.600 153 Chocom e Money 17 306.578.542 0.000 154 Tepore 17 306.578.542 0.000 155 Chocom point 17 306.578.542 0.000 160 JP BANK Card 23 35.00,000,000 0.400 161 Central Nippon Expressway Company 20 65.00,00,000 1.000 163 Central Nippon Expressway Company 20 139.400,00,000 1.000	123	Sofmap	22	100,000,000	0.167
131 Web Money 19 495,784,000 1.000 133 koca 20 100,000,000,00 0.667 134 J-WEST Card 20 100,000,000,00 0.667 138 Times 26 8.219,000,000 0.167 146 PeX 19 198,000,000 0.500 144 nanaco 23 7.500,000,000 0.500 152 Suica point club 20 200,000,000,000 NA 155 Chocom e Money 17 306,578,542 0.000 159 Chocom point 17 306,578,542 0.000 160 JP BANK Card 23 3,500,000,000 0.833 161 Point Monkey 26 80,000,000 1.000 163 Central Nippon Expressway Company 20 65,000,000,000 1.000 164 SBI Point 23 N/A 0.667 200 ENEOS Card 19 N/A 0.167 211 Point Exchange	126	Bidders	19	10,397,000,000	0.167
133 Loca 20 100,000,000 0.667 134 L-WEST Card 20 100,000,000 0.667 138 Times 26 8,219,00,000 0.167 146 PeX 19 198,00,000 0.500 148 nanaco 23 7,500,000,000 0.500 149 nanaco Point 23 7,500,000,000 NA 152 Suica point club 20 200,000,000 NA 155 Chocom e Money 17 306,578,542 0.000 160 JP BANK Card 23 3,500,000,000 0.833 161 Point Mankey 26 80,000,000 0.000 163 Central Nippon Expressway Company 20 65,000,000,00 1.000 164 SBI Point 23 NA 0.667 200 ENEOS Card 23 NA 0.167 211 MUFG Card 19 NA 1.000 212 Gentral Nippon Expressway Company 1	127	Softbank Mobile	17	177,251,000,000	0.600
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152 Suica point club 20 200,000,000,000 N/A 155 Chocom e Money 17 306,578,542 0.000 158 Tepore 17 270,000,000 0.000 159 Chocom point 17 306,578,542 0.000 160 JP BANK Card 23 3,500,000,000 0.833 161 Point Monkey 26 80,000,000 0.167 163 Central Nippon Expressway Company 20 65,000,000,000 0.000 171 MUFG Card 23 N/A 0.667 200 ENEOS Card 22 139,400,000 0.100 171 MUFG Card 23 N/A 0.667 200 ENEOS Card 22 139,400,000 1.000 206 Kactoku card 19 N/A 0.167 209 NTT East Japan (Flet internet) 17 335,000,000,000 0.000 211 Point Exchange 19 411,162,000 0.167 215 <	148	nanaco	23	7,500,000,000	0.500
155 Chocon e Money 17 306,578,542 0.000 158 Tepore 17 270,000,000 0.000 159 Chocon point 17 306,578,542 0.000 160 JP BANK Card 23 3,500,000,000,000 0.833 161 Point Monkey 26 80,000,000 0.167 163 Central Nippon Expressway Company 20 65,000,000,000 0.000 171 MUFG Card 23 N/A 0.667 200 ENEOS Card 22 139,400,000,000 1.000 205 Kaetoku card 19 N/A 0.167 206 Kaetoku card 19 N/A 0.167 207 Sitama Change 19 N/A 0.167 216 Apple World 26 200,000,000 0.000 217 Apple World 26 211,500,000 0.000 216 Apple World 26 211,500,000 0.000 217 TEPCO 1	149	nanaco Point	23	7,500,000,000	0.500
158 Tepore 17 270,000 0,000 159 Chocom point 17 306,578,542 0,000 160 JP BANK Card 23 3,500,000,000 0.833 161 Point Monkey 26 80,000,000 0.167 163 Central Nippon Expressway Company 20 65,000,000,000 1.000 164 SBI Point 23 81,681,000,000 0.000 171 MUFG Card 23 N/A 0.667 200 ENEOS Card 22 139,400,000,000 1.000 205 Kaetoku card 19 N/A 0.167 206 Kaetoku card 19 N/A 0.167 207 MTF East Japan (Flet internet) 17 335,000,00,000 1.000 211 Point Exchange 19 411,162,000 0.000 212 Gendama 19 410,090,000,000 N/A 212 GetMoney! 26 211,500,000 0.000 213 Saitama	152	Suica point club	20	200,000,000,000	N/A
