

Regression Models of the Impact of Rockmass and Blast Design Variations on the Effectiveness of Iron Ore Surface Blasting

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Abstract

The desired economics of hard rock surface mining is mainly determined by the parameters of process design which minimize the overall cost per tonne of the rock mined in drilling, blasting, handling and primary crushing in given rockmass conditions. The most effective parameters of process design could be established based on the regression models of the cumulative influence of rockmass and mine design parameters on the overall cost per tonne of the rock drilled, blasted, handled and crushed. These models could be developed from the huge data accumulated worldwide on the costs per tonne of hard rock surface mining in drilling, blasting, handling and primary crushing vs the parameters of rockmass and mine design. This paper only dwelt on the development of regression models for oversize generation, blasthole productivity and blasting cost for iron ore surface mines, whose data is available. The SPSS standard statistical correlation – regression analysis software was used in the analysis. Interpretation of the models generated shows that the individual effects of the determinant rockmass and blast design parameters on oversize generation, blasthole productivity and blasting cost are all in compliance with the findings of other researchers and the theory of explosive rock fragmentation and could be used for the estimation of oversize generation, blasthole productivity and blasting cost in rockmass and blast design conditions similar to those of the iron ore surface mines examined in this study. However, the regression models obtained here could not be used alone for the optimization of blast design because most of the determinant parameters also have conflicting effect on the other processes of drilling, handling and primary crushing the blasted rock. Also, the quality and content of the regression models could be enhanced further by increasing the content of rockmass and blast design parameters and the volume of data considered in the regression analysis.

Keywords: Blasting Effectiveness, Oversize generation, Blasthole Productivity, Blasting Cost, Rockmass Parameters, Blast Design Parameters, Regression Models

1. Introduction

Oversize generation, blasthole productivity and cost per tonne of rock blasted are the three main indices of hard rock surface blasting effectiveness and are dependent on rockmass and blast design parameters. The determinant parameters differ from one mine to the other and some of the blast design parameters could be regulated to deliver the desired blasting effectiveness. The individual influence of the determinant parameters on blasting effectiveness has been studied by several authors [1-13], but

their cumulative influence on the same is yet to be formulated. However, the huge statistical data generated from the well organized and documented large scale hard rock surface mines operating in variable conditions worldwide constitutes the only readily available resource which could be used for the analysis and generation of the regression models of oversize generation, blasthole productivity and cost per tonne of the rock blasted fit on rockmass and blast design parameters. For example, the statistical data available on several large scale iron ore surface mines which operated in the former Soviet Union

could be used to develop regression models of iron ore surface blasting effectiveness. Therefore, aim in this paper is to develop the regression models of oversize generation, blasthole productivity and cost per tonne of the rock blasted fit on rockmass and blast design parameters of iron ore surface blasting, based on the blasting data published for the year 1970 for 10 large scale iron ore surface mines which operated in the former Soviet Union [6].

2. Indices of Blasting Effectiveness

2.1. Oversize Generation

Oversize generation is a quality index of blasting effectiveness, characterizing the percentage of the blasted rock product (V_H^+ , %) which requires secondary blasting before it could be allowed into the downstream processes of handling and primary crushing. Blast design parameters which are not compatible with the rockmass conditions of blasting constitute the main cause of excessive oversize generation. Excessive oversize generation means extra cost on conducting the inefficient secondary blasting. The desired economics of hard rock surface mining could be achieved from the parameters of blast design delivering the minimum oversize and overall cost per tonne in drilling, blasting, handling and primary crushing in given rockmass conditions [1,7,8,10-12].

2.2. Blasthole Productivity

Blasthole productivity ($P_B, m^3/m$) is a quantity index of blasting effectiveness, characterizing the volume of rock blasted per unit of blasthole length. The maximum blasthole productivity achievable from hard rock surface blasting is calculated according to the formula shown on (1) [1,7,9-11]:

$$P_B = W_s \times E_B \times \frac{BH}{H}, m^3/m \quad (1)$$

Where: W_s - burden at bench toe (m); E_B - blasthole spacing (m); BH - bench height (m); H - blasthole length (m).

