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[^0]:    The figure on the front cover is from the article published in Advances in Pure Mathematics, 2013, Vol. 3, No. 7, pp. 627-632 by Fengying Wei and Cuiying Li.

