

Kinetics of Manganese Oxides Dissolution in Sulphuric Acid Solutions Containing Oxalic Acid

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ABSTRACT

The kinetics of the interaction of MnO_2 , Mn_2O_3 , and Mn_3O_4 , with sulphuric acid solutions and the effect of oxalic acid on this process are studied. As the sulphuric acid concentration is increased from 0.1 to 5 N, the dissolution rate of Mn_2O_3 , Mn_3O_4 to MnO_2 and Mn^{2+} ions decreases, whereas it increases with the concentration of Mn^{2+} ions. Upon the addition of H_2O_x , the complete dissolution of Mn_3O_4 occurs more quickly. The reaction order with respect to the H^+ and O_2^{2-} ions is $+0.5 \pm 0.1$. A mechanism of MnO_2 dissolution promotion by O_2^{2-} is proposed. The dissolution rate was

found to depend on the concentrations of $MnHO_x^+$ and HO_x^- ions and was highest at pH 1.6 ± 0.2. A rate law and mechanism are suggested for manganese oxides dissolution.

Keywords: Dual Electrical Layer; Acid-Base Model; The Kinetics of Manganese Oxide Dissolution; Oxalic Acid

1. Introduction

To accelerate the etching of manganese alloys and optimise the dressing and leaching of manganese oxide ores, it is necessary to understand the mechanisms of these processes [1-12]. The most promising method of improving the effectiveness of the etching of manganese oxides is reductive dissolution by various complexing agents [5-10]. However, the rate-limiting step has not been identified in most works on the reductive dissolution of oxides.

2. Material and Method

In the study of dissolution kinetics, we used extra-pure γ -MnO₂, Mn₂O₃ and Mn₃O₄ powder with a particle size of 60 - 80 μ m. A sample of oxide weighing 0.362 \pm 0.005 g was placed in a temperature-controlled reaction vessel containing 0.750 \pm 0.005 l of an aqueous solution of sulphuric and oxalic acids. During dissolution, the mixture was stirred magnetically at $\nu = 600$ - 700 rpm. In preliminary runs, the dissolution rate was almost independent of ν for ν > 500 rpm. The pH of the solution was adjusted by adding sulphuric acid. The concentration of sulphuric acid was varied between 0.005 and 2.5 mol/l. Most measurements were carried out at 353 K. The solution was sampled at regular intervals using an N16 Schott

filter. The manganese in solution was determined photocolourimetrically as the complex with formaldoxime [13]. The non-stoichiometric composition change during the dissolution of oxides phases in sulphuric acid was measured by a technique described in a previous study [14].

3. Results and Discussion

3.1. Analysis of the Kinetic Data of Manganese Oxide Dissolution (Mn₂O₃, Mn₃O₄ and MnO₂) in Sulphuric Acid

As seen in **Figures 1-3**, a remarkable feature of the interaction of manganese oxide with sulphuric acid is that the oxide is dissolved incompletely. The process is terminated at $\alpha = 0.66$ (α is the ratio of the concentration of Mn²⁺ ions in the solution to the total manganese in the oxide sample).

Based on the data shown in **Figures 1** and **2**, the dissolution rates of Mn₂O₃ and Mn₃O₄ decrease with increasing sulphuric acid concentration.

3.2. Calculation of the Specific Rate of Dissolution

Using these curves (**Figures 1-3**), we derived the specific dissolution rate W, the apparent orders of reaction with respect to hydrogen ions and manganese (II) ions, and

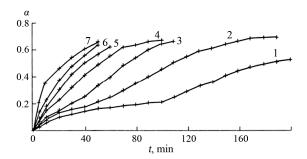


Figure 1. Dependence of the extent of dissolution of $\rm Mn_3O_4$ (α) on the time t at 353 K for various sulphuric acid concentrations: (1) 2.5, (2) 1.5, (3) 1.0, (4) 0.75, (5) 0.5, (6) 0.25 and (7) 0.05 mol/l. Points—experimental data, lines—calculation of the chain mechanism equation.

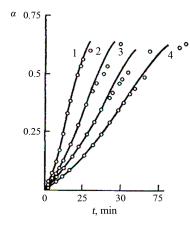


Figure 2. Dependence of the extent of dissolution of $\rm Mn_2O_3$ (α) on the time t at 353 K for various sulphuric acid concentrations: (1) 0.1, (2) 0.51, (3) 0.91 (4) 2.71 mol/l. Points—experimental data, lines—calculation of the chain mechanism equation.