Blasthole productivity could increase as a result of the increase of $W_s \times E_B$. The increase of $W_s \times E_B$ could also cause the increase of oversize generation and the cost on secondary blasting but the total volume of drilling work ($m/block$) decreases. The desired economics of hard rock surface mining could be achieved from the parameters of blast design which deliver the maximum blasthole productivity and the minimum overall cost per tonne in drilling, blasting, handling and primary crushing.

2.3. Blasting Cost

Blasting cost $C_B, RUB/ton$ is the overall quality index of blasting effectiveness and one of the components of the overall cost per tonne of hard rock surface mining in drilling, blasting, handling and primary crushing. This index is characterizes the overall cost per tonne of the rock blasted in charging and firing and secondary blasting [1,10,11]. The desired economics of hard rock surface mining could be achieved from the blast design parameters delivering the established production capacity of the mine at the maximum blasthole productivity, minimum generation of oversize, minimum blasting and overall costs per tonne of the rock mined in drilling, blasting, handling and primary crushing.

3. Regression Models of Blasting Effectiveness

3.1. Description

The levels of oversize generation, blasthole productivity and cost per tonne of the rock blasted are determined by the parameters of rockmass and blast design. Any of the rockmass and blast design parameters presented on **Table 1** could influence on blasting effectiveness [1,3-6, 10-12]. The effects of blast design parameters on the costs per tonne of the rock blasted in drilling, blasting, handling and primary crushing are conflicting. Therefore, optimum blast design parameters should be the ones delivering the established production capacity of the mine at the minimum overall cost per tonne of the rock blasted in drilling, blasting, handling and primary crushing. Consequently, the assessment of blasting effectiveness and optimization of blast design should be based on the mathematical models of the cumulative influence of rockmass and blast design parameters on oversize generation, blasthole productivity and cost per tonne of the rock blasted. These models are one of the techno-economic models of processes in the mining industry, which are developed using the method of regression analysis [13]. However, the effectiveness of regression analysis depends on the availability of the necessary content and volume of data in respect of the costs per tonne of the rock blasted in drilling, blasting, handling and primary crushing vs the parameters of rock mass and blast design.

3.2. Development

Regression models for the assessment of large scale iron ore surface blasting effectiveness were generated from the data available on the statistics of rockmass and blast

Table 1. Determinant parameters.

Rock parameters	Blast design parameters
<p>Compressive strength σ_c, Mpa ; Volume density $\rho, T/m^3$; Degree of jointing; P-wave seismic velocity $c, m/s$; blastability constant s; etc.</p>	<u>Bench geometry</u>
	Blasthole diameter Φ, mm ; Bench height BH, m ; hole length H, m ; burden at bench toe W_s, m ; subdrilling U, m ; blasthole spacing E_b, m ; row spacing E_r, m ; hole inclination i^0 ; etc.
	<u>Loading style and firing method</u>
	Powder factor $q, kg/m^3$; stemming B_s, m ; charge design; number of rows per blast N_{RB} ; initiation system; delay interval $t, m/s$; volume of rock blasted per blast $Q_v, 10^3 m^3$; etc.
	<u>Explosive properties</u>
	Type; relative strength e ; charge diameter Φ_c ; detonation velocity V_d ; etc. <u>Number of blasts per year</u> N_{BY} ; etc.

design parameters of 10 large scale iron ore surface mines in the former Soviet Union, whose average values for the year 1970 are shown on the appendix. The SPSS standard statistical correlation-regression analysis software was used to generate the regressions models of oversize generation V_H^+ , blasthole productivity P_B and blasting cost C_B fit on the parameters of rockmass (hardness and density) and blast design (bench toe burden, blasthole spacing, rows spacing, bench height, subdrilling, stemming, powder factor, number of rows blasted, volume of rock blasted per blast and number of blasts per year). The models generated are shown on (2,3).

$$V_H^+ = f \left(\begin{matrix} \sigma_c, \rho, W_s, E_b, E_r, BH, U, \\ B_s, q, N_{RB}, Q_v, N_{BY} \end{matrix} \right) \quad (2)$$

$$P_B = f \left(\begin{matrix} \sigma_c, \rho, W_s, E_b, E_r, BH, U, \\ B_s, q, N_{RB}, Q_v, N_{BY} \end{matrix} \right) \quad (3)$$

$$C_B = f \left(\begin{matrix} \sigma_c, \rho, W_s, E_b, E_r, BH, U, \\ B_s, q, N_{RB}, Q_v, N_{BY} \end{matrix} \right) \quad (4)$$

Important rockmass and blast design parameters such as, rock blastability, rock P-wave seismic velocity, type of explosive, blasthole diameter, charge diameter, deto-

nation velocity, charge design; type of initiation system and delay interval (s), etc. were not considered in the regression analysis because they were almost the same for the 10 mines examined. Beside, their data were not available.