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164 SBI Point 23 81,681,000,000 0.000 171 MUFG Card 23 N/A 0.667 200 ENEOS Card 22 139,400,000,000 1.000 206 Kaetoku card 19 N/A 1.000 208 Cue Monitor 19 N/A 0.167 209 NTT East Japan (Flet internet) 17 335,000,000,000 1.000 211 Point Exchange 19 411,162,000 0.000 212 Gendama 19 411,162,000 0.000 217 nimoca 20 126,400,000 N/A 213 GetMoney! 26 211,500,000 0.000 217 TEPCO 16 1,400,900,000,000 N/A 232 GetMoney! 26 211,500,000 0.000 233 MyVoice 19 178,000,000 0.000 234 MyVoice 19 914,000,000 0.000 240 Ikyu 19 914,00	161	Point Monkey	26	80,000,000	0.167
171 MUFG Card 23 N/A 0.667 200 ENEOS Card 22 139,400,000,000 1.000 206 Kaetoku card 19 N/A 1.000 208 Cue Monitor 19 N/A 0.167 209 NTT East Japan (Flet internet) 17 335,000,000,000 1.000 211 Point Exchange 19 411,162,000 0.000 212 Gendama 19 411,162,000 0.000 215 Apple World 26 200,000,000 N/A 217 nimoca 20 126,400,000 N/A 232 GetMoney! 26 211,500,000 0.000 237 Saitama Risona Bank 23 70,000,000,000 N/A 238 MyVoice 19 178,000,000 0.000 239 Chance Ir 19 211,500,000 0.000 240 Ikyu 19 914,000,000 0.000 241 Fastask 19 10,146,510,000 1.000 242 Ogaki Kyoritsu Bank 23	163	Central Nippon Expressway Company	20	65,000,000,000	1.000
200 ENEOS Card 22 139,400,000,000 1.000 206 Kaetoku card 19 N/A 1.000 208 Cue Monitor 19 N/A 0.167 209 NTT East Japan (Flet internet) 17 335,000,000,000 1.000 211 Point Exchange 19 411,162,000 0.000 212 Gendama 19 411,162,000 0.000 213 Apple World 26 200,000,000 0.000 214 nimoca 20 126,400,000 N/A 215 Apple World 26 211,500,000 0.000 217 nimoca 20 126,400,000 N/A 212 GetMoney! 26 211,500,000 0.000 213 Saitama Risona Bank 23 70,000,000,000 1.000 213 Saitama Risona Bank 23 70,000,000 0.000 214 Kase 19 211,500,000 0.000 215 Ogaki Kyoritsu Bank 23 36,100,000,000 1.000	164	SBI Point	23	81,681,000,000	0.000
206 Kaetoku card 19 N/A 1.000 208 Cue Monitor 19 N/A 0.167 209 NTT East Japan (Flet internet) 17 335,000,000,000 1.000 211 Point Exchange 19 411,162,000 0.000 212 Gendama 19 411,162,000 0.000 215 Apple World 26 200,000,000 0.000 217 nimoca 20 126,400,000 N/A 223 GetMoney! 26 211,500,000 0.000 234 GetMoney! 26 211,500,000 0.000 235 GetMoney! 26 211,500,000 0.000 236 GetMoney! 23 70,000,000,000 1.000 237 Saitama Risona Bank 23 70,000,000,000 0.000 238 MyVoice 19 178,000,000 0.000 240 Kyu 19 914,000,000 0.000 241 Fastask 19 10,146,510,000 1.000 242 Ogaki Kyoritsu Bank 23<	171	MUFG Card	23	N/A	0.667
208Cue Monitor19N/A0.167209NTT East Japan (Flet internet)17335,000,000,0001.000211Point Exchange19411,162,0000.000212Gendama19411,162,0000.000213Apple World26200,000,0000.000217nimoca20126,400,0001.000217GetMoney!26211,500,0000.000237Saitama Risona Bank2370,000,000,0001.000238MyVoice19178,000,0000.000239Chance It19211,500,0000.000240Ikyu19914,000,0000.000241Fastask1910,146,510,0001.000242Ogaki Kyoritsu Bank2336,100,000,0001.000	200	ENEOS Card	22	139,400,000,000	1.000
209 NTT East Japan (Flet internet) 17 335,000,000,000 1.000 211 Point Exchange 19 411,162,000 0.000 212 Gendama 19 411,162,000 0.167 215 Apple World 26 200,000,000 0.000 217 nimoca 20 126,400,000 1.000 227 TEPCO 16 1,400,900,000,000 N/A 232 GetMoney! 26 211,500,000 0.000 237 Saitama Risona Bank 23 70,000,000,000 1.000 238 MyVoice 19 178,000,000 0.000 239 Chance It 19 211,500,000 0.000 240 Kyu 19 914,000,000 0.000 241 Fastask 19 10,146,510,000 1.000 242 Ogaki Kyoritsu Bank 23 36,100,000,000 1.000	206	Kaetoku card	19	N/A	1.000