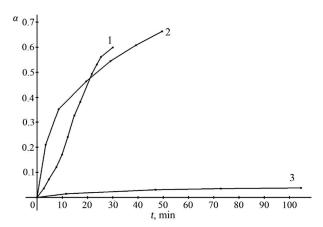


Figure 3. Dependence of the extent of dissolution of manganese oxides (α) on the time t at 353 K, 0.05 mol/l sulphuric acid: (1) Mn₂O₃, (2) Mn₃O₄, (3) MnO₂.

the activation energy of dissolution by testing various heterogeneous kinetic models (**Table 1**) using affine transformations. First, we plotted α against $t/t_{0.5}$, where $t_{0.5}$ is the time required for 50% of the sample to dissolve.

Table 1. Heterogeneous kinetic models and their equations.

Model	Equation	
1) First-order reaction	$-\ln\left(1-\frac{\alpha}{\alpha_{\infty}}\right) = Wt$	
2) Autocatalysis	$-\ln\left(\frac{\alpha}{1-\alpha}\right) = W\left(t - t_{0.5}\right)$	
3) Chain reaction	$-\ln(1-\alpha) = A\sinh(Wt)$	
4) Erofeev-Avrami	$-\ln(1-\alpha) = (Wt)^2$	
5) Shrinking sphere	$1 - \left(1 - \alpha\right)^{1/3} = Wt$	

To select the heterogeneous kinetics equations that best fit the experimental curves, the obtained α versus $t/t_{0.5}$ dependences were described by various theoretical dependences.

The choice of the equation routinely began with the most simple equation, (e). The compressed sphere equation is not applicable because the curves are s-shaped and correspond to the Fisher criterion.

The best results were obtained with the Hill function (1), which corresponds to the formation of active sites at the dislocations and grain boundaries of the oxide phase [15].

The theoretical lines well describe the experimental points (**Figures 1** and **2**), proving the applicability of the chosen Equation (1).

$$-\ln(1-\alpha) = A \cdot \sin h(Wt)$$

$$-\ln\left[\frac{-\ln(1-\alpha) + (A^2 + \ln^2(1-\alpha))^{0.5}}{A}\right] = Wt \qquad (1)$$

$$\frac{d\alpha}{dt} = W(1-\alpha)(A^2 + \ln^2(1-\alpha))^{0.5}$$

$$\frac{t}{t_{0.5}} = \frac{\ln(-\ln(1-\alpha) + (A^2 + \ln^2(1-\alpha)^{0.5})/A)}{\ln(0.6931 + (A^2 + \ln^2(1-0.5)^{0.5})/A)} \qquad (2)$$

The obtained A values (A = 0.2) were used to calculate the specific rate of dissolution (disproportionation).

$$W = \tau_{0.5} / t_{0.5} \tag{3}$$

where $\tau_{0.5} = Wt_{0.5}(\tau_{0.5} = 0.65)$.

Using Equation (1) it is possible to calculate the specific rate of dissolution for the given concentration (**Tables 2** and **3**)

The activation energy of the process calculated from the log W versus 1/T dependence gives $E_a = 80 \pm 0.5$ kJ/mol.

We found that the dissolution rates of Mn_2O_3 and Mn_3O_4 decrease as $[H^+]$ is increased, which is attributed to the disproportionation reactions, resulting in incomeplete dissolution.

Table 2. Kinetic constants for the dissolution of Mn_3O_4 in sulphuric acid solutions as a function of H_2SO_4 concentration.

[H ₂ SO ₄], mol/l	T = 353 K		
	t _{0.5} , min	$W \pm 0.2 \times 10^{-2}, \text{min}^{-1}$	
0.05	17	3.7	
0.25	30	2.1	
0.50	43	1.4	
0.75	52	1.2	
1.00	64	1.0	
1.50	84	0.8	
2.50	140	0.5	

Table 3. Kinetic constants for the dissolution of Mn_2O_3 in sulphuric acid solutions as a function of H_2SO_4 concentration.