Model 1: Over size generation, %

The value of R^2 is 0.884 showing that the five predictors entered in the regression analysis account for 88.4% of the variation in the percentage of oversize, while the F change is 6.093 and significant value is 0.052 slightly greater than 0.05 showing that the model is to a great extent significantly better at predicting the percentage of oversize generation than using the mean as the best guess. The following variables were found to be significant for the generation of oversize %: rock density, volume of rock blasted per blast, blasthole spacing and bench height. Compressive rock strength is the only variable found insignificant and was not shown on **Table 2**.

Explanation of variables and their coefficients

1) Rock density ($b = 10.704$): This value indicates that as rock density increases by one unit, percentage of oversize increases by 10.704 units. This interpretation is true only if the effects of other variables in the model are held constant. The t -test ($t = 1.307$) associated with this value indicates that it is significant ($*P < 0.05$). Rock density is making a significant contribution to the model.

Table 2. Significant variables and their coefficients.

Variables	b	Std. Error	Beta	t
Rock density	10.704	3.703	1.477	2.891
Volume blasted	-.012	.003	-2.885	-3.578
Hole spacing	2.136	.696	1.639	3.071
Bench height	-.377	.109	-.945	-3.478

Note $R^2 = 0.884$

2) Volume of rock blasted per blast ($b = -0.012$): This value indicates that as volume of rock blasted in a round increases by one unit, percentage of oversize decreases by 0.012 units. This interpretation is true only if the effects of other variables in the model are held constant. The t -test ($t = -3.578$) associated with this value indicates that it is significant ($*p < 0.05$). The volume of rock blasted per blast is making a significant contribution to the model.

3) Blasthole spacing ($b = 2.136$): This value indicates that as blasthole spacing increases by one unit, percentage oversize increases by 2.136 units. This interpretation is true only if the effects of other variables in the model are held constant. The t -test ($t = 3.071$) associated with this value indicates that it is significant ($*p < 0.05$). Blasthole spacing is making a significant contribution to the model.

4) Bench height ($b = -0.377$): This value indicates that as bench height increases by one unit, percentage oversize decreases by 0.377 units. This interpretation is true only if the effects of other variables in the model are held constant. The t -test ($t = -3.478$) associated with this value indicates that it is significant ($*p > .05$). Bench height is making a significant contribution to the model.

5) Compressive rock strength ($b = 0.245$): This value indicates that as compressive rock strength increases by one unit, percentage of oversize increases by 0.245 units. This interpretation is true only if the effects of other variables in the model are held constant. The t -test ($t = 1.307$) associated with this value indicates that it is not significant ($*p < 0.05$). The contribution of compressive rock strength to the model is not significant and therefore was removed.

Model 2: Blasthole productivity, m^3/m

The value of R^2 is 1.000 showing that the eight predictors entered in the regression analysis account for 100.00% of the variation in the blasthole productivity. The F change is 1435.690 and is much greater than 1, showing that the model is significantly better at predicting blasthole productivity than using the mean as the best

guess (significant $*p < 0.05$). The variables found to be significant for the blasthole productivity include: burden at bench toe, blasthole spacing, powder factor, rock hardness, subdrilling and stemming height. The other variables included in the analysis: rock density and volume of rock blasted were not found to be significant and were not shown in **Table 3** of results.

Explanation of variables and their coefficients

1) Burden at bench toe ($b = 6.844$): This value indicates that as burden at bench toe increases by one unit, blasthole productivity increases by 6.844 units. This interpretation is true only if the effects of other variables in the model are held constant. The t -test ($t = 28.83$) associated with this value indicates that it is significant ($*P < 0.05$). Burden at bench is making a significant contribution to the model.

