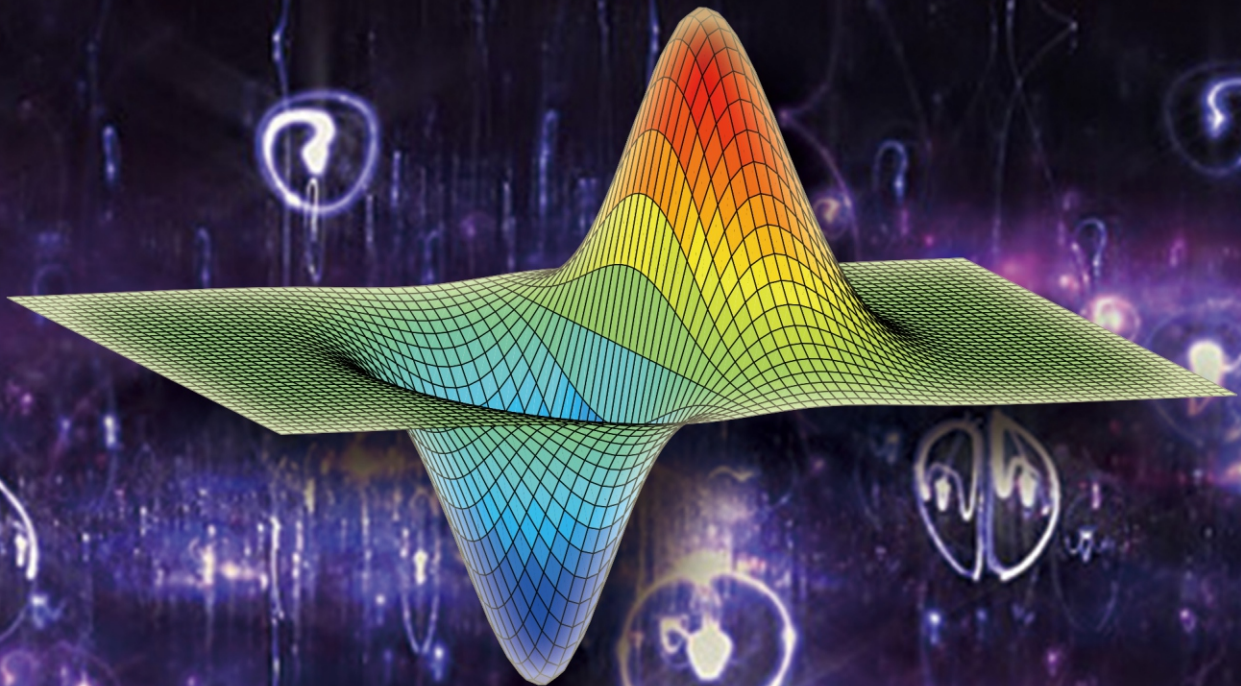


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# Table of Contents

**Volume 8    Number 7**

**July 2018**

**Anisotropic Continuum Stored Energy Functional Solved  
by Lie Group and Differential Geometry**

F. Z. Zhao.....631

**The Generalized Pythagorean Comma Harmonic Powers of a Fundamental  
Frequency Are Equivalent the Standing Wave Harmonic Fraction System**

D. Chakeres.....652

**Brief Investigation on Square Root of a Node of  $T_3$  Tree**

G. H. Chen, J. H. Li.....666

**The Proof of the Generalized Piemann's Hypothesis**

S. V. Matnyak.....672

**There Are Infinitely Many Mersenne Composite Numbers with Prime Exponents**

F. S. Liu.....687

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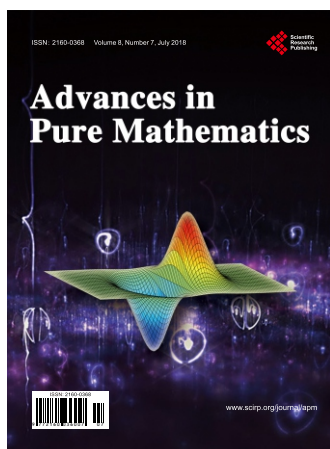
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