

# An Improved Parameters Extraction Method for Dumbbell-Shaped Defected Ground Structure

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## Abstract

The paper presents an improved equivalent circuit parameters extraction method for the dumbbell-shaped defected ground structure (DGS). The new extraction parameters equations are obtained in closed-form expressions, which contain  $S_{11}$  and  $S_{21}$ . The DGS unit with center frequency of 5 GHz is designed and fabricated on a TLX substrate with thickness of 1 mm and dielectric constant of 2.55. The circuit simulated results are in good agreement with the measured results. This parameters extraction method can be widely used for the design and analysis of DGS.

**Keywords:** Defected Ground Structure, Equivalent Circuit, Parameters Extraction Method, Dumbbell-Shaped DGS

## 1. Introduction

In the late 1990s, defected ground structure (DGS) was firstly proposed by Korean scholar J. I. Park *et al.* [1]. It is based on the idea of photonic band-gap structure, and applied to the design of planar circuits. DGS is an etched periodic or non-periodic cascaded configuration defect in ground of a planar transmission line [2] (e.g microstrip, coplanar and conductor backed coplanar wave guide), which disturbs the shield current distribution in the ground plane. This disturbance will change characteristics of a transmission line such as the line capacitance and inductance to obtain the slow-wave effect and band-stop property [3-6]. DGS has been used for the control of an active microstrip antenna [7], improved efficiency of powers [8], performance enhancement of filters [9-10], and dividers [11].

There are two main methods for the design and analysis of DGS [2]. The commercially EM software is the main simulate software to design and analyze DGS, which is relatively slow and does not give any physical insight of the operating principle of DGS. On the contrary, the equivalent circuit method can quickly give the frequency responses of DGS by exacting equivalent circuit parameters. In general, DGS can be equivalent by three types of equivalent circuits [2,12-14]: 1) LC and LCR equivalent circuits, 2)  $\pi$  shaped equivalent circuit,

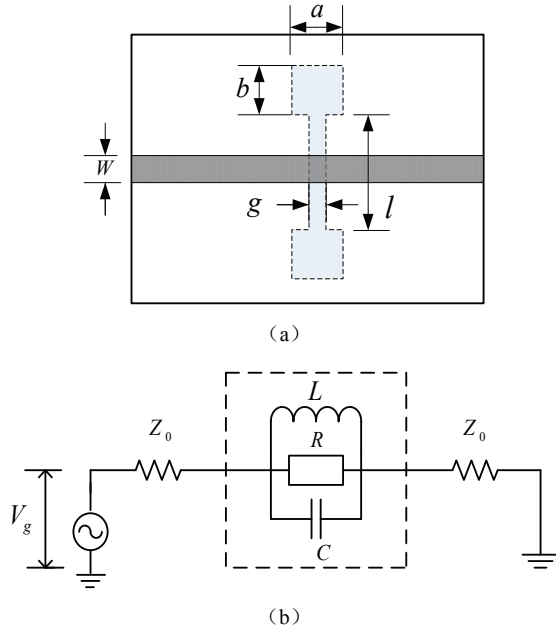
3) quasi-static equivalent circuit. The LC and LCR equivalent circuit are simple and most widely used [2]. however, the LCR equivalent circuit model can not provide the exact response curve, which should be in line with the measured or simulated results [1,15,16].

In this paper, based on the LCR equivalent circuits, an improved parameters extraction method is proposed, which uses the  $S_{11}$  and  $S_{21}$  information and can give better frequency responses of defected ground structure. To show the validity of the method, a dumbbell-shaped DGS unit was fabricated on a TLX substrate with 1mm thickness and 2.55 dielectric constant, and the measured results are in good agreement with the simulated results.

## 2. Parameters Extraction Method

The dumbbell-Shaped DGS [1] is composed of two  $a \times b$  rectangular defected areas,  $g \times l$  gaps and a narrow connecting slot wide etched areas in backside metallic ground plane, as shown in **Figure 1(a)**. DGS unit can be modeled by a parallel  $R$ ,  $L$ , and  $C$  resonant circuit connected to transmission lines at its both sides, as shown in **Figure 1(b)**.