2) Blasthole spacing ($b = -15.028$): This value indicates that as blasthole spacing increases by one unit, blasthole productivity decreases by 15.028 units. This interpretation is true only if the effects of other variables in the model are held constant. The t -test ($t = -34.888$) associated with this value indicates that it is significant ($*P < 0.05$). Average blasthole spacing is making a significant contribution to the model.

3) Powder factor ($b = -71.266$): This value indicates that as powder factor increases by one unit, blasthole productivity decreases by 71.266 units. This interpretation is true only if the effects of other variables in the model are held constant. The t -test ($t = -40.918$) associated with this value indicates that it is significant ($*P < 0.05$). Powder factor is making a significant contribution to the model.

4) Compressive rock strength ($b = -1.781$): This value indicates that as average rock hardness increases by one unit, blasthole productivity decreases by 1.781 units. This interpretation is true only if the effects of other variables in the model are held constant. The t -test

Table 3. Significant variables and their coefficients.

Variables	b	Std. Error	Beta	t
Toe burden	6.844	.237	1.044	28.830
Hole spacing	-15.028	.431	-1.381	-34.888
Powder factor	-71.266	1.742	-.767	-40.918
Rock strength	-1.781	.140	-.373	-12.744
Subdrilling	15.552	.374	.447	41.537
Stemming	-3.089	.217	-.685	-14.234

Note $R^2 = 1.000$, $*p < 0.05$

($t = -12.744$) associated with this value indicates that it is significant ($*P < 0.05$). Rock hardness is making a significant contribution to the model.

5) Subdrilling ($b = -15.552$): This value indicates that as subdrilling increases by one unit, blasthole productivity increases by 15.552 units. This interpretation is true only if the effects of other variables in the model are held constant. The t -test ($t = -41.537$) associated with this value indicates that it is significant ($*P < 0.05$). Subdrilling is making a significant contribution to the model.

6) Stemming height ($b = -3.089$): This value indicates that as average stemming increases by one unit, blasthole productivity decreases by 3.089 units. This interpretation is true only if the effects of other variables in the model are held constant. The t -test ($t = 0.045$) associated with this value indicates that it is significant ($*P < 0.05$). Stemming height is making a significant contribution to the model.

7) Rock density ($b = 2.702$): This value indicates that as rock density increases by one unit, blasthole productivity increases by 2.702 units. This interpretation is true only if the effects of other variables in the model are held constant. The t -test ($t = 0.487$) associated with this value indicates that it is not significant ($*P < 0.05$). The contribution of the rock density to the model is not significant and therefore was removed from the model.

8) Volume of rock blasted per blast ($b = 2.702$): This value indicates that as volume of rock blasted per blast increases by one unit, blasthole productivity increases by 2.702 units. This interpretation is true only if the effects of other variables in the model are held constant. The t -test ($t = 9.144$) associated with this value indicates that it is not significant ($*P < 0.05$). The contribution of the volume of rock blasted to the model was not significant and therefore was removed from the model.

Model 3: Maximum blasting Cost, RUB/T

The value of R^2 is 0.993 showing that the seven predictors entered in the regression analysis account for 99.3% of the variation in the maximum blasting cost per cubic meter of blasting, while the F change is 40.617 and is greater than one showing that the model is signifi-

cantly better at predicting the maximum cost than using the mean as the best guess (significant $*P < 0.05$). The variables found to be significant for the maximum blasting cost, RUB/T include: Compressive rock strength, rock density, volume of rock blasted per blast and burden at bench toe. The other variables which were included in the analysis: bench height, powder factor and blasthole spacing were not found to be significant and are not shown on **Table 4**.

Explanation of each variable and their coefficients

1) Compressive rock strength ($b = 39.886$): This value indicates that as compressive rock strength increases by one unit, maximum blasting cost increases by 39.89 units. This interpretation is true only if the effects of other variables in the model are held constant. The t -test associated with this value indicates that it is significant ($*P < 0.05$). Compressive rock strength is making a significant contribution to the model.

2) Rock density ($b = 851.646$): This value indicates that as rock density increases by one unit, maximum blasting cost decreases by 851.65 units. This interpretation is true only if the effects of other variables in the model are held constant. The t -test associated with this value indicates that it is not significant ($*P < 0.05$). Rock density is making a significant contribution to the model.