211Point Exchange19411,162,0000.000212Gendama19411,162,0000.167215Apple World26200,000,0000.000217nimoca20126,400,0001.000227TEPCO161,400,900,000,000N/A232GetMoney!26211,500,0000.000237Saitama Risona Bank2370,000,000,0001.000238MyVoice19178,000,0000.000239Chance It19211,500,0000.000240Ikyu19914,000,0001.000241Fastask1910,146,510,0001.000242Ogaki Kyoritsu Bank2336,100,000,0001.000	208	Cue Monitor	19	N/A	0.167
212Gendama19411,162,0000.167215Apple World26200,000,0000.000217nimoca20126,400,0001.000227TEPCO161,400,900,000,000N/A232GetMoney!26211,500,0000.000237Saitama Risona Bank2370,000,000,0001.000238MyVoice19178,000,0000.000239Chance It19211,500,0000.000240Ikyu19914,000,0000.000241Fastask1910,146,510,0001.000242Ogaki Kyoritsu Bank2336,100,000,0001.000	209	NTT East Japan (Flet internet)	17	335,000,000,000	1.000
215Apple World26200,000,0000.000217nimoca20126,400,0001.000227TEPCO161,400,900,000,000N/A232GetMoney!26211,500,0000.000237Saitama Risona Bank2370,000,000,0001.000238MyVoice19178,000,0000.000239Chance It19211,500,0000.000240Ikyu19914,000,0001.000241Fastask1910,146,510,0001.000242Ogaki Kyoritsu Bank2336,100,000,0001.000	211	Point Exchange	19	411,162,000	0.000
217ninoca20126,400,0001.000227TEPCO161,400,900,000,000N/A232GetMoney!26211,500,0000.000237Saitama Risona Bank2370,000,000,0001.000238MyVoice19178,000,0000.000239Chance It19211,500,0000.000240Ikyu19914,000,0000.000241Fastask1910,146,510,0001.000242Ogaki Kyoritsu Bank2336,100,000,0001.000	212	Gendama	19	411,162,000	0.167
227TEPCO161,400,900,000,000N/A232GetMoney!26211,500,0000.000237Saitama Risona Bank2370,000,000,0001.000238MyVoice19178,000,0000.000239Chance It19211,500,0000.000240Ikyu19914,000,0000.000241Fastask1910,146,510,0001.000242Ogaki Kyoritsu Bank2336,100,000,0001.000	215	Apple World	26	200,000,000	0.000
232GetMoney!26211,500,0000.000237Saitama Risona Bank2370,000,000,0001.000238MyVoice19178,000,0000.000239Chance It19211,500,0000.000240Ikyu19914,000,0000.000241Fastask1910,146,510,0001.000242Ogaki Kyoritsu Bank2336,100,000,0001.000	217	nimoca	20	126,400,000	1.000
237Saitama Risona Bank2370,000,000,0001.000238MyVoice19178,000,0000.000239Chance It19211,500,0000.000240Ikyu19914,000,0000.000241Fastask1910,146,510,0001.000242Ogaki Kyoritsu Bank2336,100,000,0001.000	227	TEPCO	16	1,400,900,000,000	N/A
238MyVoice19178,000,0000.000239Chance It19211,500,0000.000240Ikyu19914,000,0000.000241Fastask1910,146,510,0001.000242Ogaki Kyoritsu Bank2336,100,000,0001.000	232	GetMoney!	26	211,500,000	0.000
239Chance It19211,500,0000.000240Ikyu19914,000,0000.000241Fastask1910,146,510,0001.000242Ogaki Kyoritsu Bank2336,100,000,0001.000	237	Saitama Risona Bank	23	70,000,000,000	1.000
240Ikyu19914,000,0000.000241Fastask1910,146,510,0001.000242Ogaki Kyoritsu Bank2336,100,000,0001.000	238	MyVoice	19	178,000,000	0.000
241Fastask1910,146,510,0001.000242Ogaki Kyoritsu Bank2336,100,000,0001.000	239	Chance It	19	211,500,000	0.000
242 Ogaki Kyoritsu Bank 23 36,100,000,000 1.000	240	Ikyu	19	914,000,000	0.000
	241	Fastask	19	10,146,510,000	1.000
244 Juroku Bank 23 36,800,000,000 0.400	242	Ogaki Kyoritsu Bank	23	36,100,000,000	1.000
	244	Juroku Bank	23	36,800,000,000	0.400