The equivalent circuit parameters  $L$ ,  $C$ ,  $R$  of dumbbell-shaped DGS unit can be given by [1]:



**Figure 1. Dumbbell-shaped DGS unit and its equivalent circuit.**

$$C = \frac{\omega_c}{2Z_0(\omega_0^2 - \omega_c^2)} \quad (1)$$

$$L = \frac{1}{\omega_0^2 C} \quad (2)$$

$$R(S_{11}(\omega)) = \frac{2Z_0}{\sqrt{\frac{1}{|S_{11}(\omega)|^2} - \left(2Z_0\left(\omega C - \frac{1}{\omega L}\right)\right)^2} - 1} \quad (3)$$

where,  $\omega_0$  is the angular resonance frequency,  $\omega_c$  is the 3-dB cutoff angular frequency, and  $Z_0$  is the characteristic impedance of the microstrip line,  $S_{11}(\omega)$  is the input reflection coefficient of the equivalent circuit network.

In Equation (3), the parameter  $R$  is obtained by the magnitude of  $S_{11}(\omega)$ . In fact, it can also be found from Equation (4), which is derived from the  $S_{21}(\omega)$  variable. In general,  $R(S_{11}(\omega))$  is not equal to  $R(S_{21}(\omega))$ .

$$R(S_{21}(\omega)) = \frac{2Z_0}{\frac{|S_{21}(\omega)|^2}{1 - |S_{21}(\omega)|^2} + \sqrt{\left[\frac{|S_{21}(\omega)|}{1 - |S_{21}(\omega)|^2}\right]^2 - 4Z_0^2\left(\omega C - \frac{1}{\omega L}\right)^2}} \quad (4)$$

where,  $S_{21}(\omega)$  is the forward transmission coefficient of the equivalent circuit network.

Although the resistance  $R$  is the function of frequency, it is expected that  $R$  is independent frequency. Considering the main characteristics of DGS is single pole low-pass, the loss resistance  $R_{11}$  is determined by:

$$R_{11} = \frac{2Z_0 |S_{11}(\omega_0)|}{1 - |S_{11}(\omega_0)|} \quad (5)$$

where,  $\omega_0$  is the resonance frequency of DGS.

If the parameter  $R$  is obtained by the magnitude of  $S_{21}$ , then the parameter  $R_{21}$  is given by:

$$R_{21} = 2Z_0 \frac{1 - |S_{21}(\omega_0)|}{|S_{21}(\omega_0)|} \quad (6)$$

The resistance  $R_{11}$  obtained by Equation (5) is typically different from the resistance  $R_{21}$  obtained by Equation (6). In most literature, the resistance  $R$  in Figure 1 is obtained by Equation (5), that is  $R_{11}$ . This approach can guarantee the accuracy of  $S_{11}$ , however,  $S_{21}$  have a large error at the center frequent point. If  $S_{11}$  and  $S_{21}$  are used to extract the parameter  $R$ , the frequency responses can be better. The parameter value  $R$  is given by:

$$R = \frac{R_{11} + R_{21}}{2} \quad (7)$$

On the basis of the above principle, steps of the improved LCR equivalent circuit parameters extraction method for DGS are given as follows:

- 1) The resonant frequency  $\omega_0$ , the cut-off frequency  $\omega_c$  and the terminal impedance  $Z_0$  are obtained by frequency response curves;
- 2) Calculate the equivalent capacitance  $C$  and equivalent inductance  $L$  by Equations (1) and (2);
- 3) Calculate  $R_{11}$  and  $R_{21}$  by Equations (5) and (6);
- 4) The value of parameter  $R$  in equivalent circuit is obtained by Equation (7).