3) Volume of rock blasted per blast ($b = -0.910$): This value indicates that as volume of rock blasted per blast increases by one unit, maximum blasting cost decreases by 0.91 units. This interpretation is true only if the effects of other variables in the model are held constant. The t -test associated with this value indicates that it is significant ($*P < 0.05$). The volume of rock blasted per blast is making a significant contribution to the model.

4) Burden at bench toe ($b = 33.91$): This value indicates that as burden at bench toe increases by one unit, maximum blasting cost decreases by 33.91 units. This interpretation is true only if the effects of other variables in the model are held constant. The t -test associated with this value indicates that it is significant ($*P < 0.05$). Burden at bench toe is making a significant contribution to the model.

Table 4. Significant variables and their coefficients.

Variables	b	Std. Error	Beta	t
Constant	-3699.047	416.790		-8.875
Rock strength	39.886	5.285	.917	7.548
Rock density	851.646	99.082	1.545	8.595
Volume blasted	-0.910	.090	-2.924	-10.135
Toe burden	33.910	5.993	.568	5.658

Note $R^2 = 0.993$, $*p < 0.05$

5) Bench height ($b = -0.274$): This value indicates that as bench height increases by one unit, maximum blasting cost decreases by 0.274 units. This interpretation is true only if the effects of other variables in the model are held constant. The t -test ($t = -0.054$) associated with this value indicates that it is not significant ($*P < 0.05$). The contribution of bench height to the model is not significant and therefore was removed from the model.

6) Powder factor ($b = 362.108$): This value indicates that as powder factor increases by one unit, maximum blasting cost increases by 362.11 units. This interpretation is true only if the effects of other variables in the model are held constant. The t -test ($t = 3.625$) associated with this value indicates that it is not significant ($*P < 0.05$). The contribution of the powder factor to the model is not significant and therefore was removed from the model.

7) Blasthole spacing ($B_s = 71.095$): This value indicates that as blasthole spacing increases by one unit, maximum blasting cost increases by 71.10 units. This interpretation is true only if the effects of other variables in the model are held constant. The t -test ($t = 3.04$) associated with this value indicates that it is not significant ($*P < 0.05$). The contribution of the blasthole spacing to the model is not significant and therefore was removed from the model.

The estimated regression models for the assessment of oversize generation, blasthole productivity and blasting cost for iron ore surface blasting are as shown on formulas (5), (6) and (7) respectively.

$$V_H^+ = 10.704\rho - 0.012Q_v + 2.136E_B - 0.377BH, \% \quad (5)$$

$$P_B = 6.844W_s - 15.028E_B - 71.266q - 1.781\sigma_c + 15.552U - 3.089B_s, \frac{m^3}{m}, \quad (6)$$

$$C_B = -3699.05 + 39.89\sigma_c + 851.65\rho - 0.91Q_v + 71.10E_B, \frac{RUB}{T} \quad (7)$$

4. Discussion of Results

The impact of rockmass and blast design parameters on the effectiveness of iron ore surface blasting could be explained in accordance to the estimated regression models obtained for oversize generation, blasthole productivity and blasting cost as follows:

4.1. Rock Density

As rock density increases, generation of oversize in-

creases, resulting to the increase of blasting cost on secondary blasting. Several authors including [2,11] also noted that rock density hampers the transfer of energy into the rock mass and thus the blastability, fragmentation and cost of blasting.

4.2. Compressive Rock Strength

As compressive rock strength increases, blasthole productivity decreases, resulting to the increase of blasting cost due to the decrease of blasthole productivity. As the compressive rock strength increases, rocks become harder to break, resulting to the decrease of blasthole productivity.

4.3. Powder Factor

As powder factor increases, blasthole productivity decreases because as powder factor increases, stemming height decreases and the energy wasted on blown out holes also increases. However, the increase of blasting cost due to the increase of powder factor is not significant because the powder factors assessed are closely marched with the rockmass and other blast design parameters of the mines.

4.4. Burden at Bench Toe

As burden at bench toe increases, productivity of blasthole increases, however, effect on blasting cost is positive but insignificant probably because change itself is not significant.

4.5. Blasthole Spacing

As blasthole spacing increases, oversize generation increases and blasthole productivity goes down because, as blasthole spacing increases, utilization of the collective rock crushing capability of neighboring blastholes on the middle of their spacing decreases. As a consequence the observed increase of blasting cost is associated with the increase of secondary blasting and the decrease of blasthole productivity arising from the underutilization of the collective rock crushing capability of neighboring blastholes.