Continued				
246	Ikeda Senshu Bank	23	50,700,000,000	1.000
248	Kinki Osaka Bank	23	389,071,000,000	1.000
253	For Travel	19	915,984,000	0.000
255	Tokopo	20	N/A	0.500
259	POINT-BOX	19	10,000,000	0.000
261	East Nippon Expressway Company	20	52,500,000,000	1.000
262	Apa Hotel	26	1,912,000,000	1.000
273	E Tour	26	260,500,000	0.167
284	Go to Dentist!	26	13,000,000	0.167
286	Boox Store	22	310,100,000	0.000
296	ANA Sky Coin	20	25,000,000,000	0.667
303	QooPo	13	28,534,000,000	N/A
307	My Acuvue	22	8,000,000,000	0.333

Table A2. Nine industries which operate LPs in Japan. Each industry ID is the same as in [5].

Industry ID	Industry Name
09	Manufacturing and electrical machinery, equipment and supplies
13	Miscellaneous manufacturing industries
16	Electricity, gas, heat supply and water
17	Video picture, sound information, broadcasting and communications
19	Information services
20	Transportation and postal activities
22	Retail trade
23	Finance and insurance
26	Miscellaneous non-manufacturing industries

of damage, where IND_i indicates LP_i 's belonging industry ID, $damage_i$ is the average damage amount of its industry and $rank_i$ indicates the LP's ranking score at Poitan.net. However, this might be somewhat artificial.

B.3.2. Expense

The proxy of expense is also calculated from METI's data by the same method used for the damage. Then, $expense_i$ ($i = 1, 2, \dots, 82$) is set.

B.3.3. Vulnerability

The metric of vulnerability is the same as [5] used. We used six requirements in the registration process, the authentication (login) process, and the back-up authentication process of each LP. Table A4 shows these six requirements. They computed the security score, sec_score_i , of LP_i as the ratio of "the number of satisfied requirements in LP_i " to "the number of requirements about which we can obtain data regarding LP_i ."

 sec_score_i represents how unsuccessful an attack is, so we can view sec_score_i as a metric for *anti*-vulnerability.

Table A3. Examples of METI's data about the IT damage amount [51].