### 3. Results and Discussions

To show the validity of the method, the dumbbell-shaped DGS were designed at a fundamental resonant frequency of  $f_0 = 5$  GHz and fabricated on a TLX substrate with a thickness  $h = 1$  mm, transmission line width  $W = 2.82$  mm, and relative dielectric constant  $\epsilon_r = 2.55$ . The configuration parameters of DGS is  $a = 3$  mm,  $b = 5$  mm,

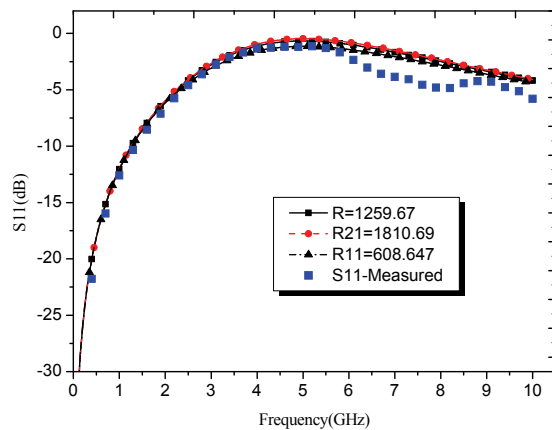
$g = 1$  mm,  $l = 11$  mm, respectively, as shown in **Figure 2**.

From the measured data, we have the scattering parameter values,  $S_{11}(\omega_0) = -1.147$  dB,  $S_{21}(\omega_0) = -25.624$  dB. According to the equivalent circuit parameter extraction steps in section II, the LCR equivalent circuit parameters are  $L = 3.969\mu\text{H}$ ,  $C = 0.2553\text{pF}$ ,  $R = 1259.67\Omega$  ( $R_{11} = 608.647\Omega$ ,  $R_{21} = 1810.69\Omega$ ), respectively.

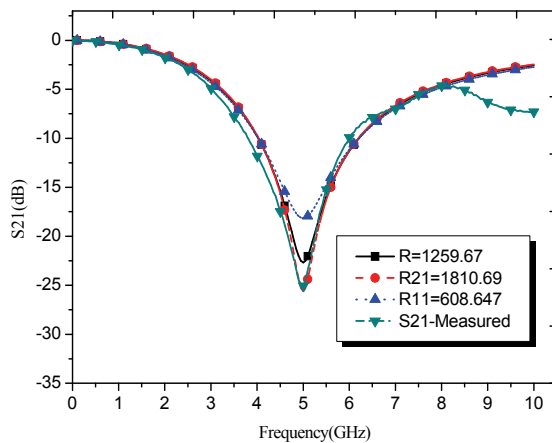
The measured results and equivalent circuit simulation results using the equivalent circuit parameters are shown in **Figure 3**. It can be seen that the equivalent circuit



**Figure 2.** Fabricated DGS unit at resonance frequency 5GHz.



(a)



(b)

**Figure 3.** Measured and equivalent circuit simulated S-parameters for various  $R$ . (a)  $S_{11}$  parameter; (b)  $S_{21}$  parameter.

**Table 1.** Evaluation equivalent circuit frequency responses and error for various resistance at center frequency.

Resistance	$S_{11}/\text{dB}$			$S_{21}/\text{dB}$		
	Circuit model	Measured	Error	Circuit model	Measured	Error
$R$	-0.664		0.483	-22.668		2.394
$R_{11}$	-1.146	-1.147	0.001	-18.155	-25.062	6.907
$R_{21}$	-0.467		0.680	-25.273		-0.211

simulation results show excellent agreement with measured results; they have the same resonance frequency. **Table 1** gives the S-parameters results of that comparison at the center frequency. When the resistance takes  $R_{11}$ , the accuracy of  $S_{11}$  can be ensured, but  $S_{21}$  have nearly 7dB error and if the resistance takes  $R_{21}$ , the accuracy of  $S_{21}$  can be ensured, but  $S_{11}$  have 0.68 dB error. Calculated the S-parameters by the proposed method, the errors of S-parameter can be smaller.

Measured results show that the improved LCR equivalent circuit parameter extraction method is effective, it can be used for DGS quick simulation and ensures higher accuracy.

## 4. Conclusions

The equivalent circuit has been widely applied to simulate the frequency responses of DGS by exacting equivalent circuit parameters. In this paper, an improved equivalent circuit parameters extraction method for dumb-bell-shaped DGS is proposed. Compared with the convenient methods, the proposed method can give the more accurate frequency response curves, it can be widely used in the design and analysis of DGS.

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