[H CO 11/1	T = 353 K		
[H ₂ SO ₄], mol/l	t _{0.5} , min	$W \pm 0.2 \times 10^{-2}, \text{min}^{-1}$	
2.58	17	6.09	
3.68	24	4.31	
4.73	31	3.34	
6.12	39	2.67	
7.51	51	2.25	
9.08	68	1.52	
10.12	93	1.11	

The process can be represented as disproportionate according to the following scheme:

$$MnO_{x_{1}} + 2\frac{x - x_{1}}{x - 1}H^{+} = \frac{x_{1} - 1}{x - 1}MnO_{x} + \frac{x - x_{1}}{x - 1}Mn^{2+} + \frac{x - x_{1}}{x - 1}H_{2}O$$
(4)

where x_1 and x are the initial and final x = [O]/[Mn] ratios for the oxide phase.

Equation (4), **Figure 4**, and **Table 4** both indicate a dependence between the extent of dissolution (α) and non-stoichiometric composition (x) with time, which can be expressed using the following equation [14]:

$$\alpha = \left[\frac{x_2 - 1}{(x_2 - x_1)} \right] - \left[\frac{(x_2 - 1)(1 - x_1)}{(x_2 - x_1)} \right] \left[\frac{1}{(1 - x)} \right]$$
 (5)

The orders of the disproportionation reaction determined from $\log W$ versus pH and logw versus $\log[Mn^{2+}]$ are as follows:

$$\frac{\partial \log W}{\partial \log \left[\mathbf{H}^{+} \right]} = -0.5$$

$$\frac{\partial \log W}{\partial \log \left[\mathbf{Mn}^{2+} \right]} = +0.5$$
(6)

Table 4. Dependence of the extent of dissolution Mn_2O_3 and non-stoichiometric index (x) of oxygen in MnO_x for time (t) in sulphuric acid at various temperatures.

t, min -	$\alpha \pm 0.2$	$x \pm 0.03$	$\alpha \pm 0.04$	x
	343 K		333 K	
30	0.075	1.52	0.02	1.51
60	0.19	1.55	0.04	1.52
90	0.39	1.62	0.06	1.53
120	0.65	1.74	0.14	1.57
150	0.76	1.81	0.27	1.62
180	0.84	1.86	0.40	1.68
210	0.88	1.89	0.50	1.72
240	0.92	1.93	0.55	1.75
270			0.64	1.79
300			0.70	1.82
330			0.76	1.84
360			0.83	1.86
390			0.9	1.88

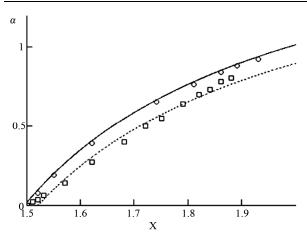


Figure 4. Dependence of the extent of dissolution (α) of $\mathrm{Mn_2O_3}$ on the stoichiometric composition of manganese oxides $(x = [\mathrm{O}]/[\mathrm{Mn}])$. Lines—calculations from Equation (2), points—experimental data.

A preliminary consideration of the effect of different factors on the kinetics of the process shows that the obtained curves are rectified in the 1/W versus $[H^+]$ and 1/W versus $[Mn^{2+}]$ coordinates. This observation allows us to describe the interaction rate of manganese oxides with H_2SO_4 by the equation:

$$W = W^{0} \left[H^{+} \right]^{-0.5} \left[Mn^{2+} \right]^{0.5} =$$

$$W^{0} \frac{K_{a1}}{\left[H^{+} \right] + K_{a1}} \frac{\left[Mn^{2+} \right]}{\left[Mn^{2+} \right] + K_{a2}}$$
(7)

where K_{al} , K_{a2} and W^0 are kinetic constants.

We propose a Mn₂O₃ dissolution mechanism that explains the negative orders for protons and positive orders

for manganese ions [6]:

1) Hydration of an oxide surface:

$$Mn_2O_3 + H_2O \rightarrow 2MnOOH^0$$
 (8)

2) Adsorption of protons:

$$MnOOH^{0} + H^{+} + A^{-} \rightarrow MnOOH_{2}^{+} + A_{aa}^{-}$$
 (9)

3) Dissolution from active sites:

$$MnOOH_{2}^{+} + A^{-} \rightarrow MnO_{aq}^{+} + H_{2}O + A_{aq}^{-}$$
 (10)

4) Volumetric reaction:

$$2MnO_{aa}^{+} \rightarrow Mn_{aa}^{2+} + MnO_{2}$$
 (11)

Integrally:

$$2MnOOH_{ag}^{+} + 2H_{ag}^{+} \rightarrow Mn_{ag}^{2+} + MnO_{2} + H_{2}O$$
 (12)

The disproportionation of Mn₃O₄ characterised by two-stage kinetics (**Figure 1**) can be represented by two overall reactions:

$$Mn_3O_4 + 2H^+ \rightarrow 2MnOOH + Mn^{2+},$$
 (13)

$$2MnOOH + 2H^{+} \rightarrow MnO_{2} + Mn^{2+} + 2H_{2}O$$
 (14)

In both cases, low-solubility MnO_2 is formed on the oxide surfaces.