									Damage	from ir	Damage from incidents (JPY)	(JPY)							
0	T Capital Size (JPY)	Total # of 1 Firms	# of responded firms	Under 0.5 million	0.5 million to 1 million	1 million r to 1.5 million r	1.5 2 million 2 to 2 million n	2 million 4 million to 4 to 6 million million		6 nillion m to 8 t nillion m	6 8 10 15 million million million million to 8 to 10 to 15 to 20 million million million million	10 nillion mi to 15 to nillion mi		20 million rr to 30 1 million rr	30 million r to 50 t million r	50 million to 100 million	Over 100 million	Not sure	Did not suffer
				# of firms	# of firms	# of firms	# of firms	# of firms	# of firms f	# of firms f	# of # firms fi	# of # firms fi	# of # firms fi	# of firms 1	# of firms	# of firms	# of firms	# of firms	# of firms
n	under 50 million	69	10	ε	-		ı	ı		ı	ı	,	ı	ı	ı			7	4
	50 million to 100 million	132	26	6	2			1		ı			ı		ı	ı	·	7	12
oivre —	100 million to 300 million	48	10	З	1	1	·	ı		ı	ı	ı	ı	ı	ī	ı	1	2	2
	300 million to 500 million	26	6	4	1			ı		ı								б	-
	500 million to 1 billion	18	9	4	·	,	ı	ı	ı	ı	_								-
	1 billion to 10 billion	39	15	5	1		ı	1	ı	ı		-	ı			ı	·	с	4
	over 10 billion	8	б	1	ı		ı	ı	ı	ı			ı		ı	ı	·		
n	unknown	1			,			,	ı	ı	·	,	ı	ı	ı	,	,	ī	,
L	Total	341	79	29	9	1	ı	2	ı	ı	1	7	ı	ı	ı	,	1	12	25
n I	under 50 million	65	5	З	ı		ı	ı	ı	ı	ı	ı	ı	ı	ı	ı	ı		7
ista v	50 million to 100 million	113	10	б	-		,			1				ı	·		,		5
 od p	100 million to 300 million	30	4	ю	,		·	·	ı	·		,	ı		ı		,		1
ana səi	300 million to 500 million	19	1		·		·		ı	ı			ı	ı	ı	·	·		
tion tivi: v	500 million to 1 billion	10	1	,	,	,	,	,		ī	,	,	,	ı	ı	'	,	-	'
atta act	1 billion to 10 billion	34	5	1	,			,		ŀ	,	,		ı	ı	,	,	0	7
o dsu	over 10 billion	15	9	7	ı	,	·	ı	ı	,	ı	ı	ı		ı	ı	ŀ	7	7
Lra C	unknown	1			,	·	·	·	·	ŀ		,			,		,	,	
Г	Total	287	32	12	1		·		ı	1		,		ı	ı		,	9	12

TableA4. Security requirer	tients in web authentications used for the calculation of sec_score [5].
Process	Requirements
Registration	 Trusted information (e.g. certified information, security code, information which is matched to certifiable document). Necessity of physical card or account. Implementation of additional security techniques (e.g. CAPTCHA, secret question).
Authentication (login)	- Data which increases difficulty to log into the account. (e.g. mobile number, physical card number, system generated ID).
Back-up authentication	- Trusted information.
(password recovery)	- Physical card or account number.

TableA4. Security requirements in web authentications used for the calculation of sec_score [5].

B.3.4. Normalization

Reference [5] did not normalize any parameters, but we normalize *damage* and *expense* with *capital size* as follows:

damage: $\log(damage_i)/\log(capital _ size_i)$, expense: $\log(expense_i)/\log(capital _ size_i)$.

Each LP-operating company has a lot of IT systems, and an LP system is just one of them. Since the empirical data of expense and damage is for all the IT systems of the company, some normalization would be necessary when we measure the expense and expense on its LP system.

Appendix C. Liquidity Definition at the Previous Research

We briefly describe how Jenjarrussakul and Matsuura [5] defined *liquidity* and used this metric.

Before they conducted quantitative analysis, they first considered the LPs security issues by industry. They listed 204domestic LPs and classified them into 9 industries. They drew a graph of the Japanese LP partnership network where each node indicates an industry. Since they were interest in how each industry node is connected, they checked the edge types—one-directional, opposite one-directional, or bidirectional—between industries and the average number of connecting LPs of all the LPs belonging to each industry.

In order to quantitatively examine which industry is more willing to connect with other industries via LP, they introduced a metric *liquidity* as a multiplier of the number of edge types, x, and the average number of partners regarding the LPs in a node, y:

$$liquidity = x * y$$
.

Then, using METI's data, they discussed the relation between liquidity and damage or security investment in the industry-wise level.

After this industry based discussion, they entered upon a LP divided discussion and carried on quantitative empirical analysis with the same liquidity definition above. However, this definition does not seem suitable and intuitively convincing when we consider how easily attackers convert the points into actual monetary profit when we consider the LP-wise situation divided from the industry-wise cluster.