4.6. Stemming Height

As stemming height increases, blasthole productivity decreases because change is accompanied by poor fragmentation of the upper parts of benches. However, change and its effect are small and not felt on the cost of blasting.

4.7. Subdrilling

As subdrilling increases, blasthole productivity increases but changes are small and not felt on the degree of fragmentation and the cost of blasting.

4.8. Bench Height

The increase of bench height reduces oversize generation because as bench height increases, the easy to displace and deform rock also increases as noted by Ash (1977). However change is small and its effect on blasting cost improvement is not significant.

4.9. Volume of Rock Blasted per Blasting Round

As the volume of rock blasted per blast increases, oversize generation and blasting cost decreases because as volume increases number of blastholes and rows fired in one blast also increases and as a result increases the secondary fragmentation caused by the collisions of rock masses moving from the increased number of blasthole and rows.

The above interpretation allows concluding that the individual effects of the investigated parameters of rockmass and blast design parameters on oversize generation, blasthole productivity and blasting cost are in compliance with the findings of other researchers and the theory of explosive rock fragmentation.

5. Conclusions and Recommendations

The regression models developed here could be used for the estimation of oversize generation, blasthole productivity and blasting cost in rockmass and blast design conditions similar to those of the 10 large scale iron ore surface mines examined in this paper.

However, alone, the regression models obtained here could not be used for the optimization of blast design because most of the determinant parameters also have conflicting effect on the other processes of the rock blasted in drilling, handling and primary crushing. Also the quality and content of the regression models could be enhanced further by increasing the content of rockmass and blast design parameters and the volume of data con-

sidered in the regression analysis.

6. References

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Appendix: Data variations of iron ore large scale mines in the former Soviet Union.

MINE VA- RIABLES GOK	ROCKMASS VARIATIONS			BLAST DESIGN VARIATIONS			
	2	3	4	5	6	7	8
	Rock Hardness σ_c [Mpa]	Rock density ρ [T/m ³]	Bench Toe Burden W_s [m]	Blasthole spacing E_B [m]	Row Spacing E_R [m]	Bench height BH [m]	Sub drilling U [m]
Krivoi South	130	3.35	11.25	8.25	7.5	15	2.5
Krivoi Central	120	3.0	9.5	6.5	7.25	15	2.5
Northern	130	2.95	9	7	7	11	2.5
NovoKrivoi	130	3.09	9.5	6.75	6.75	15	3.25
Inguleski	140	3.15	11	7	6.5	13.5	2.5
Sokolovsko	115	3.2	7.25	6.25	5.75	15	2.5
Kachkanarski	105	2.98	10	7	7.75	13.5	2.75
Kovdorski	90	3.03	9.5	6.5	6	12.5	2.75
Olenegorsk	135	2.9	10.5	6.5	6.5	12	2.75
Korshovski	95	2.98	11.5	8.5	8.5	20	2.75

BLAST DESIGN VARIATIONS				INDICES OF BLASTING EFFECTIVENESS			
9	10	11	12	13	14	15	16
Stemming B_s [m]	Powder factor q [kg/m ³]	Number of rows blasted N_{RB}	No. of Blasts per year N_{BY}	Rock Blasted Q_V [10 ³ m ³]	Oversize genera- tion V_H^+ [%]	Blasthole Prod- uctivity P_B [m ³ /m]	Blasting Cost [RUB/T]
4	0.693	5	26	867	0.05	51.4	\$101.00
4.25	0.629	4	89	209	0.05	44.5	\$150.00
0	0.8	4	50	299.8	0.56	36.2	\$145.00
5.5	0.616	3	31	296	0.058	51.4	\$215.00
5.5	0.758	6	28	430	0.42	39.9	\$283.00
6	0.63	4	131	198.9	1.33	28.4	\$214.00
5.25	0.809	3	67	96.1	2.25	26.5	\$304.00
5.25	0.69	5	120	42	2.1	39.8	\$231.00
5.5	0.68	4	120	45	2.6	38.2	\$330.00
6.5	0.523	4	60	253	0.633	38.8	\$162.00