Therefore, it is important to determine the conditions that promote the efficient dissolution MnO₂.

The kinetics of manganese dioxide dissolution were then studied in sulphuric acid solutions containing oxalic acid.

3.3. Kinetics Analysis of the Effect of Oxalic Acid on the Rate of the Interaction and Dissolution of MnO₂ in Sulphuric Acid Solutions

Influence of concentration of oxalic acid. The results of the dissolution of manganese dioxide in various concentrations of oxalic acid are shown in **Figure 5**. Based on **Figure 4**, increasing the oxalate ion concentration increases the extent of dissolution (α) . Thus, full dissolution is observed.

The specific dissolution rate increases with oxalic acid concentration at a constant sulphuric acid concentration. The plot of this dependence (**Figure 5**) resembles that of an adsorption isotherm. The dissolution rate follows the empirical equation:

$$W = W_{\text{max}} \frac{C_{\text{Ox}}}{C_{\text{Ox}} + K_a} \tag{15}$$

The Langmuir and Freundlich isotherms describe the experimental data with identical accuracies; therefore, the following is used as a first approximation:

$$W = W_{\text{max}} \frac{C_{\text{Ox}}}{C_{\text{Ox}} + K_a} \approx W_{\text{max}} \left[C_{\text{Ox}} \right]^n$$
 (16)

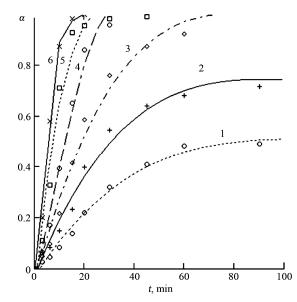


Figure 5. Dependence of the extent of MnO₂ dissolution (a) on the time (t) at $[H_2SO_4] = 0.05$ mol/l and various oxalic acid concentrations: (1) 0.050, (2) 0.075, (3) 0.010, (4) 0.020, (5) 0.030, and (6) 0.04 mol/l (T = 353 K, pH = 1.5, V = 750 ml).

where *n* is the reaction order with respect to oxalic acid, and $C_{\rm Ox}$ is the total concentration of all forms of oxalic acid (n = 0.66, $K_{\rm a} = 0.026$ mol/l, $W_{\rm max} = 0.66$ min⁻¹).

When C_{Ox} tends to infinity, the process rate reaches its maximum, W_{max} .

Influence of pH at constant oxalic acid concentration. The dissolution rate of manganese (IV), (III) oxides was studied as a function of pH in solutions containing 0.005 M oxalic acid. We found that W is highest at pH 1.6 \pm 0.2 (**Figure 6**).

From the kinetic data obtained, the following relation was derived for the dissolution of MnO₂ in oxalic acid [16-19]:

$$W = W_{\text{max}} \theta_{\text{H}^+} \theta_{\text{HOy}^-} \theta_{\text{MnHOy}^+}, \qquad (17)$$

where θ_i is the coverage of the MnO₂ surface by species i

3.4. Modelling the Manganese (IV) Oxide Dissolution Mechanism

According to the site-binding model [16-19], dissolution proceeds via the formation of intermediates when the surface is positively charged.

Scheme 1:

$$\equiv \operatorname{Mn} \longrightarrow \operatorname{OH}_{(s)}^{0} + \operatorname{A}^{-} + \operatorname{H}^{+} \xrightarrow{k_{1}} \equiv \operatorname{MnOH}_{2}^{0} \cdots \operatorname{A}_{(s)}^{-}$$

$$\equiv \operatorname{MnOH}_{2}^{+} \cdots \operatorname{A}_{(s)}^{-} + \operatorname{HO}_{x} \xrightarrow{k_{2}} \equiv \operatorname{MnOH}_{2}^{+} \cdots \operatorname{HOx}_{(s)}^{-}$$

 $+A^{-} \xrightarrow{k_3}$ dissolved products

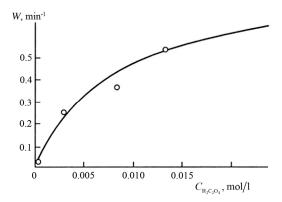


Figure 6. Specific rate of MnO_2 dissolution as a function of oxalic acid concentration at T=353 K and pH 1.5. Lines—calculatio using Equations (13) and (16) or (20), points—experimental data.

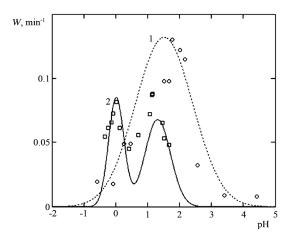


Figure 7. Specific rate of $\rm MnO_2$ (1) and $\rm Mn_2O_3$ (2) dissolution as function of pH at $C_{\rm Ox}$ =0.005 mol/l and T = 353 K. Lines—calculatio using Equation (17), points—experimental data.

here, θ_1 is the fraction of the unbound oxide surface and θ_2 and θ_3 are the coverages of the surface by $\equiv \text{MnOH}_2^+ \cdots \text{A}_{(s)}^-$ and $\equiv \text{MnOH}_2^+ \cdots \text{HO}x_{(s)}^-$ complexes, respectively. In this case, the dissolution rate may be limited by the passage of the intermediate complex into solution, which occurs at a rate proportional to θ_3 . W and θ_3 can be determined as functions of various parameters by applying the method based on a steady-state approximation and the principle of detailed balancing [16-19] to the steps preceding the rate-limiting step.

The dissolution rate at constant pH is given by: $W = k_3 \theta_3 =$

$$= W_{\text{max}} \frac{\left[\text{HOx}^{-}\right] \left[\text{H}^{+}\right]}{\left[\text{HOx}^{-}\right] \left[\text{H}^{+}\right] + K_{a1} K_{a2} \left[\text{HOx}^{-}\right] + K_{a2} \left[\text{A}^{-}\right] \left[\text{H}^{+}\right]}$$

$$= W \frac{\left[\text{H}^{+}\right]}{\left[\text{H}^{+}\right] + K_{a1}} \frac{\left[\text{HOx}^{-}\right]}{\left[\text{HOx}^{-}\right] + K_{a2}}$$
(14)

with $W_{\rm max}=0.37\pm0.05~{\rm min}^{-1}$, $K_{al}=\{k_{-1}k_{-2}+k_3(k_{-1}+k_2)\}/(k_1k_2)=2\times10^{-3}~{\rm mol/l}$ and $K_{a2}=(k_{-2}+k_3)/k_2=4\times10^{-3}~{\rm mol/l}$. Here, K_{a1} and K_{a2} are the equilibrium constants of adsorption at the dioxide-electrolyte interface. $\left[{\rm HOx}^-\right]=\theta_{{\rm HOx}^-}C_{{\rm Ox}^{2-}}$, where $\theta_{{\rm HOy}^-}$ is the fraction of ${\rm HOx}^-$ ions in solution:

$$\theta_{\text{HOx}^{-}} = \frac{\left[\text{HOx}^{-}\right]}{C_{\text{Ox}}} = \frac{1}{\left(\beta_{4} \left\lceil \text{H}^{+} \right\rceil + 1\right)\beta_{5} \left\lceil \text{H}^{+} \right\rceil + 1} \qquad (20)$$

where β_4 and β_5 are the dissociation constants of oxalic acid: $\log \beta_4 = 1.271$, $\log \beta_5 = 4.266$ [12-16].

4. Conclusions

The dissolution of manganese oxides in sulphuric acid proceeds to partial completion, whereas the addition of oxalic acid allows it to proceed to completion.

Thus, the performed experimental and theoretical investigation of the dissolution and disproportionation processes of manganese oxides in H_2SO_4 solutions in the presence of H_2O_x indicated that the dissolution mechanism involves the adsorption of H_2O_x followed by the reduction of the surface layers of the oxide.

The dissolution of manganese dioxide in sulphuric acid solutions containing oxalic acid can be accelerated considerably. The dissolution rate is affected by the HO_x^- , $MnHO_x^+$, and H^+ ions. The maximum dissolution rate is observed at pH 1.6 and a 1:5 concentration ratio for the manganese ions and oxalic ions.

The first step in manganese dioxide dissolution is the coadsorption of HO_x^- and $MnHO_x^+$ ions, followed by charge transfer. The resulting $MnHO_x^+$ ions pass into solution. The rate-limiting step is three-dimensional nucleation on the MnO_2 surface.

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